# CONTROLLER DESIGN FOR RCTA AIRCRAFT USING PARAMETER ESTIMATION TO INTEGRATE NAVIGATIONAL TECHNIQUE

A Thesis submitted to the UPES

For the Award of Doctor of Philosophy in Aerospace Engineering

> By Roli Jaiswal

Dec. 2022

SUPERVISOR (s)

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### Oct.2023

# DECLARATION

I declare that the thesis entitled "CONTROLLER DESIGN FOR RCTA AIRCRAFT USING PARAMETER ESTIMATION TO INTEGRATE NAVIGATIONAL TECHNIQUE" has been prepared by me under the guidance of D r. Om Prakash, Professor, Department of Aerospace Engineering, UPES, and D r. Sudhir Kumar Chaturvedi, Associate Professor, Department of Aerospace Engineering, UPES. No part of this thesis has formed the basis for the award of any degree or fellowship previously.

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# CERTIFICATE

I certify that Roli Jaiswal has prepared her thesis entitled "CONTROLLER DESIGN FOR RCTA AIRCRAFT USING PARAMETER ESTIMATION TO INTEGRATE NAVIGATIONAL TECHNIQUE", for the award of PhD degree of the UPES, under my guidance. She has carried out the work at School of Engineering, UPES.

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# Dedicated to My family,

# Motivated by My Beloved Husband

# ABSTRACT

System Identification is the input /output model interface to develop a mathematical model in presence of noise, disruptions, etc. These random observations in terms of process and measurement noise are distorted due to sensors, and external disturbances. Handling imperfect measurements is simplified by evaluating the parameters of the system using statistical techniques. In the past years, system Identification has expanded its growth due to its application in designing controllers, health monitoring, and analysis of dynamic systems, making system fully autonomous, and fault-tolerant. Some of the traditional methods for linear systems in the frequency/ time domain are FFT, ML, and LS. System Id is applied to study the time-variant tracking behavior of vehicle subsystems in real time to update system modeling by parameter estimation in a continuous interval to detect sensor fault, and system failure [1][2][3]. The research work displays the result of the aerodynamic parameters of Hansa-III evaluated by applying the Maximum Likelihood algorithm.

Multiple numbers datasets were collected during the flight test of Hansa-III whereas, eight data sets were finalized for parameter estimation[10]. The Terminology HA resembles 'Hansa-III', L is Longitudinal, and numerals '1-8' defines the number of data sets such as HAL1, HAL2, HAL3..... and so on. The Flight test was conducted by executing several control input forms such as Multi-step 3211 Input, Doublet Input, and Pulse Input. For longitudinal, the letter(s) accompanied by 'L' such as 'M' correspond to multi-step, 'D' as a doublet, and 'P' as pulse elevator control inputs.

The result exhibited in form of non-dimensional derivatives using the Maximum Likelihood method are considerately accurate and the value of the larger number of datasets are found close to wind tunnel values as correct calibration of the sensors before the flight test is the necessary step that needs to be executed to acquire a good quality of flight data. File processing of generated data gives information that  $C_{L_{\alpha}}$ ,  $C_{m_{\alpha}}$ ,  $C_{m_{\delta e}}$ ,  $C_{D_0}$ ,  $C_{m_0}$ ,  $C_{m_q}$  are termed as strong derivatives whereas weak parameters  $C_{L_{\delta e}}$ ,  $C_{L_q}$ ,  $C_{D_{\delta e}}$  affects in negligible amount as compared to strong so deviation in the value from wind-tunnel is neglected. It is found that there is a maximum departure in the wind-tunnel values for the Pulse Input form when comparing with Multi-step and

Doublet therefore Multi-step Input is more appropriate among all three Input forms. The type of control input (Multi-step, Doublet or Pulse) influences the estimates negligibly if the control input is appropriately excited to generate the data with proper information and frequency contents. Once the values of strong and weak derivatives are estimated then the Validation process is exercised to validate the result of derivatives that came from the wind tunnel and Maximum Likelihood methodology.

As system Identification expanded its application to design controllers thus the development of an autopilot for applications in defence, aerial surveillance, and transportation is a cause of to design of PID Controller. In the context of attitude controller design, the aircraft is modelled in longitudinal motion and the state-space matrix is formulated, and the PID controller is designed on MATLAB environment using Control System Toolbox satisfying design requirement. The time and frequency domain characteristics of different approaches such as Pole-Placement, Root-Locus, and Linear Quadratic Regulator are compared to get fruitful results. The gain parameters are optimized by comparing closed-loop PID tuning approaches such as ZN, Modified ZN, Tyreus- luyben, Astrum- Haglund for pitch control. The solution of these tuning approaches is analysed in form of gains K p, K i, K d as The constant steady-state error is brought on by K p, which also improves steady-state tracking fidelity and lessens the system's sensitivity while parameter variation. K d refers to the system- stability but acquires poor steady-state feedback, and K I have the characteristic of good steady-state response but leads to system instability. The Transfer function of PID consists of two zeros in the numerator, one pole is located at the origin in the denominator which makes the overall system highly stable. The response of the tuning technique, Astrum -Haglund is undamped oscillatory motion as it does not contain a derivative filter that leads to system instability. The response of Tyreus-Luyben experiences the larger value of K<sub>d</sub> that influences overall system parameters thus aircraft stability is increased but the steady-state value is difficult to attain. The gain values of ZN and Modified ZN are compared and depict that both controllers approach steady state rapidly and features of stability but modified ZN exhibits the finest result as the controller satisfies design requirements and approaches steady state close to zero.

The Design of the Flight control System involves classical and modern approaches. The simplest way to design a controller is using SISO (Single Input Single Output) Systems but systems applicable for industries are MIMO (Multi Input Multi Output), which are more complex[1]

[2].The foremost classical technique is Root-locus which solves control system performance by adjusting the location of closed-loop poles to attain system performance by varying system parameters as per the control design requirement applied. The Classical approach (Root-Locus) has certain limitations to SISO Systems whereas modern control techniques can be applied to MIMO time-variant, linear/ non-linear systems. The Pole-placement and Linear Quadratic Regulator are proposed for the estimation of the gain matrix. The Simulated results acquired using LQR and Pole-Placement are analysed and conclude that the settling time of the LQR Controller is 0.44s as compared to 3.08s for Pole-Placement and has the excellent feature of eliminating steady-state error to zero. The peak overshoot value gives information about deviated peak time response concerning the final one which is 0.332 which exemplifies that LQR provides more stability and deviates minutely. Simulation results prove efficacious for the LQR approach used for designing the vigorous controller.

The study also investigates the problem statement connected to parameter estimation for the aircraft positioning systems subjected to inertial sensor measurements purveyed by Hansa-III aircraft. The Integration of the D.R algorithm in Hansa-III aircraft assists in estimating longitude, latitude, and altitude ( $\theta$ ,  $\varphi$ , h). The Dead Reckoning method determines the current position by utilizing the previously determined position over elapsed time on estimated speed. The research study incorporates the implementation of the navigational approach to estimate aircraft position. Dead- Reckoning is operated for cartesian coordinate estimation using real flight data and gives precise navigational details of aircraft at lost time signal connectivity. The results are validated with exponential smoothing in graphical/ tabulated form and summarize that percentage error of Latitude, Longitude is deemed to be very less that justifies the result dominantly.

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# NOTATION AND ABBREVIATIONS

## Notation

$a_x, a_y, a_z$	Linear accelerations along x, y, z body axes $(m/s^2)$
€	Downwash
$C_{Y}$	Side force Coefficient
Е	Error
g	acceleration due to gravity
Н	Angular Momentum
J	Cost Function
Κβ	Scale Factor
L, M, N	Pitching, rolling, and Yawing moment
Μ	Net Moment
m	Mass of aircraft (kg)
p, q, r	roll, pitch, yaw rates (rad-s-1)
R	Measurement co-variance Matrix
Т	Thrust
u, v, w	Longitudinal, lateral, and vertical airspeed
V	Airspeed (m/s)
X, Y, Z	Force acting toward flow direction, toward right wing, and underneath through it
Θ	vector of unknown parameters
α	angle of attack
β	slide slip angle

Q	Dynamic Pressure
---	------------------

Δ Bias

 $\delta_a, \delta_e, \delta_r$  aileron, elevator, rudder deflection angle

- ζ Time delay
- ρ Air density
- $\Phi, \theta, \psi$  angle of roll, pitch and yaw (degree)
- $\dot{p}, \dot{q}, \dot{r}$  Rate of roll, pitch, and yaw rate
- $X_E, Y_E, Z_E$  Force acting toward Geographical North, Geographical East, and centre of the earth
- $X_w, Y_w, Z_w$  Force acting relative to velocity vector, toward right wing, and underneath through it
- $u_o, v_o, w_o$  Perturbed velocity along X, Y, and Z
- $\Delta u, \Delta v, \Delta w$  Small perturbations along X, Y, and Z
- *M<sub>a</sub>* Non-dimensional variation of pitching moment with pitch rate
- Non-dimensional variation of pitching moment with change in angle $M_{\dot{\alpha}}$ of attack
- $Z_{\alpha}$  Non-dimensional variation of Z force with angle of attack
- $M_{\alpha}$  Non-dimensional variation of pitching moment with angle of attack
- $w_{n_{sn}}$  Frequency of short period
- $\xi_{sp}$  Damping ratio of short period
- $\xi_p$  Frequency of Phugoid Motion
- $w_{n_p}$  Damping ratio of Phugoid Motion
- $\bar{C}$  mean aerodynamic chord
- $I_{XX}$ ,  $I_{YY}$ ,  $I_{ZZ}$  Moment of Inertia about x, y, z axes
- $I_{XY}$ ,  $I_{XZ}$ ,  $I_{YZ}$  Products of inertia in the XY, XZ and YZ plane, respectively, kg-m<sup>2</sup>

# Abbreviations

ACH	Attitude Control System
AH	Astrum Haglund
ANN	Artificial Neural Network
AOA	Angle of attack
ASCG	Measured from center of gravity to accelerometer
CFD	Computational Fluid Dynamics
CG	Center of gravity
CS	Control System
DC	Direct Current
DLR	Deutsche Forschungsanstalt fru && Luft- and Raumfahrt (German
	Aerospace Centre)
DR	Dead Reckoning
EKF	Extended Kalman Filter
ES	Exponential Smoothing
FFT	Fast Fourier Transformation
FOPID	Fractional Order PID Controller
FPR	Flight Path Reconstruction
FSFC	Full state feedback Controller
GLONASS	Global Navigation Satellite System
GN	Gauss Newton
GPS	Global Positioning System
IMU	Inertial Measurement Unit
INS	Inertial Navigation System
LM	Levenberg Marquardt
LP	Long Period
LQR	Linear Quadratic Regulator
LS	Least Square

MAC	Mean Aerodynamic chord
ML	Maximum Likelihood
MZN	Modified Ziegler Nicholas
NAL	National Aerospace Laboratory
NBCG	Measured from center of gravity of aircraft to nose-boom
ND	Newton Difference
NGN	Neural Gauss Newton
NLI	Non-Linear Invariant
NLO	Non-linear Observer
OAT	Outside Air Temperature
PID	Proportional, Integral, Derivative
QDR	Quadrotor Dead Reckoning
RCTA	Research cum trainer aircraft
SP	Short Period
TF	Transfer Function
TL	Tyreus- Luyben
UAV	Unmanned Aerial Vehicle
XKF	Exogeneous Kalman Filter
ZN	Ziegler Nicholas

# Subscripts

$$\alpha, \beta, \dot{\alpha}, \dot{\beta}$$
 With respect to  $\alpha, \beta, \dot{\alpha} \frac{b}{2V_{\infty}}, \dot{\beta} \frac{b}{2V_{\infty}}$ 

- ∞ Freestream
- f Fuselage
- M Mach number
- m Measured variables

p, q, r With respect to 
$$p \frac{b}{2V_{\infty}}$$
,  $q \frac{b}{2V_{\infty}}$ ,  $r \frac{b}{2V_{\infty}}$ 

- ss Steady-state
- t Horizontal tail
- w Wing

### Superscript

- . Derivative with respect to time
- ~ Variable in frequency domain

### Longitudinal Stability and Control Derivatives

- $C_{D_0}$  Coefficient of drag force at zero angle of attack
- $C_{D_{lpha}}$  Change in Coefficient of drag force with change in angle of attack Change in Coefficient of drag force with change in elevator deflection  $C_{D_{\delta \rho}}$  angle
- $C_{L_a}$  Change in Coefficient of lift force with change in angle of attack
- $C_{L_0}$  Coefficient of lift force at zero angle of attack
- $C_{L_q}$  Change in Coefficient of lift force with change in pitch rate
- $C_{L_{\delta e}}$  Change in Coefficient of lift force with change in elevator deflection angle
- $C_{m_0}$  Coefficient of pitching moment at zero angle of attack
- $C_{m_{\alpha}}$  Change in Coefficient of pitching moment with change in angle of attack
- $C_{m_q}$  Change in Coefficient of pitching moment with change in pitch rate
- $C_{m_{\delta e}}$  Change in Coefficient of pitching moment with change in elevator deflection angle

$$C_{D_{\alpha}} = \frac{\partial C_{D}}{\partial \alpha}$$

$$C_{D_{\delta e}} = \frac{\partial C_{L}}{\partial \delta_{e}}$$

$$C_{L_{\alpha}} = \frac{\partial C_{L}}{\partial \alpha}$$

$$C_{L_{q}} = \frac{\partial C_{L}}{\partial \delta_{e}}$$

$$C_{L_{\delta e}} = \frac{\partial C_{L}}{\partial \delta_{e}}$$

$$C_{m_{\delta e}} = \frac{\partial C_{m}}{\partial \delta_{e}}$$

$$C_{m_{\alpha}} = \frac{\partial C_{m}}{\partial \alpha}$$

$$C_{m_{q}} = \frac{\partial C_{m}}{\partial \alpha}$$

## **CHAPTER 1**

## **INTRODUCTION**

Control Systems are an integral part of modernization. Enormous applications of control systems surround us in day-to-day life such as traffic control systems, rocket fire, the Lift-off of a space shuttle to Earth's circle, and auto-guided vehicles transporting goods in aerospace assembly workspace glides along to reach their destination are some of the examples of an automatic control system. Based on these live examples, the research study aims to design, simulate, and develop the Control system and navigation of trainer aircraft Hansa-III based on a six degrees of freedom linear dynamic model using a maximum likelihood algorithm for estimating aerodynamic derivatives. Developing a mathematical model is a key parameter required for designing a control system. Aircraft system identification applies to engineering systems like aerospace vehicles to develop a mathematical model of the system. System identification was first defined by Zadeh stated, "Identification is a tool to identify systems on the basis of Inputs, outputs, and test conditions which is elaborately discussed in the next section(Roudbari & Saghafi, 2016)

#### **1.1 AIRCRAFT SYSTEM IDENTIFICATION**

The input-output model interface for developing the mathematical model in the existence of noise and disruptions is known as System Identification. In Layman's Understanding, System Identification is identifying parameters of the physical system subjected to observations to develop a mathematical model for the system.

*General System Identification:* The basic elements to define Identification problems include

- (a) Input to experiment behaviour of the physical system in the form of Maneuverers
- (b) Mathematical Model of the physical system
- (c) Responses in terms of Measurement
- (d) Methodology adopted to define system Identification

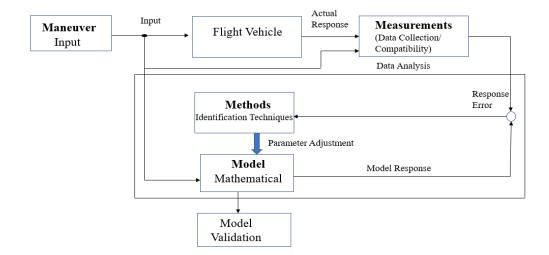


Fig 1.1: Concept of System Identification

The German Aerospace Centre (DLR) developed the Quad M by outlining five components that are essential to understanding System Identification as presented in Fig 1.1 (Hamel, 2019)(Hamel & Jategaonkar, 1996a)

Maneuverers: Control inputs are fed into system dynamics to experience the consequences despite output.

Measurement: High-quality sensors are used to evaluate the system's process and measurement noise, also known as a data compatibility check.

Model: It consists of mathematical equations based on the Newtonian law of motion. The Linear and non-linear models are used for flight vehicle system Identification.

Methodology: It is based on the Input/output interface and used for the time and frequency domain.

Validation: It defines testing, measuring, executing, and validating physical systems. It identifies whether the model meets desired expectations or not.

#### **Approaches to System Identification**

System Identification is classified on the basis of model class and model structure(Hoffer et al., 2013)

#### 1. The model class

(i) Linear/ Non-linear (ii) Parametric/ Non-parametric

Linear Models are simpler and more flexible for stochastic dynamics as well as the convergence of the physical system is guaranteed whereas the Non-linear model requires enough computations with no guarantee of convergence. Linear approximation is helpful for robust control design as Linear models give continuous responses to system parameters and give a better understanding to predict complex system behaviour. The system modelling is improved by linearized approximation thus linear modelling is advisable. Recent technology advancements expedite the more often usage in parameter estimation areas such as designing controls and autopilots, handling fault-tolerant issues, expanding the v-n curve, monitoring system health, and contrasting wind tunnel test results with analytical techniques like CFD (Computational Fluid Dynamics). Parametric Identification techniques include the least-square, maximum likelihood methodology to identify model parameters, referred to as black-box modelling(Leontaritis & Billings, 1985)(Jameson & Cooke, 2012a). Non-Parametric identification techniques include neural networks and genetic algorithms and they do not require postulates to assume a model structure. These models are used to gain knowledge of model complexity and model validation(Juang & Suzuki, 1986)

#### 2. The model Structure

(i) Black box (ii) Grey box (iii) user-defined model

The Black-box model assumes an unknown system and model parameters don't have constraints. Grey-box model assumes that some of the system-related information is known and parameters have constraints. User-defined model is a generic user-defined model using an input/ output interface.

