

Name:

Enrollment No:



UNIVERSITY OF PETROLEUM AND ENERGY STUDIES

End Semester Examination, December 2021

Programme Name: B.Tech GIE

Course Name : Statistical Methods in Geosciences

Course Code: PEGS 3014

Semester : V

Time : 03 hrs

Max. Marks : 100

Section A (All questions are compulsory. Tables are given at the end of the paper)																									
1.	Telephone calls arrive at an office on an average 2 calls per minute following a Poisson process. Let X be the waiting time in terms of minutes until the first five calls arrive. Write the mean and variance of X.	[4]	CO1																						
2.	Consider the following function $f(x) = \begin{cases} e^{-x} , & \text{if } x \geq 0 \\ 0 , & \text{if } x < 0 \end{cases}$ Is the function a probability density function? If yes, then find a. the probability $P(1 < x < 2)$ b. the value of cumulative distribution function at 2.	[4]	CO2																						
3.	Consider a sample 5, 8.5, 12, 15, 7, 9, 7.5, 6.5, 10.5 from a population following normal distribution with unknown mean μ and variance 4. Write a 95 percent confidence interval for μ .	[4]	CO3																						
4.	Assuming second order stationary condition and intrinsic hypothesis, write relation between semivariogram and covariance functions.	[4]	CO4																						
5.	Write the hypothesis for simple kriging.	[4]	CO5																						
SECTION B (Q1-Q4 are compulsory and Q4 has an internal choice. Tables are given at the end of the paper)																									
1.	Let us consider time series of two variables, say it, temperature and pressure. Explain with an example, how you will form joint distribution of these two random variables. Write two advantages of the joint distribution citing the temperature and pressure.	[10]	CO1																						
2.	Use the method of least squares to fit a regression line to the accompanying data points. <table border="1" data-bbox="302 1650 1297 1730"><tr><td>x</td><td>-1</td><td>0</td><td>2</td><td>-2</td><td>5</td><td>6</td><td>8</td><td>11</td><td>12</td><td>-3</td></tr><tr><td>y</td><td>-5</td><td>-4</td><td>2</td><td>-7</td><td>6</td><td>9</td><td>13</td><td>21</td><td>20</td><td>-1</td></tr></table> Test if the slope is significant at 0.05.	x	-1	0	2	-2	5	6	8	11	12	-3	y	-5	-4	2	-7	6	9	13	21	20	-1	[10]	CO2
x	-1	0	2	-2	5	6	8	11	12	-3															
y	-5	-4	2	-7	6	9	13	21	20	-1															

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3.	<p>In a certain condition temperature of two different types of iron bars (Bar A and Bar B) are measured as following in degrees Celsius: Bar A: 36, 42, 40, 51, 37, 36, 35, 40, 53, 48, 50, 52, 55, 52 Bar B: 58, 61, 63, 64, 59, 60, 65, 63, 68, 70, 78, 65, 59, 62</p> <p>Suppose that it is known that the temperature of Bar A in that conditions is normally distributed with unknown mean μ_1 and known variance $\sigma_1^2 = 40$, whereas the corresponding distribution for Bar B is normal with unknown mean μ_2 and known variance $\sigma_2^2 = 40$. Determine a 95 percent confidence interval for $\mu_1 - \mu_2$.</p>	[10]	CO3																												
4.	<p>Explain the semivariogram function. Discuss any three semivariogram models.</p> <p style="text-align: center;">OR</p> <p>Discuss applications and usefulness of kriging. Explain the general steps involved in ordinary kriging algorithm.</p>	[10]	CO3																												
SECTION C (Q1-2 are compulsory and each have an internal choice. Tables are given at the end of the paper)																															
1.	<p>A geologist claims that mean temperature in certain region inside the Earth in kelvin is 345K. To verify the claim, following temperatures are obtained at randomly selected locations in the region: 340, 356, 332, 362, 318, 344, 386, 402, 322, 360, 362, 354, 340, 372, 338, 375, 364, 355, 324, and 370. Do the data contradict the geologist's claim at 0.05 significance level?</p> <p style="text-align: center;">OR</p> <p>Let us consider two independent random variables X and Y, following normal distribution with unknown means and unknown but equal variances. Test the hypothesis for the equality of two means against the alternative hypothesis that they are not equal at 0.05 significance level. Use the following observations for X and Y.</p> <p>X: 1071, 1076, 1070, 1083, 1082, 1067, 1078, 1080, 1075, 1084, 1075, 1080 Y: 1074, 1069, 1075, 1067, 1068, 1079, 1082, 1064, 1070, 1073, 1072, 1075</p>	[20]	CO4																												
2.	<p>Use simple kriging to estimate the value of $Z(x_0)$ at $x_0 = (180, 120)$. Given $E[Z(x)] = 110$ and the covariance function $2000 * \exp(\frac{-h}{250})$.</p> <table border="1" data-bbox="415 1440 1089 1598"><thead><tr><th></th><th>X</th><th>Y</th><th>Z</th></tr></thead><tbody><tr><td>x_1</td><td>387</td><td>72</td><td>50</td></tr><tr><td>x_2</td><td>392</td><td>81</td><td>56</td></tr><tr><td>x_3</td><td>388</td><td>56</td><td>52</td></tr></tbody></table> <p style="text-align: center;">OR</p> <p>Use ordinary kriging to estimate the value of $Z(x_0)$ at $x_0 = (180, 120)$. Given, covariance function as $2000 * \exp(\frac{-h}{250})$.</p> <table border="1" data-bbox="415 1724 1089 1845"><thead><tr><th></th><th>X</th><th>Y</th><th>Z</th></tr></thead><tbody><tr><td>x_1</td><td>387</td><td>72</td><td>50</td></tr><tr><td>x_2</td><td>392</td><td>81</td><td>55</td></tr></tbody></table>		X	Y	Z	x_1	387	72	50	x_2	392	81	56	x_3	388	56	52		X	Y	Z	x_1	387	72	50	x_2	392	81	55	[20]	CO5
	X	Y	Z																												
x_1	387	72	50																												
x_2	392	81	56																												
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	X	Y	Z																												
x_1	387	72	50																												
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STANDARD NORMAL DISTRIBUTION: Table Values Represent AREA to the LEFT of the Z score.