Vehicle categorization is correlated and captures one aspect of system identification at one time on the basis of model class and structure(Roudbari & Saghafi, 2016)(Hardier & Bucharles, 2010)(Tischler & Remple, 2006)

#### General Attributes of System Identification are

- (i) Cost-effective
- (ii) Self-governing System
- (iii) Elimination of Random/Systematic error

### **1.2 AIRCRAFT CONTROLLER DESIGN**

In terms of multi-rotor drones, flying cars, and hybrid airships, aerospace technology is expanding rapidly. In the context of automatic control design, it has played a crucial role as a catalyst by encouraging the researcher's interest in areas such as reconnaissance missions, terrain surveillance, aerial photography, etc. An autopilot alleviates pilot tasks during innumerable flight regimes and handles adverse weather conditions to provide stability. The controller design requires comprehensive expertise in control theory, parameter estimation(R. Kumar, 2012) (Harper & Cooper, 1986), and flying handling quality. An enormous PID tuning approach to optimize gain values of the controller such as Ziegler Nicholas, Astrom-Haglund, Modified Ziegler Nicholas, and Tyreus-Luyben are used to study time domain characteristics as discussed by (Deepa & Sudha, 2016)(JAISWAL & PRAKASH, 2022). Modern approaches such as Pole-Placement, and LQR to design the Pitch controller of Hansa-III aircraft are discussed elaborately in chapter 5 of the thesis.

#### **1.3 AIRCRAFT NAVIGATION SYSTEM**

The evolution of research in the discipline of Navigation is always captivating as it is applied to detect orientation, exact position, and velocity. The research study inspects the problem statement for aircraft positioning systems depending on inertial sensor measurement apportioned by Hansa-III. The dead Reckoning approach measures position once GPS is not functional as suggested by M. Jayachandran thus D.R. algorithm is accomplished within the aircraft display system which acquires position information, and attitude(Jayachandran et al., 2009). The numerous applications of Dead Reckoning are surveillance, mobile robots, marine navigation, aircraft navigation, and automotive navigation. Pure D.R. technique is cheaper, economical, and causes systematic error thus pure D.R. technique is not applied where accurate position, radio-signal-based navigation is required. INS is integrated with dead reckoning equipment to provide accurate, reliable navigation results.

#### **1.4 RESEARCH MOTIVATION**

An enormous amount of work in the area of parameter estimation using various methodologies like Output error method (OEM), Filter error method (FEM), and Equation error method (EEM) had been accomplished for Hansa-III aircraft but there is a clear research gap when it comes to design a controller to make the

system fully autonomous so that it can be utilized for training pilots, analysis of dynamic systems, research-oriented activities, fault-tolerant system, accidental investigation.

No research is carried out for Hansa-III in terms of navigation henceforth, the dead reckoning navigational technique will be implemented to study the attitude, and orientation of the system so that it can be used for surveillance in terrain-prone areas, aerial photography, monitoring of floods/droughts.

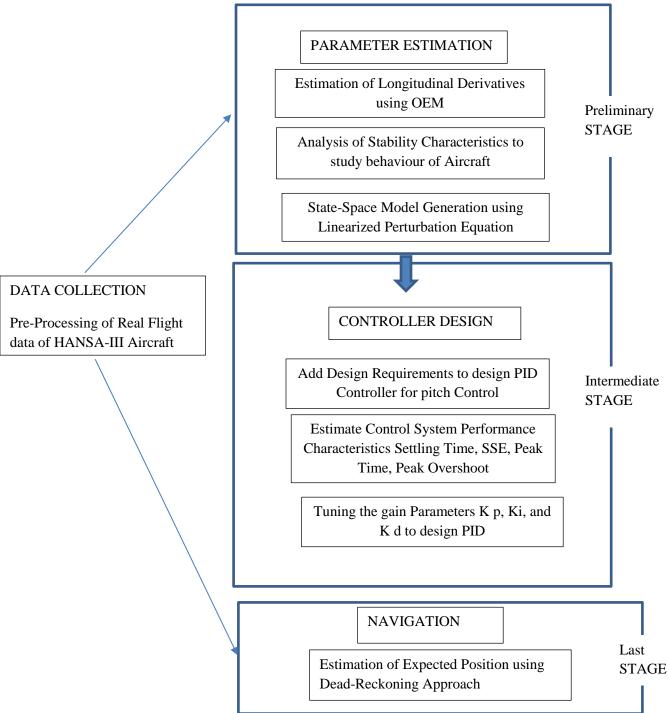
Designing an auto-controller, and integrating a novel navigational approach using parameter estimation of Hansa-III motivates to perpetrate research in this area.

## **1.5 RESEARCH OBJECTIVES AND METHODOLOGY**

### **Research Objectives**

- 1. Estimation of longitudinal stability and control derivatives from real flight data of Hansa-III aircraft using Output Error Method
- 2. Design of PID Controller for aircraft pitch control, analyzing stability and performance characteristics for hardware implementation
- 3. Integration of Dead Reckoning approach to estimate the expected position of Hansa-III Aircraft

## Methodology:



The methodology proposed for this study is discussed in form of a flow-chart:

Fig 1.2 Flowchart Representation of Methodology

#### **1.6 CHAPTER SCHEME**

The thesis comprises Seven Chapters which are outlined as:

**Chapter 1** The first chapter contains the overview of Aircraft parameter Estimation, Control Design Approaches, Aircraft Navigation System, research motivation, objectives, modelling tools, and research summary

**Chapter 2** covers the literature survey of the attitude control system, aircraft system Identification, modelling, simulation, and dead reckoning method, design of the pitch control system.

**Chapter 3** discusses the classification and categories of aircraft and a brief description of model specifications.

**Chapter 4** discusses the procedure of Parameter Estimation, file processing, Data compatibility check, Mathematical modelling, and Maximum Likelihood Technique for the estimation of longitudinal derivative.

**Chapter 5** briefly presents aircraft stability and control, automatic control system, Reference frame, Linearized equation of motion, state-space matrix representation for controller design, PID Controller Design, Tuning PID parameters using ZN, AH, MZN, TL techniques, Controller design using Root-Locus, pole-placement, LQR approach and comparing results using Simulation

**Chapter 6** presents an estimation of navigational parameters (latitude, longitude, altitude) using Dead Reckoning, a Comparison of results using exponential smoothing, and the Newton-difference method.

**Chapter 7** discusses the conclusion derived from the three objectives and a brief scope for future work is identified to extend the research study. Lastly, references in the form of the research paper, technical report, book, and chapters are referred to in the thesis.

## **SUMMARY:**

In this chapter, we discussed the concepts of aircraft system Identification, aircraft controller design, and aircraft navigation system. Additionally, the research motivation for choosing the topic, research objectives, and methodology are also presented. The chapter scheme covers topics such as Introduction, Literature Review, Aircraft Model Specifications, Aircraft Parameter Estimation, Aircraft Controller Design, Aircraft Navigation System, conclusion, and scope for future work.

# CHAPTER -2

## LITERATURE SURVEY

System Identification is a scientific discipline to identify the model based on the Input/ output observations. Parameter Estimation is an extremely formidable, extensively applied example of system Identification that estimates the attributes of a dynamic system based on conceptualization consideration of the mathematical model (Hamel, 1979)(IIiff, 1989). The task of best estimate determination is known as parameter estimation. A lot of research has been conducted in the area of parameter estimation of Hansa-III. The current technological advancement reflects the gap between automation and to design attitude controller of Hansa-III. The research study aims to design a controller by implementing a statistical output error approach to estimate the expected position of Hansa-III. To intervene in the gap, the autonomous controller integrated with the dead Reckoning algorithm to estimate navigational parameters is designed.

The Literature is reviewed in three different sections a) Parameter Estimation, b) Controller Design, and c) Aircraft Navigation as Dead Reckoning

## **2.1 PARAMETER ESTIMATION**

The task of best estimate determination is known as parameter estimation. The successful application is due to fine data processing handling capability, bettermeasuring techniques, and appropriate flight-test for adequate aerodynamic modelling (Hamel, 1979)(Klein, 1989) Bryan discussed the adequacy of modelling forces and moments and validated the mathematical model. The author introduces aerodynamic modelling that includes the relationship of forces and moments about an axis respectively. The aerodynamic model is in the form of Taylor series expansion such as

$$C_j = \sum_j \frac{\partial C_j}{\partial \sigma} \sigma + \sum_j \frac{\partial C_j}{\partial u} u$$

Where j stands for rolling, pitching, and yawing moment (l, m, and n), X, Y, and Z forces in X, Y, and Z direction,  $\sigma$  as motion variables airspeed, angle of attack, side-slip angle, and u as control input(Bryan, 1911).

E. Seckel, J. Morris, and R. D. Finck stated aerodynamic parameters are estimated using three different approaches at the early stage of aircraft design such as wind-tunnel Testing Method, Flight test, and analytical method. Among all the three modes, the analytical method was the convenient process of estimating parameters but the accuracy is low to attain thus results obtained from the analytical need to be validated from wind-tunnel and flight tests [21]- [22]

Hamel, P. G., and Jategaonkar, R. V., discussed the theory and evolution of system Identification of various flight vehicles in chronological order. The author also determined the damping ratio and frequency from flight data as well as applications in the area of system Identification(Hamel & Jategaonkar, 1996b).

K.W. Iliff, Hamel, and Jategaonkar stated Maximum Likelihood has been successfully used to flight data for parameter estimation. The acknowledged standard approach for estimating an aircraft's stability and control derivatives uses ML with process noise and measurement noise. (Hamel & Jategaonkar, 1996a)(Iliff, 1989) (Jategaonkar, 2015)

Hamel, Jategaonkar, Maine and Iliff covered a broader aspect of output error as its applicability has been extended to the non-linear system. The most applicable

version of Maximum Likelihood: its advantages and properties are discussed elaborately(Hamel & Jategaonkar, 1996a)(Maine & Iliff, 1986) (Hamel, 1979)

Klein addressed linear regression for model determination, the applicability of ML in the frequency domain and time domain, and data compatibility. The parameter estimation techniques at different flying regimes, and unsteady, unstable aircraft conditions were also addressed by the author(Klein, 1989).

D. Kuehme, N. R. Alley, C. Phillips, B. Cogan, E. A. Morelli and J. A. Grauer discussed OEM, FEM, EEM, EKF, Regression analysis in the time domain for parametric identification as this methodology describes a correlation between flight test-bed data and linear model(Kuehme et al., 2014) used this technique to study longitudinal, lateral Stability, control, and damping coefficients of PTERA research aircraft using SI Toolbox SIDPAC. The disadvantages of the time domain led to the introduction of the concept of a frequency domain. FFT is a method for analysis that changes the domain from time to frequency as the convergence rate is faster, handles control design problems easily, robustness to noise (Morelli & Grauer, 2020)

R. Jategoankar, states that there are three categories for parameter estimation: equation error method (EEM), output error method (OEM), and filter error technique (FEM)stated parameter estimation is categorized into three types: equation error method (EEM), output error method (OEM), filter error method (FEM) [8]. The equation error method defines a class as the Least square method which defines the cost function. Using the output error method, the error is reduced that occurs between the system output variable and the system predicted variable. (Jategaonkar, 2015)

Peyada et.al addressed parameter estimation methods in terms of process and measurement noise. Traditional methods: EEM cannot handle process and measurement noise, OEM handles measurement noise, and both process and measurement noise are handled by FEM from flight data. The research article also uses GN and LM optimization techniques in estimating the parameters of Hansa-III(Peyada et al., 2008)

R. Kumar discussed the estimation of derivatives for highly maneuverable, unsteady, unstable aircraft at a high angle of attack. This motivates researchers to study in this field as special efforts are required to meet the challenges involved in non-linear model identification. The author successfully estimated the parameters of Hansa-III near stall region using Maximum Likelihood. This method is widely applicable in time-domain analysis to estimate derivatives using flight data of the vehicle. Maximum Likelihood is a widely used statistical technique to minimize the error and make the system dynamically stable. The author estimated the lateral-directional parameters of Hansa-III using a conventional approach such as Least-square, Maximum Likelihood, and Neural Technique as Neural Gauss-Newton. The background information of both approaches is discussed as well and variations of the effect of the type of control inputs are also highlighted in the article (Jategaonkar, 2015)(R. Kumar & Ghosh, 2014)

Grauer discussed the estimation of aerodynamic derivatives using the filter error method (FEM), of a non-linear aircraft model in consideration of turbulence effects. Results were simulated with NASA's generic aircraft Transport model. Time and frequency domain approaches were used to demonstrate the effectiveness of the approach. This paper explains how to solve real-time data compatibility problems. Data compatibility is a part of parameter estimation and is used to check data accuracy by making bias-free and error-free flight data(Grauer, 2015)

E. T. C. Kim explained that M.L.E.M was implemented to estimate **the** stability and control derivative of a 4-seater canard aircraft, firefly. This methodology has benefits that measure both process and measurement noise. Results from DATCOM and CFD were compared to those from a wind tunnel.(Kim et al., 2015)

C. Gottlicher, discussed optimal control methodology is operated for parameter estimation of the dynamic model utilizing Cost function 'J' that is derived by using

OEM. Estimated results are compared with the least square method to get the optimum result.(Göttlicher et al., 2016)

R. K Chauhan and S. Singh, reviewed the applicability and background information of various parameter estimation techniques such as OEM, FEM, EEM, and ANN. Techniques like Modified delta, delta, and ML were also successfully reviewed. Results are compared based on the critical review of the research work.(Chauhan & Singh, 2018)

S. Sadrela, R. Dhayalan et.al, discussed longitudinal, lateral-directional characteristics of CDRW-based UAV. The mathematical model of UAVs is formulated and a kinematic consistency check of real flight data is performed. Various techniques like Neural Gauss Newton (NGN), ML, and LS were implemented to obtain weak and strong derivatives of UAV(Saderla et al., 2019).

H.O. Verma and N.K. Peyada, estimated stability and control derivatives using the classical estimation approach ML, and LS. The author discussed ANN as an alternative approach to the stall condition of an aircraft. The efficacy of the Extreme learning machine method in terms of standard deviation such as Gauss Newton is validated with Maximum Likelihood(Verma & Peyada, 2021)

R. Jaiswal, O. Prakash, and S. Chaturvedi, "A Preliminary Study of Parameter Estimation for Fixed Wing Aircraft and High Endurability Parafoil Aerial Vehicle" 2022 discussed ML as the best tool to define output error method. This methodology is highly efficient when the sample size is large but inefficient in handling process noise. This statistical technique is not used for non-linear dynamic systems and noisy environmental interruptions (Jaiswal et al., 2020)(R. Kumar, 2012)

### 2.2 AIRCRAFT CONTROLLER DESIGN

The attitude control design requires a suitable controller to fulfil the required needs. The theory of modern control plays a vital role in the robust control system. This type of robust method such as Linear Quadratic Regulator deals with non-linearity and uncertainty without affecting system performance. The traditional control approach makes trade-offs amidst robustness and performance. Many research problems are solved using the same technique that results in optimal performance. A lot of research has already conducted to intervene in the gap between traditional and modern methodology.

E.H.J Pallet explained the principle of aircraft stability and control, fundamental of aerodynamics. The longitudinal motion modes, including long-period and short-period modes, are thoroughly described. (Pallett, 1954)

Jefferey D. Robinson discussed LQR Technique to locate poles precisely for an optimal solution. The author developed the LQR algorithm by minimizing the value of cost-function J and choosing Q, R scaler weighs wisely(Robinson, 1991)

R.C. Nelson discussed aircraft equation of motion. The author also reviewed the basic principle of aircraft stability and control along with auto-pilot design. For designing the pitch attitude control system, time and frequency domain design requirements were discussed. The comparative study of classical and modern control methods was also briefed (Nelson, 1989)

Krishnaswamy Srinivasan presented pole-placement and LQR technique for estimation of state-feedback gain matrix k. The state and observer estimation were explained thoroughly(Srinivasan, 2006)

Wahid. N, Hassan, et al proposed two methodologies PID and fuzzy logic PID to control aircraft Pitch angle. The mathematical model of aircraft is developed and implemented in the Simulink environment. The results were compared in the form of time-domain characteristics and fuzzy PID proved to produce the best optimal solution(Wahid & Hassan, 2012).

Yibo Li, et al, discussed the LQR method for designing the control law of the Longitudinal stability Augmentation System of UAVs. The control law is designed using output feedback (Yibo Li, Chao Chen, n.d.)

Mohammad Shahrokhi and Alireza Zomorodi, present a comparative assessment of various open-loop and closed-loop tuning methods. The techniques are analyzed for Single Input Single Output Systems to get the optimized value of gains K<sub>P</sub>, K<sub>I</sub>, and K<sub>D</sub>(Mohammad Shahrokhi and Alireza Zomorrodi, 2005)

Amir Torabi, et al, compared performances of classical and modern control approaches for aircraft pitch attitude control systems. The performances of fuzzy logic, PID, and LQR Controllers were compared to get an optimal solution (Torabi et al., 2021)

Khoi Niguen Dang, optimized the design of the attitude controller of the quad-rotor using a system Identification approach. LQR theory was used to design Linear quality servos to improve performance characteristics (Dang et al., 2015)

Deepa and Sudha discussed a mathematical model for pitch control of general aviation aircraft and designed a PID Controller by tuning PID parameters with Ziegler Nicholas, Modified Ziegler Nicholas, Tyreus-Luyben, and Astrum-Haglund approaches. Results in the form of Time-domain specifications of different tuning techniques are compared. ZN proved to be better in all terms and conditions(Deepa & Sudha, 2016)

Amlan Basu, et al, focus on designing PID and FOPID Controller using tuning techniques like Ziegler Nicholas, Astrum-Hagglund, Cohen-Coon, and CHR. The fundamental of each method is discussed and well explained in the form of a step response (Basu et al., 2016)

Tamayo used UAV as a platform that aims to study all three aircraft parameters such as system Identification, control, and navigation. Eigenvalues of the nonlinear model are linearized using linearization theory to study dynamic performances(Basu et al., 2016)

Joao P. Hespanha, discussed state-space representation, state-feedback design, controllability, observability, and optimal control methods. This book aims to provide background information for modern design techniques(Jo & December, 2017)

Valderrama, designed an aircraft pitch controller to improve the stability and performance of UAVs. Ziegler Nicholas methodology was adopted to tune the PID controller. Various time domain performances to study the performance of the controller were discussed (Villarreal-Valderrama et al., 2019)

W. Ahmed designed a longitudinal autopilot for altitude and pitch control. He designed multi-loop configurations using eigen-structure Assignment (EA) and PID. The inner loop is configured by EA for stability and the PID Controller is used to design the outer loop for controlling altitude and pitch Control. (W. Ahmed, Z.Li, 2019)

M. Raja and Om Prakash discussed the satellite attitude control system. The PDcompensated controller to meet design specifications using the root-locus algorithm is constructed using the control system toolbox. Time-domain characteristic of the satellite is discussed elaborately (Raja & Prakash, 2020)

### 2.3 AIRCRAFT NAVIGATION SYSTEM

Aircraft Navigation System as Dead Reckoning

The theory investigates the problem statement related to parameter estimation for aircraft positioning systems based on Inertial sensor measurements provided by flight test of Hansa-III aircraft. In terrain-prone, steep places, some satellite-based signal transmission techniques, such as (GNSS), cannot be used; as a result, the Dead Reckoning method is used to make precise future predictions.

Philips G Mattos discussed the implementation of an algorithm describing GPS and DR. The drift issues caused by unaided GPS, unaided DR, coupled GPS, and DR are explained. Integrated GPS (global positioning satellite) and DR (Dead Reckoning) sensors are used to track and navigate low-cost vehicles. Results for GPS, DR with a loosly coupled, and DR with a tight coupled were compared and discussed. Tightly coupled DR gives the best optimum result as compared with all three (G.Mattos, 1994)

Zeev Berman. et al, discussed future aspects of the aviation navigation systems such as the dead reckoning system. The author discussed background information on Dead Reckoning and Inertial sensors. Different configurations of aviation navigation systems are discussed. He presented an actual statistical model and varied wind vectors to match actual data. To quantify horizontal positional inaccuracy, the Dead Reckoning system, standalone inertial sensors, and inertial sensors integrated with the DR system were compared. (Berman, 1998)

M. Jayachandran, presented a dead-Reckoning approach using Inertial sensors for position estimation at the time GPS drops out. When GPS is not working, the method is useful for navigation. A Navigational algorithm is implemented within the display system of aircraft that receives information about attitude, and position (Jayachandran et al., 2009)

G. S. Reddy presented various advanced navigational systems varying from satellite to archaic forms for the application of aircraft. This study investigates various navigation systems to enhance system's accuracy as the accuracy range for the type of military application is the major concern of systems. The research concentrates on a gyro-based inertial navigation system to increase the system's accuracy. Integration of the INS-GPS-GLONASS system is applied for combat aircraft, ships, and long-range missiles (Reddy & Saraswat, 2013)

Lorenzo, experimented with the dead reckoning of UAV using XKF (Exogeneous Kalman filter) and NLO (Non-linear observer) IMU sensors such as (acceleration, rate gyros, an inclinometer); and altimeter; the camera is used. Position, velocity, and altitude are used as observed states. XKF gives the best optimum result as compared with NLO. The result of calculated velocity comprises a bias effect. Biases of various sensors such as accelerometers, gyroscopes, and optical flow velocity are also estimated up till the availability of GNSS (Fusini et al., 2017)

Parinaz Kasebzadeh covered broader aspects of parameter estimation for applications of mobile positioning. The navigational parameters such as position using the PDR of mobile robots were estimated. The PDR algorithm was designed to get more accurate gait parameters which will improve the accuracy of the position estimate. The Pedestrian Dead Reckoning algorithm is developed for the mobile position. Various cases of positioning algorithms are discussed and the drawbacks are mitigated using a model-based sensor fusion technique (Kasebzadeh, 2017)

T. Mahmoud discussed the benefits as well as drawbacks of integrating the INS system with GPS. The specification of the system varies in accuracy, reliability, update rate, budget, size, and mass. The study investigates the performance of INS/GPS systems and different algorithms. INS is integrated with dead reckoning equipment to provide accurate, reliable navigation results. This study investigates the performances of loose couple INS/ GPS, tightly coupled INS/GPS, and INS using SIMULINK. Tightly coupled INS/GPS gives better performance than loosely coupled integration (Mahmoud & Trilaksono, 2018)

Pedro Paulo Liborio Lima do Nascimento, discussed the alternative procedure of estimating navigation coordinates once GPS systems are inaccurate, unavailable in tunnels, dense and terrain-prone areas. The author integrated the dead reckoning algorithm with a GDOP (Geometric Dilution of precision) based positioning solution. The simulated results in term of root mean square error are compared to

stand-alone GPS, GPS +DR. The error was reduced from 97%- 98% to 83%-88%(Do Nascimento et al., 2018)

I.K. A. Shurin, The research used quadrotors for applications both indoors and outdoors such as surveillance, mapping, and transportation. The fusion of accurate navigation systems such as INS/GNSS is required to accomplish the task. Environmental Constraints lead to drift in time in the navigation solution thus pedestrian dead reckoning is mitigated in pure Inertial Navigation. It enables the quadrotor to estimate the distance from peak to peak. The simulated result shows the accuracy of the navigation solution while comparing INS and QDR approaches. QDR navigation solution is bounded while the INS solution diverges (Shurin & Klein, 2020)

Piotr Lichota presents an aircraft controller design procedure for tracking aircraft trajectory. The study used Maximum Likelihood and Extended Kalman filter estimation techniques to identify parameters and obtain a mathematical model of a non-linear transport aircraft model. The Linear Quadratic Regulator approach is used to design a controller for accurate aircraft tracking trajectory. It is found that tracking error is proportional to wind velocity in the presence of wind proportional to turbulence intensity in the presence of turbulence and admissible for small-moderate disturbances (Lichota et al., 2020)

Omri Asraf, Firas Shama, and Itzik Klein, the study suggested PDR Net, a deeplearning version of pedestrian dead reckoning that can be used for user positioning. In the study, distance regression and changing heading angles are used to identify smartphone locations. Indoor navigation is a good application for the PDR technique. Experimental Results display proposed methodology outperforms the traditional one (Asraf et al., 2022)

### SUMMARY

This chapter entrusts a literature survey on Parameter Estimation, Controller design, and Navigation. Based on the study, it was observed that the M.L technique is applied to the flight data in the time-domain for the estimation of parameters. It is the standard approach for the estimation of derivatives of an aircraft and has capability of handling measurement noise too. Once the ML technique is applied to estimate the parameters, the methodology adopted to design attitude controller on the basis of the research study is LQR. This robust method deals with optimal problems by concentrating on design requirements without sacrificing its performance. Some surveys in term of aircraft navigation system observed signal transmission methods such as GNSS is not able to forecast future information at the time of signal loss thus Dead Reckoning methodology can be used for future prediction.

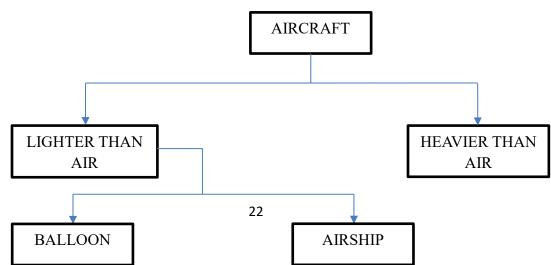
# CHAPTER- 3

# AIRCRAFT SPECIFICATIONS

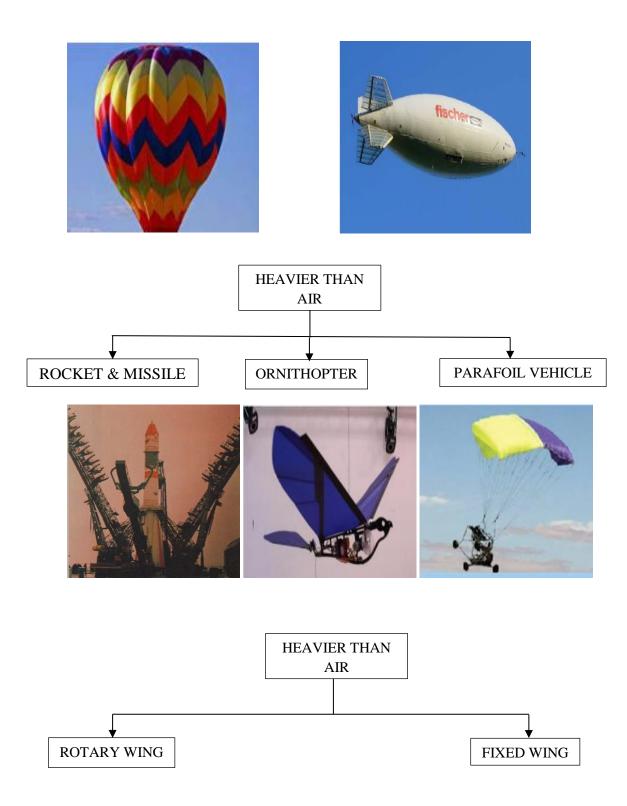
The study addresses the classification of aircraft as lighter than air/ heavier than air machines. The stratification of the aeroplane as Military, Commercial, Transport, and Trainer is discussed as a research study focalized on the research cum trainer aircraft- Hansa-III. It is a fully composite, low-wing configuration, tricycle landing gear, and two-seater aircraft. The drawing as shown in Figure 3.3 illustrates the characteristics of the model concerned. The general features and specifications are mentioned in the below section

#### **3.1 AIRCRAFT**

The generic term "Aircraft" includes all man-made machines flying in the air for example kites, parachutes, helicopters, aero-planes, rockets, missiles, airships, gliders, auto-gyro, hybrid aerial vehicles, etc. An aeroplane is an aircraft but the reverse of it is not always the same. Fixed wing heavier than aerial machines includes an aero-plane which stands for vehicles that fly in the air and are propelled forward by jet engines to produce thrust. Aircraft are broadly classified as displayed in Figure 3.1:



#### **CLASSIFICATION**





Helicopter

Aeroplane

Fig 3.1 Aircraft Classification(Devalla & Prakash, 2014)(R. Kumar & Ghosh, 2015)(Kornienko & Well, 2003)(Heredia & Ollero, 2009)(Ramesh et al., 2020)(SPACE India, 1988)

## Lighter than Air:

A man-made vehicle that flies in the air and produces thrust on its own to move forward without an engine falls under this class. The aerodynamic force (lift) is always greater than its weight which helps this class of vehicles to fly in the air. These systems include balloons, dirigibles, and blimps, often used for surveillance, monitoring natural calamities, and advertisement as shown in Figure 3.1

Balloons:

Montgolfier brothers were the first individuals who succeeded in placing the man-made object "Balloon" in the air in 1782 (SABHARWAL, 2003). It consists inflated bag with a gondola attached by ropes. It is difficult to control the flight as it moves in the wind direction.

Airship:

Controlled balloons with non-rigid structures often referred to as dirigibles consist of a gondola and an inflated bag with an engine and propeller. Horizontal tail fins with movable rudder are attached in dirigibles termed airship which is used for movement in upward, downward, left, and right direction. Henry Gifford's airship on 24 September 1852 was the first airship144 feet long, with a diameter of 39(SABHARWAL, 2003). feet flew in the air. Rigid airships called zeppelins include a framework of steel and aluminium with a long cylinder of the nose and pointed tail. The first ever-built, biggest hydrogen-filled airship 'Hidenberg' is 803 feet long, 135 feet in diameter with a space of 70 passengers (SABHARWAL, 2003). These machines are often used for surveillance, and advertisement due to excellent endurability, and durability.

### Blimps:

Non-rigid small airships fall in this class of vehicle. Blimps are used for advertisement and submarine patrols.

### **Heavier than Air:**

Machines that fly in the air and are propelled forward by jet engines to produce thrust falls under this category. It comprises ornithopters, rockets and missiles, parafoil aerial vehicles, multi-copters, and airplanes as referred to in Fig 3.1

### Missile:

Missiles are heavy-range guided weapons that possess the capability of self-ignition for damage on the selected target.

#### Ornithopter:

The hovering of insects and birds inspired to generate the concept of a flapping machine termed an Ornithopter. Flapping flight has two classesbird and Insect(Ansari et al., 2006). Bird is useful for indoor application and too fast in forward flight whereas insects have light wing structure approximately 1% of the insect's weight proves to be viable for the production of MAV(Ellington, 1984). Flapping wing micro aerial vehicles have agile behaviour, small size, broad v-n curve, and promising characteristics at low Reynolds(Caetano et al., 2013)

### PAV:

PAV is the category of parachute UAV having characteristics of high endurability, robustness, and safety during system damage. It contains a non-rigid wing structure termed parafoil depends on wind gusts for manoeuvring.

### Helicopter:

Rotary wing aircraft derive lift from rotary blades termed rotorcraft. The helicopter has a set of blades known as main rotor blades and tail rotor blades move opposite to each other to maintain stability.

#### Aero-plane:

Fixed wing, heavier than aerial machines includes an aero-plane which stands for vehicles that fly in the air and are propelled forward by jet engines to produce thrust. Based on type, an aero-plane is categorized into (i) Military (ii) Transport/cargo (iii) Commercial (iv)Trainer, and many more as shown in Figure 3.2. Military aircraft are designed to protect the nation from an enemy. It may be fixed or rotary. These combat aircraft are purposefully designed to enable aerial warfare. Cargo-type aircraft are commercially designed for the transportation of goods. Commercial aircraft come under civil aircraft used for the transportation of passengers or multiple loads of cargo.

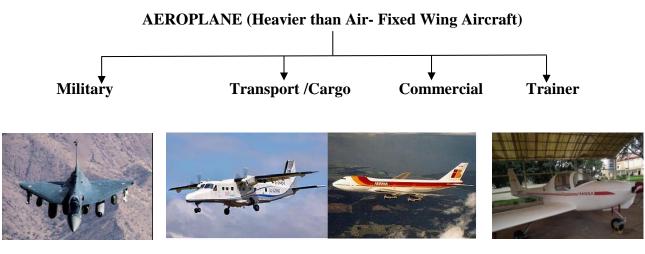
Research cum trainer aircraft is used for study as well as for research

purposes. These types of aircraft are also used for flight training. One of the examples of Indian research aircraft is Hansa.

Various Categories of aircraft are compared on the basis of their features discussed in above section is displayed in Table 3.1

S. No.	Factors	Airship	UAV	Rotorcraft	Fixed Wing Aircraft
1	Design	Simple	Moderate	Complex	Complex
2	Stability	Stable	Highly Stable	Less Stable	Stable
3	Manoeuvrability	Less	Moderate	Highly	Moderate
4	Control	Simple	Simple	Complex	Complex
5	Auto-Controller	Primitive	Advanced	Advanced	Advanced
6	Flight Data Test Time	High	High	Less	Moderate

Table 3.1: Comparison of Aircraft



Tejas

Dornier-228

Boeing -747

Hansa-III

Fig 3.2 Classification of Airplane (*Timeline of HAL Tejas*, n.d.)(*Dornier-228*, n.d.)(*Boeing-747*, n.d.)(*NAL Hansa*, 2000)

## **3.2 HANSA-III AIRCRAFT**

Hansa-III is a research cum trainer, two-seater aircraft manufactured by NAL, India, and useful for research purposes. Three designs were developed

by NAL in which Hansa-II was built as a prototype and Hansa-III was finalized for production.

This aircraft fully satisfies my problem statement so I chose this particular aircraft for my study. To fetch the flight data, multi-variant sensors are instrumented in the aircraft for flight data acquisition. The aircraft structure is fully composite having a low wing configuration with a tricycle landing gear arrangement. It consists of a Rotax-914 F3 engine coupled with a Hoffmann propeller(R. Kumar, 2012). Hansa-III has already covered more than 4000 flying hours.



Fig 3.3.Hansa-III aircraft (Jaiswal et al., 2020)

Geometrical Parameters	Value	Geometrical Parameters	Value
Win	ng	Horizoi	ntal Tail
Planform area (S)	12.47(m <sup>2</sup> )	Planform area $(S_t)$	2.04(m <sup>2</sup> )
Aspect ratio (A)	8.8	Aspect ratio (A)	6.35
MAC $(\bar{c})$	1.21(m)	MAC $(\bar{c})$	0.59(m)
Root Chord $(c_r)$	1.3(m)	Root Chord $(c_r)$	0.78(m)
Tip Chord $(c_t)$	0.8	Tip Chord ( $c_t$ )	0.354(m)
Taper ratio ( $\Lambda$ )	6(deg)	Taper ratio $(\Lambda)$	0.454
Airc	raft	Aerodynamic De	rivatives
Aircraft span (b)	10.47(m)	$(C_{L_{\alpha},w})_{ss}$	4.5

Mass (m)	750(kg)	$(C_{L_{\alpha_t}})_{ss}$	1.48
Velocity (V)	36(m/s)	$(\mathcal{C}_{m_{\alpha,f}})_{ss}$	0.3
Moment of Inertia I <sub>Y</sub>	907(kg-m <sup>2</sup> )	$(C_{L_{\alpha_t}} \frac{d\epsilon}{d\alpha})_{\rm ss}$	0.22
Moment arm $(l_t)$	3.624(m)		
Density (p)	0.96(kg/m <sup>3</sup> )		
Moment of Inertia I <sub>X</sub>	925(kg-m <sup>2</sup> )		

Table 3.2: Geometrical and Aerodynamic Parameters of Hansa-III (R. Kumar, 2012)

# **POWER PLANT SPECIFICATIONS**

Number of engines	One
Make	Bombardier Rotax 914 F3
Engine limits	100 BHP @ 5500 rpm
Max. continuous power	(Propeller rpm 2265)
Engine max. power	1 15% @ 5800 rpm (5 min)
	(Propeller rpm 2385)
Idle RPM	1400 rpm (Propeller rpm 580)
Manifold pressure	38.4in Hg at 115% power (max. 5 min)
Acceleration	Max. 5 secs. at -0.5g
Rating, full throttle at	100 BHP, Max, continuous @ 5500 RPM (Propeller rpm 2265)
sea level pressure	115 BHP @ 5800 rpm (Propeller rpm 2385) contingency power for
altitude	max. 5 min.
Max. Oil Temp.	Max. 130°C
	Min. 50°C
Max. Oil pressure	7 bar
Fuel grade	AV Gas 100 LL
Oil specification	Castrol Syntron, non-detergent, fully synthetic engine oil
Coolant	SERVOKOOL
Propeller Limit	Hoffmann makes
	HO-V 352F( ) 170 FQ+3
	Max. propeller RPM never exceeds 2700 RPM
Altitude (Max	10,000 feet
Operating)	

Table 3.3: Power Plant Specifications of Hansa-III (NAL, 2000)

## CONTROL SURFACE MOVEMENT

Rudder	30° left, 30° right; -1-2°
Wing flaps	20° for landing 1° 20° for take-off 1°
Elevator	$30^{\circ}$ up, $25^{\circ}$ down; $+2^{\circ}$
Elevator trim tab	22° up, 33° down; A2°
Aileron	$20^{\circ}$ up, $20^{\circ}$ down; $+2^{\circ}$
Forward limit	21.94 % of MAC aft of wing MAC LE
Aft. Limit	27.47 % of MAC aft of wing MAC LE

Table 3.4: Specification of Control Surface deflection and C.G Range of Hansa-III(NAL, 2000)

## SUMMARY

This chapter represents a brief model description in terms of geometrical, aerodynamic parameters, power plant, and control surface specifications so that it can be useful for deducing the state-space representation of the model.