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.9	.00005	.00005	.00004	.00004	.00004	.00004	.00004	.00004	.00003	.00003
-3.8	.00007	.00007	.00007	.00006	.00006	.00006	.00006	.00005	.00005	.00005
-3.7	.00011	.00010	.00010	.00010	.00009	.00009	.00008	.00008	.00008	.00008
-3.6	.00016	.00015	.00015	.00014	.00014	.00013	.00013	.00012	.00012	.00011
-3.5	.00023	.00022	.00022	.00021	.00020	.00019	.00019	.00018	.00017	.00017
-3.4	.00034	.00032	.00031	.00030	.00029	.00028	.00027	.00026	.00025	.00024
-3.3	.00048	.00047	.00045	.00043	.00042	.00040	.00039	.00038	.00036	.00035
-3.2	.00069	.00066	.00064	.00062	.00060	.00058	.00056	.00054	.00052	.00050
-3.1	.00097	.00094	.00090	.00087	.00084	.00082	.00079	.00076	.00074	.00071
-3.0	.00135	.00131	.00126	.00122	.00118	.00114	.00111	.00107	.00104	.00100
-2.9	.00187	.00181	.00175	.00169	.00164	.00159	.00154	.00149	.00144	.00139
-2.8	.00256	.00248	.00240	.00233	.00226	.00219	.00212	.00205	.00199	.00193
-2.7	.00347	.00336	.00326	.00317	.00307	.00298	.00289	.00280	.00272	.00264
-2.6	.00466	.00453	.00440	.00427	.00415	.00402	.00391	.00379	.00368	.00357
-2.5	.00621	.00604	.00587	.00570	.00554	.00539	.00523	.00508	.00494	.00480
-2.4	.00820	.00798	.00776	.00755	.00734	.00714	.00695	.00676	.00657	.00639
-2.3	.01072	.01044	.01017	.00990	.00964	.00939	.00914	.00889	.00866	.00842
-2.2	.01390	.01355	.01321	.01287	.01255	.01222	.01191	.01160	.01130	.01101
-2.1	.01786	.01743	.01700	.01659	.01618	.01578	.01539	.01500	.01463	.01426
-2.0	.02275	.02222	.02169	.02118	.02068	.02018	.01970	.01923	.01876	.01831
-1.9	.02872	.02807	.02743	.02680	.02619	.02559	.02500	.02442	.02385	.02330
-1.8	.03593	.03515	.03438	.03362	.03288	.03216	.03144	.03074	.03005	.02938
-1.7	.04457	.04363	.04272	.04182	.04093	.04006	.03920	.03836	.03754	.03673
-1.6	.05480	.05370	.05262	.05155	.05050	.04947	.04846	.04746	.04648	.04551
-1.5	.06681	.06552	.06426	.06301	.06178	.06057	.05938	.05821	.05705	.05592
-1.4	.08076	.07927	.07780	.07636	.07493	.07353	.07215	.07078	.06944	.06811
-1.3	.09680	.09510	.09342	.09176	.09012	.08851	.08691	.08534	.08379	.08226
-1.2	.11507	.11314	.11123	.10935	.10749	.10565	.10383	.10204	.10027	.09853
-1.1	.13567	.13350	.13136	.12924	.12714	.12507	.12302	.12100	.11900	.11702
-1.0	.15866	.15625	.15386	.15151	.14917	.14686	.14457	.14231	.14007	.13786
-0.9	.18406	.18141	.17879	.17619	.17361	.17106	.16853	.16602	.16354	.16109
-0.8	.21186	.20897	.20611	.20327	.20045	.19766	.19489	.19215	.18943	.18673
-0.7	.24196	.23885	.23576	.23270	.22965	.22663	.22363	.22065	.21770	.21476
-0.6	.27425	.27093	.26763	.26435	.26109	.25785	.25463	.25143	.24825	.24510
-0.5	.30854	.30503	.30153	.29806	.29460	.29116	.28774	.28434	.28096	.27760
-0.4	.34458	.34090	.33724	.33360	.32997	.32636	.32276	.31918	.31561	.31207
-0.3	.38209	.37828	.37448	.37070	.36693	.36317	.35942	.35569	.35197	.34827
-0.2	.42074	.41683	.41294	.40905	.40517	.40129	.39743	.39358	.38974	.38591
-0.1	.46017	.45620	.45224	.44828	.44433	.44038	.43644	.43251	.42858	.42465
-0.0	.50000	.49601	.49202	.48803	.48405	.48006	.47608	.47210	.46812	.46414