## **CHAPTER-4**

## AIRCRAFT SYSTEM IDENTIFICATION

A flying machine's motion in the atmosphere is characterized by flight dynamics. The vehicular attitude and the resultant flight path are decided by the vehicle responding to aerodynamics, gravitational, propulsive, and control forces acting upon it. The domain of flight dynamics is sectioned into features such as stability and control, Performance, Navigation, and guidance. System Identification is a part of flight dynamics that creates a mathematical model of a physical system based on measurements.

System Identification is defined as "Identification is the process of determining a system's initial and final states using input and output from another system that belongs to the same class as the system being tested."(Zadeh, 1962)

The random observations in the course of measurement and process noise are distorted due to sensors, and external disturbances. Boeing-737 Max disaster represents failure of stability Augmentation system(Sgobba, 2019). Reforming the system for innovation, and providing certification to a new computer-based system leads malfunctioning of MCAS (Maneuvering characteristic Augmentation system) resulting in a catastrophic crash that took 346 lives(Psas et al., 2014). Tools are needed to address fatalities due to faulty sensors, flight handling characteristics at high AOA, and fault-tolerant control systems. Wind tunnel testing, modelling and Simulation predict aircraft dynamics to design controllers but are limited to small- scale models therefore System Identification

approach should be used to handle imperfections(Jameson & Cooke, 2012b). Handling of imperfect measurements is simplified by evaluating the parameters of the system using statistical techniques. In the past years, system Identification has expanded its growth due to its application in designing controllers, health monitoring, and analysis of dynamic systems, making systems fully autonomous, and fault-tolerant. System Identification is applied to study the time-variant tracking behavior of vehicle subsystems in real time to update system modeling by parameter estimation in continuous intervals to detect sensor fault, and system failure(Tang et al., 2009a)(Melody et al., 2000)(Hardier et al., 2016). Real-time LS is applied in the area of Robotics, aerospace and automotive(Ljung & Gunnarsson, 1990)(Hardier, 2015)

Aircraft parameter estimation is the best illustration of system identification methodology. The process of determining the best estimates that occur in the dynamic model to represent the physical system is the methodology of parameter estimation. System Identification is a statistical investigation that handles estimating the value of derivatives based on measured experimental data. Designing autopilots and controllers, expanding the flight envelope, comparing the results of analytical techniques like CFD with wind tunnel tests, simulation, dynamic analysis, evaluating flying characteristics, confirming aircraft performance, and accident investigation are some of the major applications. Development of mathematical models for the physical systems subjected to imperfect observation or measurement. This phenomenon is termed as system identification.

Bryan intuited the conception of aerodynamic modelling, which relates forces and moments as a function of translational and rotational motion variables respectively. The analytical methodology is the foremost technique of parameter Estimation at the initial phase of aircraft design as the accuracy level is low thus Flight and Wind-Tunnel test is required. The observational/ experimental method provides a strong

hold to attain the desired result as compared to the analytical. Some of the traditional methods for linear systems in the frequency/ time domain are FFT, ML, and LS(Bryan, 1911).

The values acquired through wind tunnel testing require validation from flight test data as it is difficult to obtain the value of power effects, and propulsive effects at different flight conditions.

The advancement of Flying Vehicular System Identification and its application in chronological order is discussed by Hamel and Jategaonkar(Hamel & Jategaonkar, 1996a). Miliken first tried to use the static and dynamic parameters from actual flight data in 1947(Milliken W.F.Jr, 2003)

The three categories of traditional parameter estimation techniques are as follows as suggested by Ravindra Jategaonkar(Jategaonkar, 2015): (i) EEM, (ii) OEM, (iii) FEM. Least square also known as regression analysis defines a category of Equation error method in which the flight dynamic model of the physical system is not known. The least-square accounts for process noise, not measurement noise. Non-linear/ Ordinary LS methodology was introduced by Shinbrot and Greenberg(Shinbrot, 1951)(Greenberg, 1951). The performance capability of this methodology is robustly determined by data quality. The cost function is in the form of an Input-Output equation defined directly in the Equation-error Method. In the case of the output error method (OEM), the model parameters are altered consecutively for error minimization between the system output and response of the predicted model. This method has the potential to solve non-linear optimization problems too. Its application for parameter estimation makes use of flight data and needs the postulation of accurate flight dynamic formulation. This process assumes that process noise is imperceptible and handles measurement noise along with process noise. This is the most applicable time-domain method for aircraft parameter estimation. One of the most efficient OEMs is the Maximum Likelihood intuited by Fischer is inapplicable to the non-linear system as handling a non-linear model structure is practically difficult. The FEM faces difficulty in extending it

through multiple experiments by treating the process noise distribution matrix independently for every maneuver as proposed by the researcher (Iliff, 1989) [23]It does not guarantee the correct postulate of the model. This methodology has the capability of handling process and measurement noise and is also extended to the non-linear system as proposed by Jategoankar (Jategaonkar, 2015) thus FEM is applied for unique cases only as the majority of parameter estimation problems are solved by the Output error method or Least-square method. Since the last three decades, the method of maximum likelihood has been used successfully for parameter estimates utilizing flight data. This statistical technique minimizes error and makes the system dynamically stable as proposed by Rakesh Kumar(R. Kumar, 2012).ML is the best tool to define output error method. This methodology is highly efficient when the sample size is large but inefficient in handling process noise thus process noise is assumed to be negligible and measurements taken by sensors are corrupted by measurement noise. This statistical technique is not used for nonlinear dynamic systems and noisy environmental interruptions. Accuracy is measured in terms of Cramer-Rao bounds in this method.

Numerous subjects related to estimating aircraft parameters include linear and stepwise regression, characteristics, and applicability of statistical techniques, like maximum likelihood as explained by Klien (Klien & Morelli, 2006). The research work in the area of parameter estimation in different flying regimes at high AOA for unstable aircraft is also addressed by Klein. Estimating unsteady aerodynamics on a lifting surfaces involves several techniques which are complex for a purpose of estimating parameters(Morino, 1974)(Robert, n.d.). Quiezo.et.al discussed the vortex system to consider the downwash effect for swept, and tapered wing(Queijo et al., 1978). The unsteady aerodynamic derivatives(Queijo et al., 1979)(Raisinghani & Ghosh, n.d.)(Wells, W. R., Banda, S. S., and Quam, 1979)(Singh & IIT Kanpur, n.d.).

A wider level of fidelity for non-linear systems like aircraft, rotary-wing aircraft, missiles, and UAVs makes this technique unique and novel on the other side ANN faces difficulty in estimating parameters at higher AOA. System Id is applied to study the time-variant tracking behaviour of vehicle subsystems in real time to update system modelling by parameter estimation in the continuous interval (Tang et al., 2009b)(Hardier, 2015)(Ljung & Gunnarsson, 1990)to detect sensor fault and system failure. Real-time LS is applied in the areas of Robotics, aerospace, and automotive(Jategaonkar, 2015)(Tischler & Remple, 2006)(Zadeh, 1962)

*General System Identification:* The Quad-M in system Identification defines Maneuverers, Models, Measurement, and Methodology which is discussed elaborately in the below section

- (a) Input to experiment behaviour of the physical system in the form of Maneuverers
- (b) Mathematical Model of the physical system
- (c) Responses in terms of Measurement
- (d) Methodology adopted to define system Identification

## **4.1 FLIGHT DATA GENERATION**

The Flight test of Instrumented Research cum Trainer Aircraft Hansa-III was regulated at the flight Lab of IIT Kanpur and flight data was collected operating data acquisition system(R. Kumar, 2012)

### Symbolic Representation to define Real Flight data :

During flight testing, numerous longitudinal flight data sets were acquired. Using the eight data sets, longitudinal aerodynamic characteristics were estimated making use of Maximum likelihood. The Terminology HA resembles 'Hansa-III', L is Longitudinal, and numerals '1-8' define the number of data sets such as HAL1, HAL2, HAL3 For longitudinal, the letter(s) accompanied by 'L' such as 'M' correspond to multistep, 'D' as a doublet, and 'P' as pulse elevator control inputs.

### **Flight Data Generation:**

Hansa-III is a research cum trainer, two-seater type aircraft manufactured by NAL, India, and useful for research purposes. Three designs were developed by NAL in which Hansa-II was built as a prototype and Hansa-III was finalized for production. This aircraft fully satisfies my problem statement so I chose this particular aircraft for my study. To fetch the flight data, multi-variant sensors are instrumented in the aircraft for flight data acquisition. The aircraft structure is fully composite having a low wing configuration with a tricycle landing gear arrangement. It consists of a Rotax-914 F3 engine coupled with a Hoffmann propeller (NAL, 2000). A Flight test is carried out to record an enormous amount of longitudinal flight data for evaluating longitudinal parameters using the Maximum likelihood method (Jategaonkar, 2015). The flight tests at different altitudes such as (4000ft, 6000ft, and 8000ft) at 1200 N thrust were conducted. Elevator control inputs such as multistep, doublet, and pulse were accustomed for generating flight data at low AOA. The raw data is computed in the form of velocity (V), rates (p, q, r), pitch angle ( $\theta$ ), yaw angle( $\psi$ ), roll angle ( $\phi$ ), deflection angles ( $\delta_e$ ,  $\delta_a$ ,  $\delta_r$ ) accelerations  $(a_x, a_y, a_z)$ ,  $\alpha$ , and  $\beta$  for locating the sensors position. An accelerometer reading measures accelerations in the body axes that are in close proximity to the C.G. The deflections by control surfaces  $\delta_e$  are measured through a potentiometer. The Gyroscope measures the angular rates (p, q, r) and  $(\dot{p}, \dot{q}, \dot{r})$  are calculated from angular rates numerical differentiation (p, q, r). OAT gauze measures the temperature. Some calibration factors and correction factors are recommended while sensor measurement so that they can be incorporated into the mathematical modeling of aircraft.

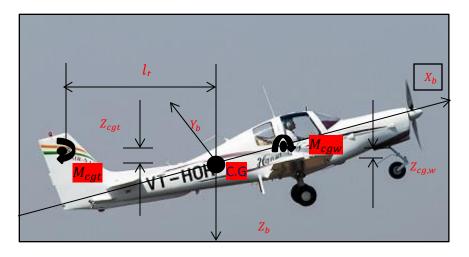


Fig 4.1 Wing and Tail Contribution to the Pitching Moment of Hansa-III

### Flight Data at Low Angle of Attack

In terms of voltage (3-2-1-1) multi-step, doublet, and pulse input types, the raw flight data was recorded. The raw data was converted using the relevant calibration chart into the corresponding motion and control variables. Figures 4.5-4.9 presented below show five data sets of longitudinal multistep 3211 Input form (HALM1, HALM2, HALM3, HALM4, and HALM5), one dataset (HALD1) and two datasets (HALP1, HALP2) were generated using the elevator as input. Figure 4.2 discusses below mentioned ( $\delta_e$ ) elevator deflection angle, ( $\alpha$ ) angle of attack, ( $\theta$ ) pitch angle, (q) pitch rate, (V) velocity, ( $a_x$ ) acceleration along the x-axis and ( $a_z$ ) acceleration along the z-axis in the graphical representation.

About the trim state, the elevator deflects by ( $\pm 2$  to  $\pm 6$  degrees). The Xaxis and Z-axis linear accelerations ( $a_x$ ,  $a_z$ ) at trim conditions are 1 ms<sup>-2</sup> and -10 ms<sup>-2</sup>, The  $\alpha_{trim}$  varies from 2-10 deg and the perturbation speed is 56m/s. The state variables  $\alpha$ ,  $\theta$ ,  $\beta$ ,  $\psi$ ,  $\delta_e$ ,  $\varphi$  in degree  $a_x$ ,  $a_y$ ,  $a_z$  are in m/s<sup>2</sup> p, q, r in degree/s, and V in m/s.

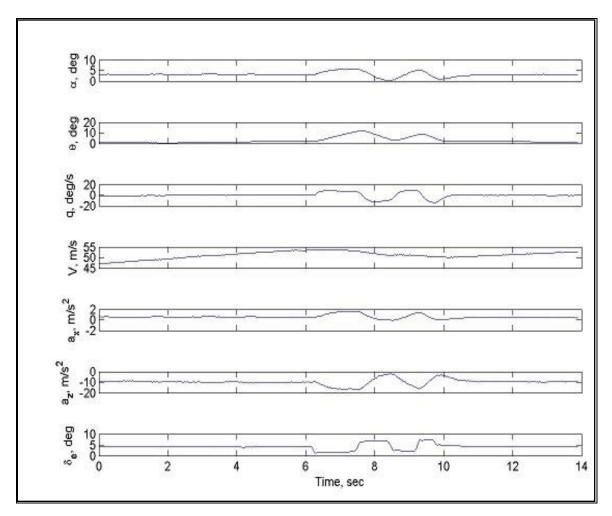


Fig 4.2 Flight Dataset Pre-processing HALM5

Figure 4.2 shows the processed longitudinal flight data about HALM5 input form including motion variables ( $\alpha$ ) angle of attack in degrees, ( $\theta$ ) pitch angle in degrees, (q) pitch rate in degree/s, (V) velocity in m/s, ( $a_x$ ) acceleration along the x-axis and ( $a_z$ ) acceleration along the z-axis in m/s<sup>2</sup>

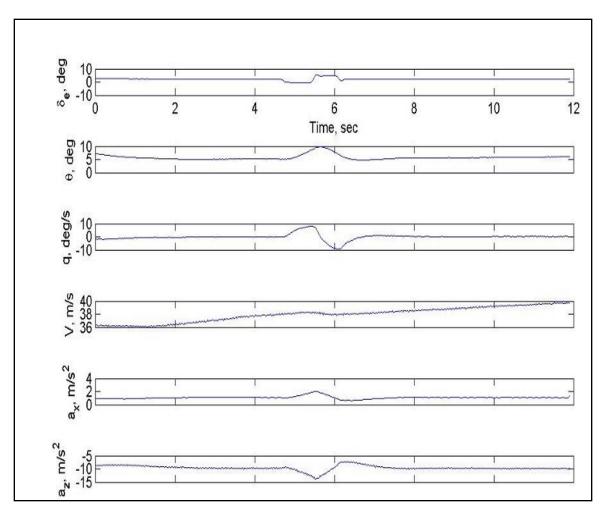


Fig 4.3 Flight Dataset Pre-processing, HALD1

Figure 4.3 shows the processed longitudinal flight data about doublet HALD1 input form including motion variables ( $\alpha$ ) angle of attack in degrees, ( $\theta$ ) pitch angle in degrees, (q) pitch rate in degree/s, (V) velocity in m/s, ( $a_x$ ) acceleration along the x-axis and ( $a_z$ ) acceleration along the z-axis in m/s<sup>2</sup>

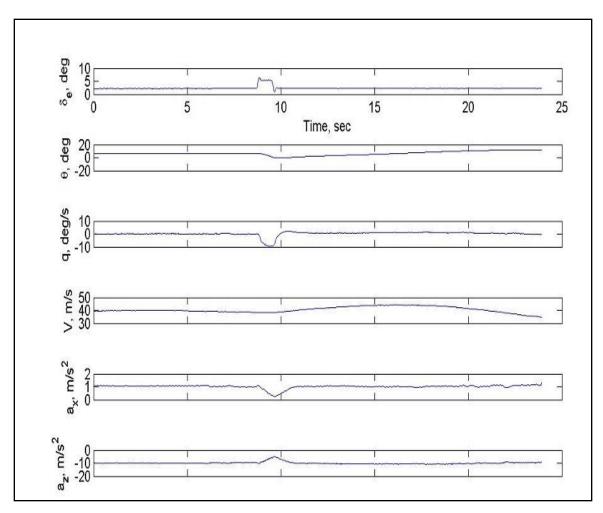


Fig 4.4 Flight Dataset Pre-processing, HALP1

Figure 4.4 shows the processed longitudinal flight data about the Pulse HALP1 input form including motion variables ( $\alpha$ ) angle of attack in degrees, ( $\theta$ ) pitch angle in degrees, (q) pitch rate in degree/s, (V) velocity in m/s, ( $a_x$ ) acceleration along the x-axis and ( $a_z$ ) acceleration along the z-axis in m/s<sup>2</sup>

The three variations of Elevator Control Input: Multi-step (3-2-1-1), Doublet, and Pulse are presented in this chapter. The pilot executes these three elevator forms by deflecting the elevator from its trim state to acquire longitudinal data.

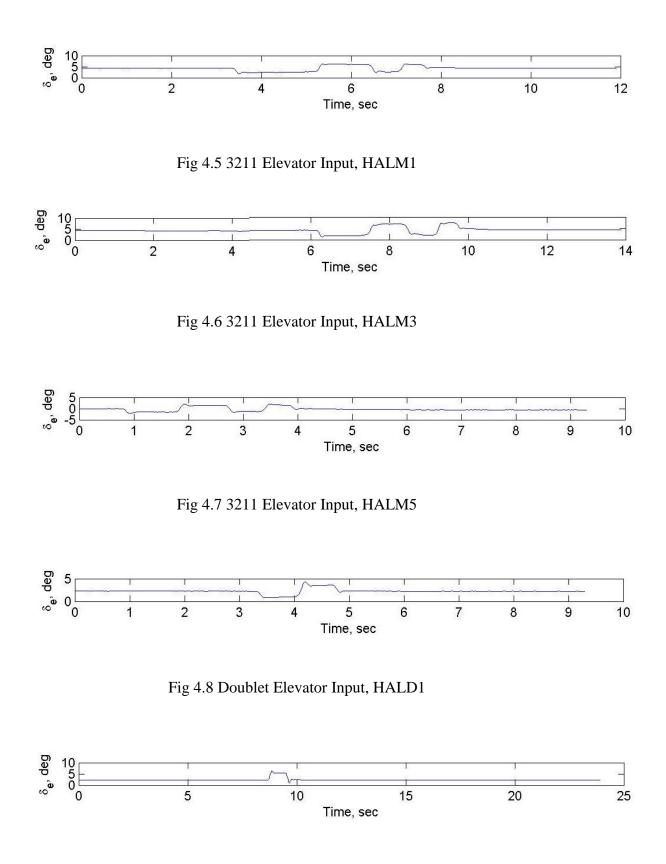


Fig 4.9 Pulse Elevator Input, HALP1

Figures 4.5 - 4.9 present different forms of elevator control input at the low and moderate angles of attack to generate longitudinal datasets.

### 4.2 DATA COMPATIBILITY CHECK

Sensors that detect accelerations, locations, and rates related to the translational and rotational motion of the C.G. and additionally orientation/ magnitude of the velocity of the relative air are part of the instrumentation on Research Cum trainer aircraft To verify that the measurements are mutually consistent, kinematic relationships between the attributes are used. The analysis is termed data compatibility analysis (Klien & Morelli, 2006)

Data compatibility analysis demonstrates that the kinematic relations satisfy the sensor measurements if the measurements are perfect. Practically, Sensor Measurement includes a systematic error, as well as random errors thus these equations, serve as tools for calibrating the instrumentation errors as well as correcting the measured data from the sensors to estimate systematic errors. Accuracy and consistency is prerequisite for modelling the structure and parameter estimation. Consequently, these measurements are applied to rigid aircraft that are checked for compatibility. Processed flight data include systematic and random error which requires to be removed.

The chapter covered data compatibility checks for the Hansa-III flight data. The systematic errors includes zero shift biases, scale factors, and time shifts that make data incompatible to be used. In the context of the parameter Estimation of an aircraft, an enormous variable is measured and recorded during testing. therefore, a data compatibility check must be carried out before parameter estimation.

The goal of flight path reconstruction (FPR), also known as data compatibility check, was to confirm that the measurements used to identify the model were accurate and consistent. Data Compatibility is first introduced by

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Gerlachin in 1966, for flight path reconstruction. All biases are measured and initial conditions were evaluated by Mulder 1975(Klien & Morelli, 2006)

#### **Mathematical Model**

The six DOF model consists of kinematic equations, recorded angular rates, and measured accelerations.

1) Determination of systematic error that includes zero shifts, scale factors, and time delays.

2) Generation of aircraft states such as velocity components, which implies state estimation.

The bias and scale factor present in the measured state variable using the Maximum Likelihood MATLAB Code (Jategaonkar, 2015). The following equations used for reconstructing the dynamics of RCTA Aircraft are mentioned in the below section

### **Kinematic Equations**

These equations are sets of translational, rotational, and navigation equations on body-fixed axis.

### Translational Equations

$\dot{u} = -q w + r v - g \sin \theta + a_x \qquad 4.1$
---

 $\dot{v} = -r \, u + pw + g \sin \theta \cos \varphi + a_y \tag{4.2}$ 

 $\dot{w} = -p v + q u + g \sin \theta \cos \varphi + a_z$  4.3

### **Rotational Equations**

 $\dot{\varphi} = p + q \sin \varphi \tan \theta + r \cos \varphi \tan \theta \qquad 4.4$ 

$\dot{\theta} = q \cos \varphi - r \sin \theta$	4	5

 $\dot{\psi} = q \sin \varphi \sec \theta + r \cos \varphi \sec \theta \qquad 4.6$ 

#### Navigational Equations

$$\dot{x}_{E} = u \cos \psi \cos \theta + v (\cos \psi \sin \theta \sin \varphi - \sin \psi \cos \varphi)$$

$$+ w (\cos \psi \sin \theta \cos \varphi + \sin \psi \sin \varphi)$$

$$\dot{y}_{E} = u \sin \psi \cos \theta + v (\sin \psi \sin \theta \sin \varphi + \cos \psi \cos \varphi) + w (\sin \psi \sin \theta 4.8$$

$$\cos \varphi - \cos \psi \sin \varphi)$$
$$\dot{h} = u \sin \theta - v \cos \theta \sin \varphi - w \cos \theta \cos \varphi$$
4.9

The above equations are nonlinear, coupled differential equations. The equations contain (u, v, w),  $(\psi, \theta, \varphi)$ ,  $(x_E, y_E, h)$ , (p, q, r), and  $(a_x, a_y, a_z)$  as state variables that can be evaluated using measured angular rates, and linear accelerations. Based on an estimation of the above state variables, utilizing the equations provided below, it is simple to deduce other variables as well.

$$V = \sqrt{u^2 + v^2 + w^2} \tag{4.10}$$

$$\alpha = \tan^{-1}(\frac{w}{u}) \tag{4.11}$$

$$\beta = \sin^{-1}(\frac{v}{v}) \tag{4.12}$$

$$\overline{q} = \frac{1}{2} \rho \, \mathrm{V}^2 \tag{4.13}$$

Since the effects of flight under given operating conditions are not easy to test in a laboratory thus calibration is essential for error elimination from flight data. Let us consider the sensor model equation in terms of biases, time delay, scale factor, and measured variable ' $y_m$ ' as

$$y_{m}(t) = k_{y} y(t - \zeta) + \Delta y \qquad 4.14$$

Where k stands for scale factor,  $\Delta$  is bias effect and  $\zeta$  the time delay. Ideally, the value of scale-factor must come unity. The bias factor ( $\Delta$ ), and time-delay ( $\zeta$ ) should be negligible. It is assumed to be a constant instrumentation error. The linear accelerations calibrated at COG are estimated from acceleration  $(a_{x m} A^{S})$ , a ym<sup>AS</sup>, a zm<sup>AS</sup>) by using a navigational sensor, accelerometer, and X, Y, Z in equation (4.15-4.17) refers to the position of accelerometer (R. Kumar, 2012)

$$a_{x CG} = a_{x m} + (q^{2} + r^{2}) X + (p q - r) Y - (p r + q) Z - \Delta a_{x}$$

$$4.15$$

$$a_{yCG} = a_{ym} \cdot (pq+r) X + (p^2+r^2) Y \cdot (qr-p) Z \cdot \Delta a_y$$
4.16

$$a_{zCG} = a_{zm} - (p r - q) X - (q r - p) Y + (p^2 + q^2) Z - \Delta a_z$$

$$4.17$$

Where subscript *m* refers to measured quantities. XASCG, YASCG, and ZASCG as accelerometer positions to COG. The bias measurement a  $_x$   $^{CG}$ , a  $_y$   $^{CG}$ , a  $_z$   $^{CG}$  indicated by  $\Delta$  a  $_x$ ,  $\Delta$  a  $_y$  and  $\Delta$  a  $_z$ The rates p, q, and r stand for  $p_m - \Delta p$ ,  $q_m - \Delta q$  and  $r_m - \Delta r$  acquired from measured rates ( $p_m$ ,  $q_m$  and  $r_m$ ) correcting biases ( $\Delta p, \Delta q$ , and  $\Delta r$ ). The state equations (4.18-4.24) incorporate the bias term as given below. Refer Appendix C

$$\dot{u} = -(q_m - \Delta q)w + (r_m - \Delta r)v - g\sin\theta + a_x^{CG}$$

$$4.18$$

$$\dot{v} = -(r_m - \Delta r) u + (p_m - \Delta p) w + g \cos \theta \sin \varphi + a_y^{CG}$$

$$4.19$$

$$\dot{w} = -(p_m - \Delta p)v + (q_m - \Delta q)u + g\cos\theta\cos\varphi + a_z^{CG}$$

$$4.20$$

$$\dot{\varphi} = (p_m - \Delta p) + (q_m - \Delta q) \sin \varphi \tan \theta + (r_m - \Delta r) \cos \varphi \tan \theta \qquad 4.21$$

$$\dot{\theta} = (q_m - \Delta q) \cos \varphi - (r_m - \Delta r) \sin \varphi \qquad 4.22$$

$$\dot{\psi} = (q_m - \Delta q) \sin \varphi \sec \theta + (r_m - \Delta r) \cos \varphi \sec \theta \qquad 4.23$$

$$\dot{h} = u \sin \theta - v \cos \theta \sin \varphi \cdot w \cos \theta \cos \varphi \qquad 4.24$$

.

The sideslip angle and the angle of attack at nose-boom modelled in term of scale factor and bias is given below where variables  $k_{\alpha}$  and  $k_{\beta}$  stands for scale factors,  $\Delta \alpha_{NB}$  and  $\Delta \beta_{NB}$  as biases for  $\alpha$ , and  $\beta$ .

$$V_{\rm m} = \sqrt{u^2 + v^2 + w^2} \tag{4.25}$$

$$\alpha_{NB, m} = K_{\alpha} \tan^{-1} (w_{NB}/u_{NB}) + \Delta \alpha_{NB}$$

$$4.26$$

$$\beta_{NB, m} = K_{\beta} \sin^{-1} \left( \frac{v_{NB}}{(u_{NB}^{2} + V_{NB}^{2} + w_{NB}^{2})^{1/2}} \right) + \Delta \beta_{NB}$$

$$4.27$$

$$\varphi_{\rm m} = \varphi \tag{4.28}$$

$$\Psi_{\rm m} = \Psi \tag{4.29}$$

$$\mathbf{h}_{\mathrm{m}} = \mathbf{h} \tag{4.30}$$

The  $x_{NBCG}$ ,  $y_{NBCG}$ , and  $z_{NBCG}$  stand for offset distances taken from COG in the below equation, and at the aircraft nose-boom the velocity components are given by

$$U_{NB} = \mathbf{u} - (r_m - \Delta r) y_{NBCG} + (q_m - \Delta q) z_{NBCG}$$

$$4.31$$

$$V_{NB} = v - (p_m - \Delta p) z_{NBCG} + (r_m - \Delta r) x_{NBCG}$$

$$4.32$$

$$W_{NB} = w - (q_m - \Delta q) x_{NBCG} + (p_m - \Delta p) y_{NBCG}$$

$$4.33$$

#### **Compatibility Factors Calculation Using Longitudinal Actual Flight Data**

Flight path Reconstruction using ML Matlab code was taken on real processed data at a low-moderate angle of attack applying observations equation (Jategaonkar, 2015)

Figure 4.10 - 4.12 displays the input variables  $\alpha$ ,  $\theta$ ,  $\beta$ , q,  $a_Z$  and V measured and estimated responses.

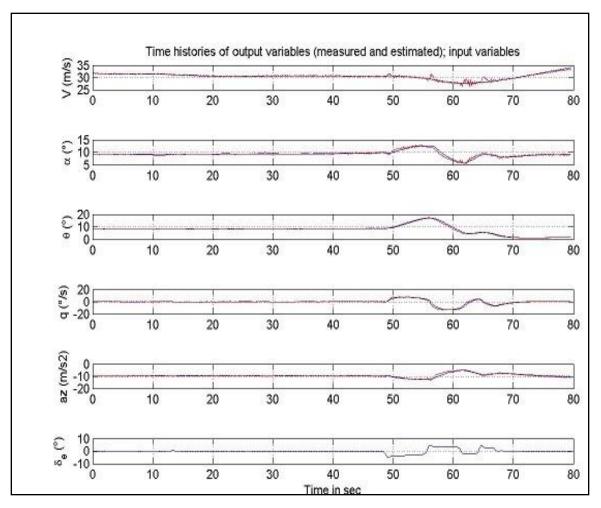


Figure 4.10 displays measured and estimated responses of longitudinal motion variables ( $\theta$ , a <sub>z</sub>,  $\alpha$ , q, V,  $\delta$  <sub>e</sub>) obtained from FPR for multistep HALM5 Input form

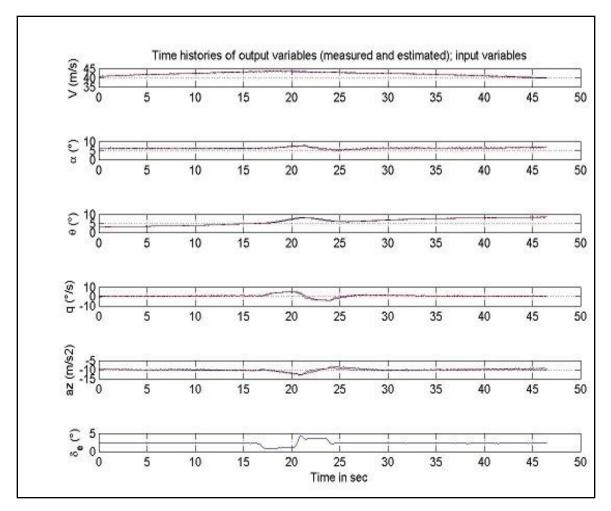


Figure 4.11 displays measured and estimated responses of longitudinal motion variables ( $\theta$ , a <sub>z</sub>,  $\alpha$ , q, V,  $\delta$  <sub>e</sub>) obtained from FPR for doublet HALD1 Input form.

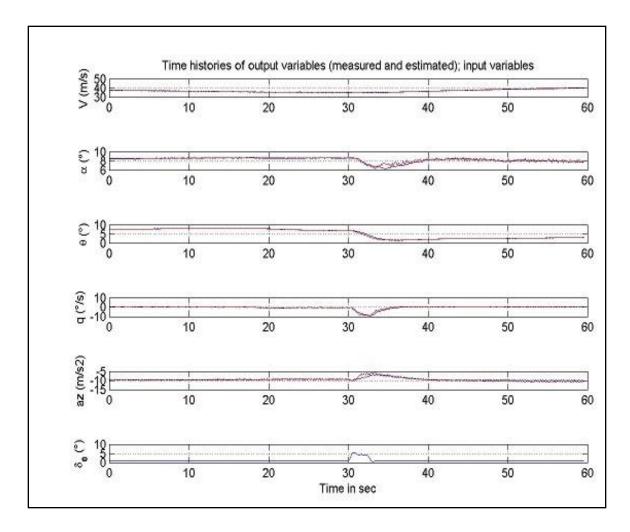


Figure 4.12 displays measured and estimated responses of longitudinal motion variables ( $\theta$ , a <sub>z</sub>,  $\alpha$ , q, V,  $\delta$  <sub>e</sub>) obtained from FPR for pulse HALP1 Input form.

It is remarked from the above figures that estimated responses compliment well with given measured responses. It is found that the desired control input is enforced so fast that velocity variation is slightly low which mismatches the estimated response with the measured one.

The estimation of scale factors using the Maximum Likelihood method to check data compatibility is represented below (R. Kumar, 2012)

$$\Theta = [\Delta p \Delta q \,\Delta r \Delta a x \Delta a y \,\Delta a \, z \Delta \alpha \Delta \, k \alpha]^{\mathrm{T}}$$

$$4.34$$

The unknown vector represents bias and scale factor for the reconstruction of longitudinal dynamics of RCTA aircraft. The ML technique is used for the estimation of compatibility factors. The level of parameter accuracy is evaluated by the Cramer-Rao bounds.

Table 4.1 presented in the below section shows the values of bias, and scale factor  $(\Delta k\alpha)$  in the form of  $\Delta p\Delta q \Delta r\Delta a x\Delta a y \Delta a z\Delta \alpha \Delta k\alpha$  for all data-sets. It has been noted that the scale factor value is nearly one and bias is assumed to be negligible. The deviation in the values of these factors is due to interference effects produced by the propeller or atmospheric turbulence thus slight deviation in these factors is assumed during flight test.

S. No	Data	$\Delta a_x$	Δa <sub>y</sub>	$\Delta a_z$	Δp	Δq	Δr	Κα	Δα
1	HALM1	0.412	-0.218	-0.59	0.0019	-0.00075	-0.0059	0.93	0.045
2	HALM2	0.238	-0.235	-0.297	0.0015	-0.0015	-0.0058	0.85	0.045
3	HALM3	0.089	0.086	-0.012	-0.0004	-0.0009	0.0037	1.01	0.039
4	HALM4	0.137	-0.115	-0.286	-0.0001	-0.0015	-0.0021	0.91	0.143
5	HALM5	-0.35	-0.087	-0.178	-0.000048	-0.0029	-0.0004	0.7	0.02
6	HALD3	0.814	0.116	-0.454	-0.000005	0.00001	-0.0035	0.89	0.194
7	HALP1	1.01	0.15	-0.09	0.000003	0.00002	0.00001	0.87	0.073
8	HALP2	0.11	0.135	0.0151	-0.0003	-0.0007	0.002	0.92	0.075

Table 4.1: Estimation of Scale factor and bias factor

Table 4.1 shows the scale and bias factor of different data sets and it is observed that data set HALM3 of multi-step elevator input has the value of scale factor is 1.01 which illustrates its relevancy from other datasets.