TABLE A-3		<i>t</i> Distribution: Critical <i>t</i> Values				
	0.005	0.01	Area in One Tail			
			0.025	0.05	0.10	
Degrees of Freedom	Area in Two Tails					
	0.01	0.02	0.05	0.10	0.20	
1	63.657	31.821	12.706	6.314	3.078	
2	9.925	6.965	4.303	2.920	1.886	
3	5.841	4.541	3.182	2.353	1.638	
4	4.604	3.747	2.776	2.132	1.533	
5	4.032	3.365	2.571	2.015	1.476	
6	3.707	3.143	2.447	1.943	1.440	
7	3.499	2.998	2.365	1.895	1.415	
8	3.355	2.896	2.306	1.860	1.397	
9	3.250	2.821	2.262	1.833	1.383	
10	3.169	2.764	2.228	1.812	1.372	
11	3.106	2.718	2.201	1.796	1.363	
12	3.055	2.681	2.179	1.782	1.356	
13	3.012	2.650	2.160	1.771	1.350	
14	2.977	2.624	2.145	1.761	1.345	
15	2.947	2.602	2.131	1.753	1.341	
16	2.921	2.583	2.120	1.746	1.337	
17	2.898	2.567	2.110	1.740	1.333	
18	2.878	2.552	2.101	1.734	1.330	
19	2.861	2.539	2.093	1.729	1.328	
20	2.845	2.528	2.086	1.725	1.325	
21	2.831	2.518	2.080	1.721	1.323	
22	2.819	2.508	2.074	1.717	1.321	
23	2.807	2.500	2.069	1.714	1.319	
24	2.797	2.492	2.064	1.711	1.318	
25	2.787	2.485	2.060	1.708	1.316	
26	2.779	2.479	2.056	1.706	1.315	
27	2.771	2.473	2.052	1.703	1.314	
28	2.763	2.467	2.048	1.701	1.313	
29	2.756	2.462	2.045	1.699	1.311	
30	2.750	2.457	2.042	1.697	1.310	
31	2.744	2.453	2.040	1.696	1.309	
32	2.738	2.449	2.037	1.694	1.309	
34	2.728	2.441	2.032	1.691	1.307	
36	2.719	2.434	2.028	1.688	1.306	
38	2.712	2.429	2.024	1.686	1.304	
40	2.704	2.423	2.021	1.684	1.303	
45	2.690	2.412	2.014	1.679	1.301	
50	2.678	2.403	2.009	1.676	1.299	
55	2.668	2.396	2.004	1.673	1.297	
60	2.660	2.390	2.000	1.671	1.296	
65	2.654	2.385	1.997	1.669	1.295	
70	2.648	2.381	1.994	1.667	1.294	
75	2.643	2.377	1.992	1.665	1.293	
80	2.639	2.374	1.990	1.664	1.292	
90	2.632	2.368	1.987	1.662	1.291	
100	2.626	2.364	1.984	1.660	1.290	
200	2.601	2.345	1.972	1.653	1.286	
300	2.592	2.339	1.968	1.650	1.284	
400	2.588	2.336	1.966	1.649	1.284	
500	2.586	2.334	1.965	1.648	1.283	
750	2.582	2.331	1.963	1.647	1.283	
1000	2.581	2.330	1.962	1.646	1.282	
2000	2.578	2.328	1.961	1.646	1.282	
Large	2.576	2.326	1.960	1.645	1.282	