### 4.3 AERODYNAMIC MODELING OF HANSA-III AIRCRAFT

Equations of motion are used to create the mathematical model of the Hansa-III aircraft. The aerodynamic forces and moments will be estimated using this. The

flight test was carried on at different manoeuvres of the elevator such as multi-step, doublet, and pulse input. It is mostly found that longitudinal motion predominantly excites short-period mode rather than phugoid thus short- period equations are used to estimate longitudinal parameters. These equations are a set of state equations, observation equations, and equations of motion (refer to Appendix C)

*Governing Longitudinal Equation in Wind Axis in short-period mode* (Peyada et al., 2008) (Jategaonkar, 2015)

### **Force Equation**

$$\dot{V} = -\left\{\frac{\bar{q}.s}{m}\right\} C_D + g \sin(\alpha - \theta) + \left\{\frac{T}{m}\right\} \cos \alpha$$

$$4.35$$

$$\dot{\alpha} = -\left\{\frac{\bar{q}.s}{m.v}\right\} C_L + q + \frac{g}{v} \cos(\alpha - \theta) - \left\{\frac{T}{m.v}\right\} \sin \alpha$$

$$4.36$$

$$\dot{\theta} = q \tag{4.37}$$

#### **Moment Equation**

$$\dot{q} = \left(\frac{\bar{q}.s.c}{l_y}\right). C_m + \left\{\frac{T}{l_{YY}}\right\} l_{tz}$$

$$4.38$$

To analyse the aircraft dynamics, the aircraft is modelled in terms of mathematical equations as aerodynamic stability and control derivatives shown below

$$C_{L} = \{ C_{L_{0}} + C_{L_{\alpha}} \cdot \alpha + C_{L_{q}} \cdot \frac{q\bar{c}}{2U_{1}} + C_{L_{\delta_{e}}} \cdot \delta_{e} \}$$

$$4.39$$

$$C_D = \left\{ C_{D_0} + C_{D_\alpha} \cdot \alpha + C_{D_q} \cdot \frac{q\bar{c}}{2U_1} + C_{D_{\delta_e}} \cdot \delta_e \right\}$$

$$4.40$$

$$C_m = \left\{ C_{m_0} + C_{m_\alpha} \cdot \alpha + C_{m_q} \cdot \frac{q\bar{c}}{2U_1} + C_{m_{\delta_e}} \cdot \delta_e \right\}$$

$$4.41$$

Assumptions:

Thrust setting angle = 0; Flight path  $\gamma$  = constant at cruise state; flight velocity is constant as elevator control input excites short-period dynamics(JAISWAL & PRAKASH, 2022)

Simplified longitudinal state equation to estimate non-dimensional derivatives as longitudinal stability and control predominantly excite short-period mode

$$\dot{\alpha} = -\left\{\frac{\overline{q}.s}{m.\nu}\right\}C_L + q \tag{4.42}$$

$$\dot{\theta} = q \tag{4.43}$$

$$\dot{q} = \left(\frac{\bar{q}.s.c}{I_y}\right).C_m \tag{4.44}$$

Simplifying set of equations

$$\dot{\alpha} = q - \frac{\rho V S_w}{2m} \{ C_{L_0} + C_{L_{\alpha}} \cdot \alpha + C_{L_q} \cdot \frac{q\bar{c}}{2U_1} + C_{L_{\delta_e}} \cdot \delta_e \}$$

$$4.45$$

$$\dot{\theta} = q \tag{4.46}$$

$$\dot{q} = \frac{\rho V^2 S_w \bar{c}}{2Iy} \{ C_{m_0} + C_{m_\alpha} \cdot \alpha + C_{m_q} \cdot \frac{q\bar{c}}{2U_1} + C_{m_{\delta_e}} \cdot \delta_e \}$$

$$4.47$$

The parameter vector ( $\Theta$ ) determines the value of non-dimensional longitudinal derivatives which is given as (R. Kumar, 2012)

$$\Theta = \left[C_{L_0} C_{L_a} C_{L_{\delta e}} C_{D_0} C_{D_{\delta e}} C_{m_0} C_{m_{\alpha}} C_{m_{\alpha}} C_{m_{\delta e}}\right]^{\mathrm{T}}$$

$$4.48$$

# 4.4 METHODOLOGY OF PARAMETER ESTIMATION

### Maximum Likelihood

Maximum likelihood is generally applicable for estimating longitudinal

derivatives of dynamic models utilizing actual flight data. M.L estimators are reliable, effective, efficient, and used for covariance matrices with no state noise. It is formulated by minimizing Cost function 'J' which is the difference between measured and estimated response as expressed in equation(Jategaonkar, 2015)(R. Kumar, 2012) (Jaiswal et al., 2020)

$$J(\Theta, R) = L(z|\Theta, R) = \frac{1}{2} \sum_{k=1}^{N} [z(tk) - y(tk)]R - 1 [z(tk) - y(tk)] + N/2 \quad 4.49$$
  
ln [det(R)] + Nn<sub>y</sub>/2 ln(2]])

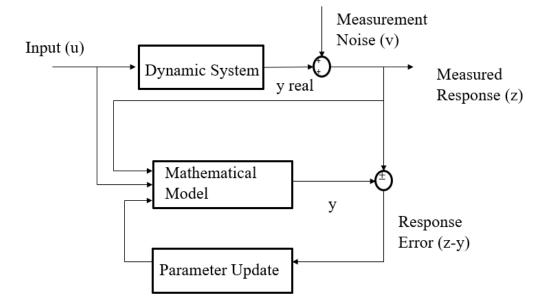


Figure 4.13 Output Error Method

#### **Properties of Maximum likelihood function**(Jategaonkar, 2015):

1. Asymptotically unbiased is a characteristic property of maximum likelihood estimates  $\lim_{n \to \infty} E(\Theta_{ML}) = \Theta$ 

2. The novel feature of maximum likelihood estimates is that they are asymptotically consistent.

3. The estimates ML have the virtue of being asymptotically efficient with respect to the statistical precision bounds known as Cramer Rao bounds.

# PARAMETER ESTIMATION

The longitudinal derivatives were estimated using the compatible flight data corresponding to various control inputs, including multi-step [3211], doublet, and pulse using the ML code (Jategaonkar, 2015)

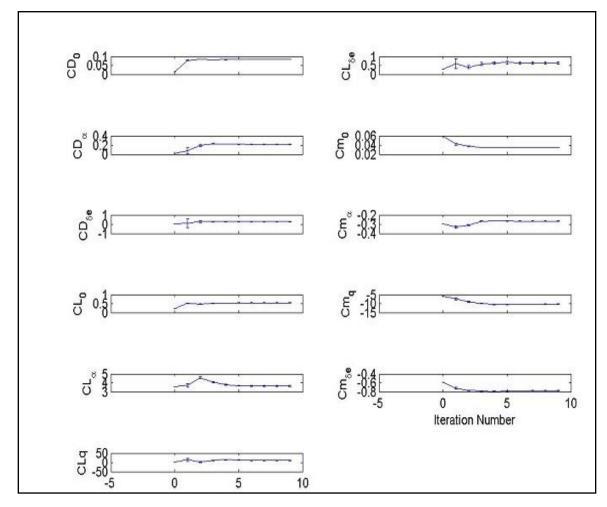


Fig 4.14 shows the convergence of HALM5 Multi-step Input in terms of Aerodynamic Derivatives  $(C_{L_q}, C_{L_{\alpha}}, C_{D_0}, C_{D_{\alpha}}, C_{D_{\delta e}}, C_{m_q}, C_{m_0}, C_{m_{\alpha}}, C_{m_{\delta e}})$ 

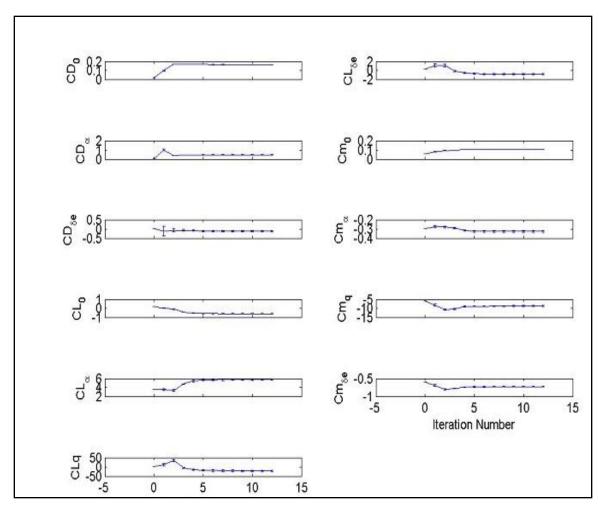


Fig 4.15 shows the convergence of HALD1 Doublet Input in terms of Aerodynamic Derivatives ( $C_{L_q}$ ,  $C_{L_{\alpha}}$ ,  $C_{D_0}$ ,  $C_{D_{\alpha}}$ ,  $C_{D_{\delta e}}$ ,  $C_{m_q}$ ,  $C_{m_0}$ ,  $C_{m_{\alpha}}$ ,  $C_{m_{\delta e}}$ )

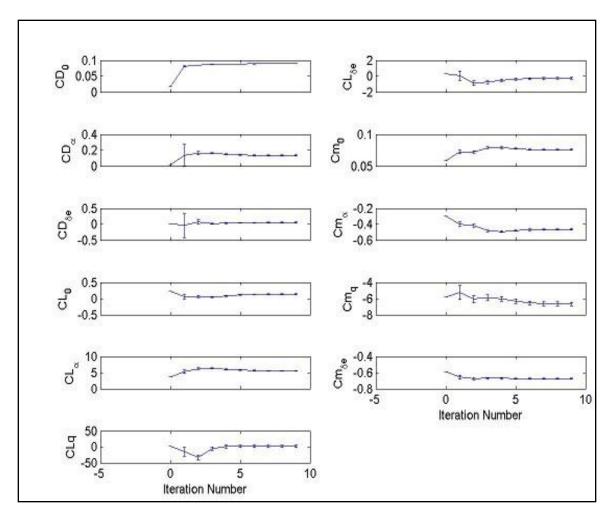


Fig 4.16 shows the convergence of HALP1 Pulse Input in terms of Aerodynamic Derivatives  $(C_{L_q}, C_{L_{\alpha}}, C_{L_0}, C_{D_0}, C_{D_{\alpha}}, C_{D_{\delta e}}, C_{m_q}, C_{m_0}, C_{m_{\alpha}}, C_{m_{\delta e}})$ 

Figures presented in the above section show the estimated response of derivatives  $(C_{L_q}, C_{L_{\alpha}}, C_{L_0}, C_{D_0}, C_{D_{\alpha}}, C_{D_{\delta e}}, C_{m_q}, C_{m_0}, C_{m_{\alpha}}, C_{m_{\delta e}})$  The ML technique is applied to eight data- sets of elevator input as a multi-step, doublet, and Pulse for parameter estimation.

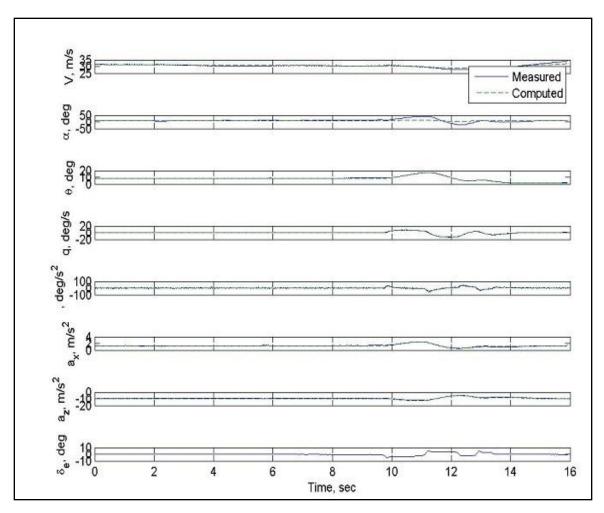


Fig 4.17 The measured and computed results obtained from ML: HALM5

Figures 4.17 presented in the above section measure the estimated and measured response of variables ( $\alpha$ ,  $\theta$ , q,  $a_x$ , and  $a_z$ ) through the X, Z body axis in the act of parameter estimation. The data sets' responses HALM5 show a strong correlation between the estimated and measured motion variables

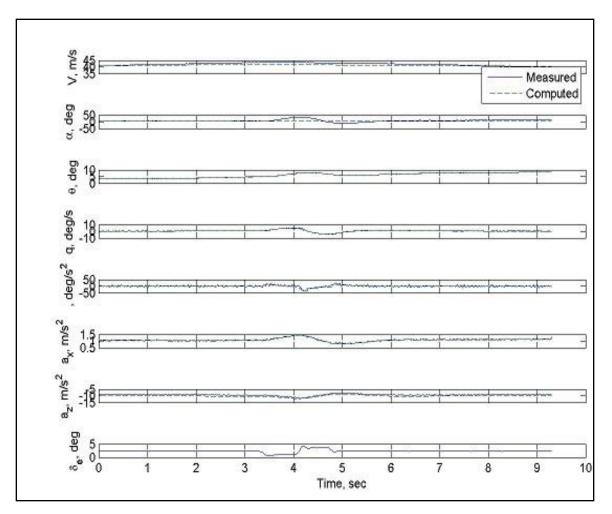


Fig 4.18 The measured and computed results obtained from ML: HALD1

Figure 4.18 presented in the above section measure the estimated and measured response of variables ( $\alpha$ ,  $\theta$ , q,  $a_x$ , and  $a_z$ ) through the X, Z body axis in the act of parameter estimation. The data sets' responses HALD1 show a strong correlation between the estimated and measured motion variables.

Table 4.2 presents the numeric value of parameters estimated through the ML method. It is observed from the tabulated data that the value of parameters is accurate and close to wind tunnel values.

Data	$C_{D_0}$	$C_{D_{\alpha}}$	$C_{D_{\delta e}}$	$C_{L_0}$	$C_{L_a}$	$C_{L_{\delta e}}$	$C_{m_0}$	$C_{m_{\alpha}}$	$C_{m_{\delta e}}$	$C_{m_q}$
W.T	0.035	0.086	0.026	0.354	4.97	0.26	0.052	-0.4596	-1.008	
HALM1	0.059	0.263	0.165	0.037	5.964	0.194	0.078	-0.407	-0.734	-8.57
HALM2	0.053	0.216	0.136	0.0842	5.69	0.184	0.076	-0.429	-0.711	-8.11
HALM3	0.0588	0.093	0.058	-0.18	3.94	0.5367	0.071	-0.35	-0.851	-11.1
HALM4	0.145	0.408	0.202	0.1141	6.16	0.27	0.0918	-0.6437	-0.909	-6.77
HALM5	0.0408	0.0282	0.0473	0.2254	6.4592	0.0196	0.0787	-0.4259	-	-
HALD1	0.2178	0.344	-0.577	-0.44	3.75	-2.027	0.183	-6.67	-0.51	-0.642
HALP1	0.164	0.463	-0.128	-0.606	5.78	-0.818	0.103	-8.67	-0.33	-0.728

Table 4.2: ML-based parameter estimation technique for the longitudinal

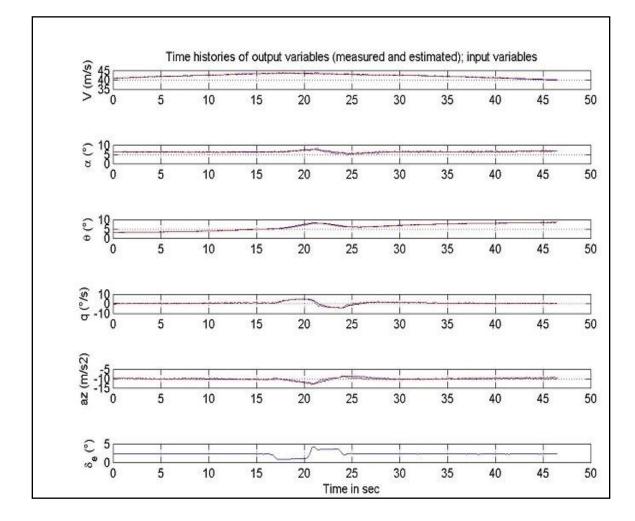
case: Multi- step, Doublet, and Pulse Inputs

Table 4.2 exhibit that obtained values of aerodynamic derivatives using ML is reasonably accurate. The value of  $C_{L_{\alpha_i}} C_{m_{q_i}}, C_{m_{0,}}, C_{m_{\delta,e_i}} C_{m_{\alpha_i}}, C_{D_{0_i}}$  is seen to approach wind tunnel values for most data sets and shows a slight variation in parameters such as  $C_{L0}$ ,  $C_{D\alpha}$ . The variance in the value from the wind tunnel is ignored since the weak parameters  $C_{L_{\delta,e_i}} C_{L_{q_i}}$ , and  $C_{D_{\delta,e_i}}$  have a minimal impact compared to the strong ones. It is also found that rare techniques are available to determine the accurate value of the weak parameters due to the unavailability of proper flight data or elevator input is not able to follow the desired variation.

Additionally, one observation is noticed that there is a maximum deviation in the values from the Wind Tunnel result in the case of pulse Input as compared to Multistep and Doublet. The Multi-step is more consistent as compared to different elevator Inputs. The results depicted in tabulated form provide information to the researcher about the Control Input types respectively.

#### **4.5 VALIDATION**

Model Validation is a proof-match exercise that is carried out by making use of the flight dataset HALM4 corresponds to the doublet input HALD1. The response was estimated by resolving six degrees of freedom Equations of motion. It is noticed



that the estimated response from HALM4 is close to the measured response of HALD1 and validates the result.

Fig.4.19 Parameter estimation from HALM4 and validation using HALD1

The results are also validated with the results that came from wind tunnel results as well as a reference paper. The results of strong derivatives are validated as they predominantly influence the stability and control of the system. MLH35 is the data set referred from the research paper as presented in Table 4.3 (R. Kumar, 2012)

Data	$C_{L_0}$	$C_{L_a}$	$C_{L_{\delta e}}$	$C_{m_0}$	$C_{m_{\alpha}}$	$C_{m_{\delta e}}$	$C_{m_q}$
W.T	0.354	4.97	0.26	0.052	-0.4596	-1.008	
MLH35	0.092	5.409	0.282	0.073	-0.395	-0.719	-9.406
HALM1	0.037	5.964	0.194	0.078	-0.407	-0.734	-8.57
HALM2	0.0842	5.69	0.184	0.076	-0.429	-0.711	-8.11
HALM3	-0.18	3.94	0.5367	0.071	-0.35	-0.851	-11.1
HALM4	0.1141	6.16	0.27	0.0918	-0.6437	-0.909	-6.77
HALM5	0.2254	6.4592	0.0196	0.0787	-0.4259	-0.8665	-11.612

Table 4.3: Compared Results of Longitudinal Derivatives of Wind-Tunnel, Multistep Datasets, and MLH35 (R. Kumar, 2012)

The bar pictorial representation of Longitudinal Derivatives of Hansa-III is compared with the results of Wind-Tunnel, Dataset HALM5, and MLH35 (R. Kumar, 2012) in Fig 4.20

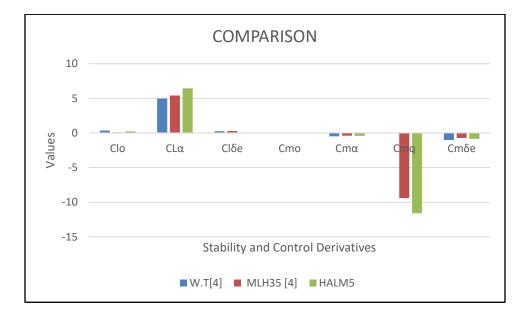


Fig 4.20 Compared Results of Wind-Tunnel, Dataset HALM5, and MLH35[10] in term of Graphical representation.

The result of multiple data sets is compared in the form of bar representation and the dataset HALM5 shows minimum variation with wind tunnel result as presented

in Table 4.3 thus the values of coefficients of HALM5 are utilized to calculate the transfer function of the pitch controller for execution of the second objective.

### **SUMMARY:**

In this chapter, a flight test of Hansa-III was conducted for file processing. The Data Compatibility is checked for processed flight data to ensure measurements used in the model are error-free. Once the FPR is ensured then the equations of motion in the wind axis were used to formulate the aircraft mathematical model (refer to section 5.3) and longitudinal aerodynamic derivatives were estimated using ML Code (Jategaonkar, 2015). Model Validation is exercised once the parameters are estimated. Different datasets were used for designing the controller using different approaches as discussed in Appendix D1,D2.

# CHAPTER -5

# AIRCRAFT CONTROLLER DESIGN

This chapter addresses the introduction of aircraft stability, dynamics & automatic control. Hence, developing the expression of deriving six DOF equations of motion, linearized longitudinal perturbation equations, and longitudinal equations of motion in wind axes, the axes system is reviewed. Classical control theory and modern control theory is applied to design control system. To apply traditional, classical theory to design a control system, it is important to understand the concept of transfer function whereas, the concept of state-space formulation of system from governing equations is important for modern control methods. Both approaches are important to design control systems. The chapter discussed open-loop / closed-loop PID tuning techniques to the PID controller's gain parameters. The pitch controller is designed using Root-locus, Pole-placement, and Linear quadratic regulator methods for optimal results. Simulated Results of traditional, classical, and modern control methods are compared in this chapter.

#### **5.1 CONTROL SYSTEM**

Advanced level of control systems involved in all engineering disciplines such as aerospace automation, missile guidance, and control systems, robotics engineering, automotive, and space science. Hence it is necessary to be familiar with the basics of the control system. This chapter focuses on control system analysis both in the time and frequency domain as well a glimpse of an aircraft control system is introduced with a clear explanation. A system comprises the number of components assigned to perform a specific task. The system is described as a control system since the input controls the output variable in it.

# **Classification:**

1. Open-Loop and Closed-Loop Control System

# **Open-loop**:

A system where measured output is independent of controlled activity. It consists of a system, controller, Input, and output signals for example:

- 1. Electric bulb
- 2. Stepper motor
- 3. Switching ON Fan

Advantages:

- 1. Simpler
- 2. Economical to operate.
- 3. A less complex system reduced maintenance cost
- 4. Highly Stable

Dis-Advantages:

- 1. Less accurate and reliable.
- 2. Calibration is required from time to time

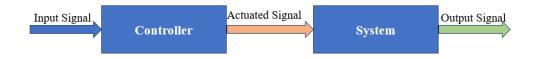


Fig 5.1 Open-loop Control System

# **Closed-loop**:

A system where controlled action depends on measured output is additionally known as a feedback control system. It consists of a system, controller, Input, output, feedback, and actuators for example:

- 1. An autopilot controller
- 2. Speed control of DC Motor
- 3. Missile/ Rocket Launcher system

### Advantages:

- 1. High accuracy than open-loop systems.
- 2. Recalibration is not required
- 3. Automation Facility
- 4. Robustness

**Dis-Advantages:** 

- 1. More Complex system increases maintenance cost
- 2. Less stable than the open-loop control system

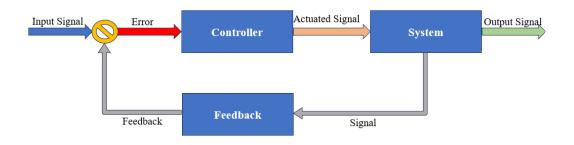


Fig 5.2 Closed-loop control system

# 2. Linear and non-linear Control Systems

### **Linear Control Systems:**

A linear system is defined as a system in which variables have an exponent one for example y = 3 \*x

### **Non- Linear Control Systems**

A non-linear system is defined as a system in which variables have an exponent other than one for example  $x^2 + y^2 = 6$ 

# 3. Time variant and Time in variant Control systems

#### Time variant control system:

Parameters of the control system vary with time and can be defined as the timevariant control system

### Time In-variant control system:

The Parameters of the control system do not vary with time and can be defined as a time-invariant control system.

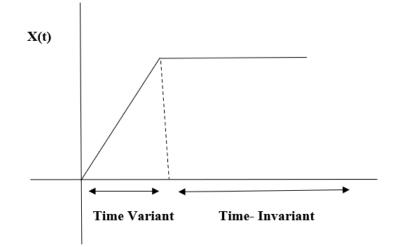


Fig 5.3 Time-Variant Vs Time- Invariant

# 4. Linear Time Variant and Non-linear Time Variant control system Linear Time Variant control system:

The combination of linear systems with time-variant are the systems in which variables have an exponent of one and are time dependent.

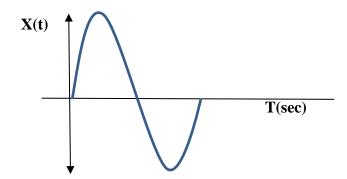


Fig 5.4 Linear Time Variant control system

# Non-Linear Time Variant control system:

The combination of non-linear systems with time-variant are the systems in which variables have an exponent other than one and are time-dependent.



T(sec)

Fig 5.5 Non-Linear Time Variant control system

## 5. SISO and MIMO Control system

Single Input Single Output (SISO): The control system consists of one Input and one output for example speed controller of the fan.

Multiple Input Multiple Output (MIMO): The control system consists of multiple Input and multiple output parameters for example aircraft controller design, and auto-controller of the space vehicle.

To design an accurate control system for our research objective closed-loop, linear, time-invariant, SISO control system is elaborately discussed in sections 1,2,3,4 and 5

# 5.2 AIRCRAFT STABILITY AND CONTROL SYSTEM

# 5.2.1 AIRCRAFT STABILITY

Stability is the characteristic of the equilibrium state being stable. In physical terms, the net moment and resultant forces about the centre of gravity must be zero to satisfy stability conditions.

It is classified as static stability and dynamic stability

**Static:** Stability is the ability of a system to resume equilibrium even after being moved from its initial state. An example to discuss types of static stability is illustrated in the below section

# **Positive Static Stability**

If the system is displaced from its initial state and restored to its original state such that forces and moments tend the system to attain an equilibrium point is referred to as a stable system as seen in Fig 5.6

#### **Negative Static Stability**

If the system is displaced from its initial state and tries to go away from its original state such that forces and moments tend the system to move away from the equilibrium point is referred to as an unstable system

#### **Neutral Static Stability**

The equilibrium point of the system is independent of displacing from the original state and is referred to as a neutrally stable system.



(i) Stable System (ii) Unstable System (iii) Neutral System

Fig 5.6 Stable, Unstable, and Neutral System

**Dynamic:** The response and behaviour of the motion of the system while displaced from its original state is termed dynamic stability.

#### **Positive Dynamic Stability**

If the system is displaced from its initial state and oscillations dampen the system towards the equilibrium point is termed a dynamically stable system

#### **Negative Dynamic Stability**

If the system is displaced from the initial state and amplitude of the oscillations rises and the system has negative damping then the system will never approach towards trim state thus referred to as a dynamically Unstable system

#### **Neutral Dynamic Stability**

If the system is displaced from its initial state and the amplitude of the oscillations never damps or remains constant termed a neutrally dynamically stable system

# **5.2.2 AIRCRAFT CONTROLS**

# Elevator:

The control surfaces are hinged to the trailing edge of the horizontal tail. These are found in pairs and provide longitudinal stability to an aircraft mentioned in Fig 5.7 Pitch control is attained by changing the aircraft lift by deflecting the flapped portion of the horizontal tail entitled as the elevator.

### Ailerons:

The control surfaces are hinged to the trailing edge of an aircraft wing tip. These are found in pairs and provide lateral stability to an aircraft. They are performed in a synchronized manner as one aileron is raised and the other is lowered known as the aircraft's rolling motion.

### Rudder:

The control surfaces are hinged to the trailing edge of the vertical tail and provide directional stability to an aircraft. Yaw control is attained by deflecting the flapped portion of the vertical tail termed as rudder. It turns the aircraft in the left and right direction similar to the rudder of a boat.



Fig 5.7 Aircraft Controls

# 5.2.3 AIRCRAFT AXES AND REFERENCE SYSTEM

Aircraft controls can be acknowledged by defining an axes coordinate system as the aircraft is free to rotate about 3 axes which are mutually perpendicular to each other as mentioned in Fig 5.8 and the pilot can handle and control the motion about axes in all directions hence the axes system is defined as

# Longitudinal Axis:

Lateral stability about longitudinal axes is a key feature of these axes. Ailerons are lateral control that provides rolling motion to an aircraft that moves one wing down and the other wing up.

# Lateral Axis:

Longitudinal stability about lateral axes is a key feature of these axes. Elevators are longitudinal control that provides pitching motion to an aircraft that moves the aircraft nose in an up-and-down direction.

# Vertical Axis:

Directional stability about vertical axes is a key feature of these axes. Rudders are directional control that provides Yawing motion to an aircraft which moves the aircraft to the left and right.



Fig 5.8 Stability Axes System

# **5.2.4 REFERENCE FRAMES**

Inertial Axes: A frame of reference that is having constant velocity or remains stationary. All of Newton's laws are applied in this frame of reference.

Earth Axes: A frame of reference in which the origin is located on the earth's surface.  $X_E$  points towards the geographical north,  $Y_E$  points towards the geographical east, and  $Z_E$  points towards the centre of the earth.

Body Axes: A frame of reference in which the origin is located on the aircraft's centre of gravity, with the X pointing towards the aircraft nose and the Y axes pointing towards the right wing and the Z axis passing beneath through it.

Wind Axes: A frame of reference in which the origin is situated on the aircraft's centre of gravity, with X  $_{\rm w}$  axes pointing forward relative to the velocity vector, Y  $_{\rm w}$  axes pointing towards the right wing, and Z axes underneath through it.

Stability Axes: This axes system is defined for aircraft stability and fixed with aircraft. X-axes point forward toward the flow direction. Y-axes point towards the right wing, and Z-axes underneath through it.

Based on the Axes control system, Aircraft stability is classified into three types as

- 1. Longitudinal Stability
- 2. Lateral Stability
- 3. Directional Stability

# 5.2.5 LONGITUDINAL STABILITY

The synonym term "pitch stability" is the tendency of an aircraft to attain a trim state about the lateral axis. Longitudinal Stability provides pitching motion by moving the aircraft nose in upward and downward directions. Elevators are control surfaces that contribute longitudinal motion of an aircraft.

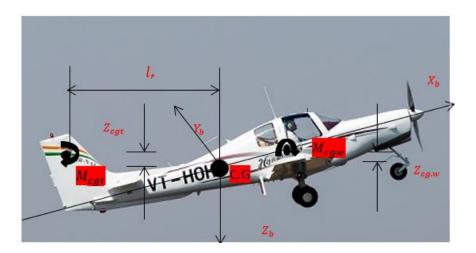


Fig 5.9 Wing and tail Contribution of Hansa-III Aircraft

Geometrical Parameters	Value	Geometrical Parameters	Value	
Wi	ng	Horizontal Tail		
Planform area (S)	$12.47(m^2)$	Planform area $(S_t)$	2.04(m <sup>2</sup> )	
Aspect ratio (A)	8.8	Aspect ratio (A)	6.35	
MAC ( <i>c</i> )	1.21(m)	MAC ( <i>c</i> )	0.59(m)	
Root Chord $(c_r)$	1.3(m)	Root Chord ( $c_r$ )	0.78(m)	
Tip Chord ( $c_t$ )	0.8	Tip Chord ( $c_t$ )	0.354(m)	
Taper ratio $(\Lambda)$	6(deg)	Taper ratio $(\Lambda)$	0.454	
Airc	raft	Aerodynamic Derivatives		
Aircraft span (b)	10.47(m)	$(C_{L_{\alpha},w})_{ss}$	4.5	
Mass (m)	750(kg)	$(C_{L_{\alpha_t}})_{ss}$	1.48	
Velocity (V)	36(m/s)	$(C_{m_{\alpha,f}})_{ss}$	0.3	
Moment of Inertia (I <sub>Y</sub> )	907(kg-m <sup>2</sup> )	$(C_{L\alpha_t} \frac{d\epsilon}{d\alpha})_{ss}$	0.22	
Moment arm $(l_t)$	3.624(m)			
Density (p)	$0.96(kg/m^3)$			
Moment of Inertia (I <sub>X</sub> )	925(kg-m <sup>2</sup> )			

Table 5.1 Geometrical and Aerodynamic Parameters (R. Kumar, 2012)

# Analytical Calculation to estimate Longitudinal Stability

The pitch stiffness  $C_{m_{\alpha}}$  is the deciding factor in to state longitudinal stability of the system which is estimated by referring to fig 5.9 and Table 5.1

The permissible range of C.G: Forward C.G position is 21.94% of MAC and aft C.G Position is 27.47% of MAC as MAC of the wing is 1.21m (NAL, 2000)

Forward C.G position= 0.26

#### Aft C.G Position= 0.332

C.G = (0.26 + 0.332)/2 = 0.296

The Aerodynamic centre lies at the quarter chord point for a symmetrical airfoil as MAC is 1.21 m hence  $X_{ac} = 0.3025$ 

$$V_H = \frac{l_t \times S_t}{S \times \bar{C}} = \frac{3.624 \times 2.04}{12.47 \times 1.21} = 0.489$$

$$\eta = \frac{Q_t}{Q_w} < 1$$
 (Assume tail efficiency factor as unity)

The wing's pitching moment coefficient

$$C_{m_{\alpha,w}} = C_{L_{\alpha},w} (X_{cg} - X_{ac}) / \text{MAC}$$

$$= 4.5(0.296 - 0.3025)/1.21 = -0.207$$

The coefficient of the horizontal tail's pitching moment

$$C_{m_{\alpha,t}} = -C_{L_{\alpha_t}} \eta V_H (1 - \frac{d\epsilon}{d\alpha})$$
  
= -1.48\*1\*0.489+ 0.489\*0.22= -0.6155

The coefficient of the fuselage pitching moment

$$C_{m_{\alpha,f}} = 0.3$$

By combining the contributions from the airplane's wings, fuselage, and tail, the total pitching moment may be calculated as (Nelson, 1998)

$$C_{m_{\alpha}} = C_{L_{\alpha},w}(X_{cg} - X_{ac}) / MAC + C_{m_{\alpha,f}} - C_{L_{\alpha_t}} \eta V_H (1 - \frac{d \epsilon}{d\alpha})$$
  
= 4.5(0.296-0.3025)/1.21 + 0.3 +0.22\*0.489- 1.48\*1\*0.489 = -0.345

The contributing factor determining aircraft static stability is  $C_{m_{\alpha}} < 0$  to attain longitudinal stability.

The Stick-Fixed neutral point(Nelson, 1998)

$$\bar{X}_{np} = X_{ac} - C_{m_{\alpha,f}} / C_{L_{\alpha,W}} + C_{L_{\alpha_t}} \eta V_H (1 - \frac{d\epsilon}{d\alpha})$$
$$= 0.3025 + 0.089 = 0.3915$$

Stick-fixed Static Margin =  $\bar{X}_{np} - \bar{X}_{cg} = 0.3915 - 0.296 = 0.095$ 

The Positive value of the Static Margin illustrates that the system is longitudinally statically stable thus control system can be designed to attain the research objective

#### Longitudinal modes of motion:

Frederick W. Lanchester, Aerodonetics, develops the fundamental concept of longitudinal dynamic stability(Nelson, 1989).In the early stages of his study, Lanchester noticed the motions of a glider during flying. He conducted various experiments with gliders and discovered that all flying machines possess oscillatory motions while disturbed from the original equilibrium state. Two oscillatory modes are long-period and short-period.

#### Long Period mode

This oscillatory mode is lightly damped and its motion occurs at a constant angle of attack. As its name, this mode has a long period also termed phugoid

#### **Short Period mode**

This oscillatory mode is heavily damped and its motion occurs at a constant speed. As its name, this mode has a short period.

Longitudinal Dynamics is characterised by damping ratio & frequency of short period and long period. Before deducing the expression of longitudinal modes, the equation of motion must be linearized by applying the small disturbance theory as explained below.

#### Linearized Perturbation equation using small-disturbance theory

This theory solves complex engineering application-based problems by linearizing force and moment equations to reduce system complexity. This theory applies to steady-state flight conditions and is inapplicable for stalled flights. It is assumed

that all state variables are replaced with a summation of steady-state value and perturbation.

$u = u_0 + \Delta u$	$X = X_0 + \Delta X$
$v = v_0 + \Delta v$	$Y = Y_0 + \Delta Y$
$w = w_0 + \Delta w$	$Z = Z_0 + \Delta Z$
$p = p_0 + \Delta p$	$L = L_0 + \Delta L$
$q = q_0 + \Delta q$	$M = M_0 + \Delta M$
$r = r_0 + \Delta r$	$N = N_0 + \Delta N$
$\delta = \delta_0 + \Delta \delta$	

Assumptions:

1. It is assumed that X- axes lie along the aeroplane velocity vector.

2. Considering reference conditions as symmetric.

3. It is assumed that forces in the force equation include propulsive force and thrust force is assumed to be constant. Thrust force is produced due to the propulsion system of an aircraft and creates a moment if not lies through the airplane's Centre of gravity assumed to be constant.

X-axes force equation can be rewritten as;

$$X_0 + \Delta X - mgSin(\theta_0 + \Delta \theta) = m\left[\frac{d}{dt}(u_0 + \Delta u) + (q_0 + \Delta q)(w_0 + 5.1)\right]$$

$$\Delta w) - (r_0 + \Delta r)(v_0 + \Delta v)]$$

Assuming  $w_0 = v_0 = q_0 = r_0 = p_0 = \phi_0$  for X axes, the equation reduces to

$$X_0 + \Delta X - mgSin(\theta_0 + \Delta \theta) = m\Delta \dot{u}$$
 5.2

As per trigonometric identity;  $Sin(\theta_0 + \Delta \theta) = Sin\theta_0 Cos\Delta\theta + Cos\theta_0 Sin\Delta\theta$ 

For Smaller angles  $Sin\Delta\theta = \Delta\theta$ ;  $Cos\Delta\theta = 1$ 

Substituting all trigonometric relations in the above equation to obtain force equation in reduced form  $Sin(\theta_0 + \Delta \theta) = Sin\theta_0 + \Delta \theta Cos\theta_0$ 

Thus,  $X_0 + \Delta X - mg(Sin\theta_0 + \Delta\theta Cos\theta_0) = m\Delta \dot{u}$ 

If perturbations are set equal to zero; then reference steady-state conditions are depicted as  $X_0 - mgSin\theta_0 = 0$ 

Finalized X force equation can be written as:  $\Delta X - mg(Sin\theta_0 + \Delta\theta Cos\theta_0) = m\Delta \dot{u}$ 

 $\Delta X$  as  $\Delta$  in resultant forces in X-direction and if X is a function of  $u, w, \delta_e, \delta_T$  then  $\Delta X$  is represented as  $\Delta X = \frac{\partial X}{\partial u} \Delta u + \frac{\partial X}{\partial w} \Delta w + \frac{\partial X}{\partial \delta_e} \Delta \delta_e + \frac{\partial X}{\partial \delta_T} \Delta \delta_T$ 

 $\frac{\partial x}{\partial u}, \frac{\partial x}{\partial w}$  terms are known as stability derivatives  $\frac{\partial x}{\partial \delta_e}, \frac{\partial x}{\partial \delta_T}$  as Control derivatives where  $\delta_e$  is elevator input, and  $\delta_T$  is throttle input.

Substituting the value of  $\Delta X$  relation from the above equation to obtain the equation as

$$\frac{\partial X}{\partial u}\Delta u + \frac{\partial X}{\partial w}\Delta w + \frac{\partial X}{\partial \delta_e}\Delta \delta_e + \frac{\partial X}{\partial \delta_T}\Delta \delta_T - mg\,\Delta\theta Cos\theta_0 = m\Delta \dot{u} \qquad 5.3$$

Now re-arranging above equation to deduce the X direction force equation as

$$(m\frac{d}{dt} - \frac{\partial X}{\partial u})\Delta u - (\frac{\partial X}{\partial w})\Delta w + (mg \ Cos\theta_0)\Delta\theta = \frac{\partial X}{\partial \delta_e}\Delta\delta_e + \frac{\partial X}{\partial \delta_T}\Delta\delta_T \qquad 5.4$$

Dividing the above equation by 'm' to get a simplified expression as  $(\frac{d}{dt} - \frac{\partial X}{\partial u})\Delta u - (\frac{\partial X}{\partial w})\Delta w + (g \cos \theta_0)\Delta \theta = \frac{\partial X}{\partial \delta_e}\Delta \delta_e + \frac{\partial X}{\partial \delta_T}\Delta \delta_T$  where  $X_u, X_w$  are aerodynamic derivatives.

The set of linearized perturbation equations of motion in the X direction is expressed as:

$$\left(\frac{d}{dt} - X_u\right)\Delta u - X_w\Delta w + (g \cos\theta_0)\Delta\theta_0 = X_{\delta_e}\Delta\delta_e + X_{\delta_T}\Delta\delta_T$$
5.5

Linearized Longitudinal perturbation force and moment equation can be expressed as (Nelson, 1989):

$$(\frac{d}{dt} - X_u) \Delta u - X_w \Delta w + (g \cos \theta_0) \Delta \theta_0 = X_{\delta_e} \Delta \delta_e + X_{\delta_T} \Delta \delta_T$$

$$-Z_u \Delta u + [(1 - Z_w)) \frac{d}{dt} - Z_w] \Delta w - [(u_0 + Z_q)) \frac{d}{dt} - (g \sin \theta_0)] \Delta \theta =$$

$$5.7$$

$$Z_{\delta_e} \Delta \delta_e + Z_{\delta_T} \Delta \delta_T$$

$$-M_u \Delta u - (M_w \frac{d}{dt} + M_w] \Delta w + (\frac{d^2}{dt^2} - M_q \frac{d}{dt}) \Delta \theta = M_{\delta_e} \Delta \delta_e +$$

$$5.8$$

$$M_{\delta_T} \Delta \delta_T$$

$$Z_{\dot{w}} = -C_{z\dot{\alpha}} \frac{c}{2u_0} \frac{QS}{u_0 m}$$

$$5.9$$

$$Z_u = -C_{zq} \frac{c}{2u_0} \frac{QS}{m}$$
5.10

 $C_{z\dot{\alpha}}$ ,  $C_{zq}$  is Z force non-dimensional components contribute pitching motion very little so neglected  $Z_q$  and  $Z_{\dot{w}}$  effects hence rewriting sets of longitudinal equations in statespace form

Where x is a state vector, A as a state matrix, u refers to the control vector and B is the control matrix. Comparing state-space form with generalized state-space equation yields

$$\begin{bmatrix} \Delta \dot{u} \\ \Delta \dot{w} \\ \Delta \dot{q} \\ \Delta \dot{\theta} \end{bmatrix} = \begin{bmatrix} X_u & X_w & 0 & -g \\ Z_u & Z_w & u_0 & 0 \\ M_u + M_{w\dot{Z}_u} & M_w + M_{\dot{w}}Z_w & M_q + M_{\dot{w}}u_0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \Delta u \\ \Delta w \\ \Delta q \\ \Delta \theta \end{bmatrix} +$$

$$\begin{bmatrix} X_{\delta_e} & X_{\delta_T} \\ Z_{\delta_e} & Z_{\delta_T} \\ M_{\delta_e} + M_{\dot{w}} Z_{\delta_e} & M_{\delta_T} + M_{\dot{w}} Z_{\delta_T} \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta \delta_e \\ \Delta \delta_T \end{bmatrix}$$
5.11

 $\dot{X} = Ax + Bu$ 

### **Long-Period Approximation**

Approximating longitudinal state-space equation to the long-period mode by assuming  $\Delta \alpha$  as zero and neglecting pitching moment equation to deduce expression of long-period mode.

The characteristics of long-period mode are changes in altitude, pitch altitude, and motion occurring at constant " $\alpha$ "

$$\Delta \alpha = \frac{\Delta w}{u_0}, \ \Delta \alpha = 0$$
 signifies  $\Delta w = 0$ 

The simplified state equation is reduced by applying assumptions such as (Nelson, 1998):

$$\begin{bmatrix} \Delta \dot{\boldsymbol{u}} \\ \Delta \dot{\boldsymbol{\theta}} \end{bmatrix} = \begin{bmatrix} \boldsymbol{X}_{\boldsymbol{u}\pm} & -g \\ \frac{-\boldsymbol{Z}_{\boldsymbol{u}}}{\boldsymbol{u}_{\boldsymbol{0}}} & 0 \end{bmatrix} \begin{bmatrix} \Delta \boldsymbol{u} \\ \Delta \boldsymbol{\theta} \end{bmatrix}$$
 5.12

The eigenvalues of matrix A can be solved by  $|\lambda I - A| = 0$ 

$$\lambda^2 - X_u \lambda - \frac{Z_u g}{u_0} = 0 \tag{5.13}$$

$$\lambda_{lp} = [X_u \pm \sqrt{X_u^2} + 4\frac{z_{ug}}{u_0}]/2$$
5.14

The physical systems are modelled by the second-order differential equation. To illustrate aircraft dynamic motion let us consider the mechanical system comprised

of mass, spring, and damper system. The non-homogeneous second-order differential equation of the physical system can be explained as:

$$m\frac{d^{2}x}{dt^{2}} + c\frac{dx}{dt} + kx = F(t); \frac{d^{2}x}{dt^{2}} + \frac{c}{m}\frac{dx}{dt} + \frac{k}{m}x = \frac{F(t)}{m}$$
 5.15

*m*Where F(t) is the forced force function. If the driving force is zero, then the system response is termed a free response and vice versa referred to as a forced response. The differential equation's solution can be expressed in writing by substituting as  $x = Ae^{\lambda t}$  in the above equation

$$\lambda^2 A e^{\lambda t} + \frac{c}{m} \lambda A e^{\lambda t} + \frac{k}{m} A e^{\lambda t} = 0 \text{ or } \lambda^2 + \frac{c}{m} \lambda + \frac{k}{m} = 0 \text{ or } \lambda^2 + 2\xi \omega_n \lambda + \omega_n^2 = 0$$

The above phrase refers to the roots of the characteristic equation as

$$\lambda_{1,2} = -\frac{c}{2m} \pm \sqrt{(\frac{c}{2m})^2} - \frac{k}{m}$$

Comparing the above equation with characteristic equation of long-period mode yields a damping factor and natural frequency as

$$\omega_{nlp} = \sqrt{-\frac{Z_u g}{u_0}}$$

$$\xi_{lp} = -\frac{X_u}{2\omega_{nlp}}$$
5.16
5.17

# **Short-period Approximation**

Short-period motion is heavily damped and characterized by assuming  $\Delta u = 0$  and leaving the X-force equation. The change in AOA and the motion that continues for several seconds at a constant speed are the hallmarks of short-period mode.

The simplified state equation is reduced by applying assumptions such as(Nelson, 1998):

$$\begin{bmatrix} \Delta \dot{w} \\ \Delta \dot{q} \end{bmatrix} = \begin{bmatrix} Z_w & u_0 \\ M_w + M_{\dot{w}} Z_w & M_q + M_{\dot{w}} u_0 \end{bmatrix} \begin{bmatrix} \Delta w \\ \Delta q \end{bmatrix}$$
5.18

In terms of AOA using the expression,  $\Delta \alpha = \frac{\Delta w}{u_0}$  the equation can be rewritten as

$$\begin{bmatrix} \Delta \dot{\alpha} \\ \Delta \dot{q} \end{bmatrix} = \begin{bmatrix} \frac{Z_{\alpha}}{u_0} & 1 \\ M_{\alpha} + M_{\dot{\alpha}} \frac{Z_{\alpha}}{u_0} & M_q + M_{\dot{\alpha}} \end{bmatrix} \begin{bmatrix} \Delta \alpha \\ \Delta q \end{bmatrix}$$
 5.19

The eigenvalues of the above state equation are estimated by using the expression  $|\lambda I - A| = 0$ 

The characteristic equation of the above expression can be written as

$$\lambda^2 - \left(M_q + M_{\dot{\alpha}} + \frac{Z_{\alpha}}{u_0}\right)\lambda + M_q \frac{Z_{\alpha}}{u_0} - M_{\alpha} = 0$$
5.20

The roots of the above characteristic equation are:

$$\lambda_{sp} = \left[ \left( M_q + M_{\dot{\alpha}} + \frac{Z_{\alpha}}{u_0} \right) \pm \left[ \left( M_q + M_{\dot{\alpha}} + \frac{Z_{\alpha}}{u_0} \right)^2 - 4 \left( M_q \frac{Z_{\alpha}}{u_0} - M_{\alpha} \right) \right]^{\frac{1}{2}} \right] / 2 \quad 5.21$$

The characteristic equation and the above equation being compared of short-period mode yields a damping factor and natural frequency as(Nelson, 1998)

$$\omega_{nsp} = \left[ \left( M_q \frac{Z_\alpha}{u_0} - M_\alpha \right) \right]^{1/2}$$
5.22

$$\xi_{sp} = -\left[M_q + M_{\dot{\alpha}} + \frac{Z_a}{u_0}\right] / (2\omega_{nsp})$$
5.23

The flight control designer handles the flying quality of aeroplane by estimating short- and long-period damping and frequency of Hansa-III by referring to Table 5

$$V_H = \frac{l_t \times S_t}{S \times \overline{C}} = \frac{3.624 \times 2.04}{12.47 \times 1.21} = 0.489$$
  
$$\eta = \frac{Q_t}{Q_w} < 1 \text{ (Assume tail efficiency factor as unity)}$$
  
$$C_{m_{\dot{\alpha}}} = -2C_{L\alpha_t} \eta V_H \frac{l_t}{\overline{c}} \frac{d\epsilon}{d\alpha} = \frac{-0.7797}{1.21} = -0.644$$

$$M_{\alpha} = u_{0}C_{m_{\alpha}}\frac{QS\bar{c}}{u_{0}l_{yy}} = -4.379/s \quad u_{0} = 36.244 \text{m/s}; C_{m_{\alpha}} = -0.4259$$

$$M_{q} = C_{m_{q}}\frac{\bar{c}}{2u_{o}}\frac{QS\bar{c}}{l_{yy}} = \frac{-144.47}{72.48} = -1.99/s$$

$$M_{\dot{\alpha}} = C_{m_{\dot{\alpha}}}\frac{QS\bar{c}}{l_{yy}}\frac{\bar{c}}{2u_{o}} = -0.1105/s$$

$$C_{Z_{\alpha}} = -\left[(C_{L_{\alpha}} + C_{D_{0}})\right] = -6.4908$$

$$Z_{\alpha} = C_{Z_{\alpha}}\frac{QS}{m} = -68.040$$

Estimating un-damped natural frequency and damping ratio of Short-period and long-period mode by substituting values of non-dimensional stability and control derivatives from the above equations

# **Short-period Approximations**

$$w_{n_{sp}} = \sqrt{\frac{Z_{\alpha}M_q}{u_0} - M_{\alpha}} = \sqrt{\frac{(-68.040 \times -1.99)}{36.244} - (-4.379)} = \sqrt{\frac{135.399}{36.244}} = 2.84 \text{ rad/s}$$
$$f_{n_{sp}} = \frac{2.84}{6.28} = 0.45/\text{s}$$
$$\xi_{sp} = -\frac{\left(M_q + M_{\dot{\alpha}} + \frac{Z_{\alpha}}{u_0}\right)}{2w_{n_{sp}}} = \frac{3.9975}{5.68} = 0.70$$

# **Long-period Approximations**

$$w_{n_p} = \sqrt{\frac{-Z_{ug}}{u_0}}$$
  

$$\xi_p = \frac{-X_u}{2w_{n_p}}$$
  

$$X_u = \frac{-[C_{D_u} + 2C_{D_0}]QS}{mu_0} = \frac{[-3C_{D_0}]QS}{mu_0} = \frac{0.1224 \times 630.47 \times 12.47}{27,183} = -0.0354/s \quad C_{D_u}$$
 is neglected at low flight speed; subsonic a/c

$$Z_{u} = \frac{C_{Z_{u}}QS}{mu_{0}} = \frac{\left[\left\{\frac{-M^{2}}{1-M^{2}}\right\}C_{L_{0}} - 2C_{L_{0}}\right]QS}{mu_{0}} = \frac{\left[-2C_{L_{0}}\right]QS}{mu_{0}} = \frac{-0.458 \times 630.47 \times 12.47}{27,183} = -0.1303/s \quad ;$$
Musch is neglected at subsonic flight

Mach is neglected at subsonic flight

$$w_{n_p} = \sqrt{\frac{-Z_u g}{u_0}} = \sqrt{\frac{1.2782}{36.244}} = 0.1877 \text{rad/s}$$

$$\xi_p = \frac{-X_u}{2w_{n_p}} = \frac{-(-0.0354)}{2 \times 0.1877} = 0.0942$$
$$\lambda_{1,2} = -\xi_p w_{n_p} \pm i w_{n_p} \sqrt{1 - \xi_p^2}$$

 $\lambda_{1,2} = -0.0176 \pm i0.186$ 

Non- dimensional	Value	Non- dimensional	Value
Derivative		Derivative	
$M_{\alpha}$ (s <sup>-2</sup> )	-4.379	$X_{u}$ (s <sup>-1</sup> )	-0.0354
$M_q$ (s <sup>-1</sup> )	-1.99	$Z_u$ (s <sup>-1</sup> )	-0.1303
$M_{\dot{\alpha}}$ (s <sup>-1</sup> )	-0.1105	$C_{m_{\dot{lpha}}}$	-0.644
ξ <sub>p</sub>	0.0942	$W_{n_p}$ (rad/s)	0.1877
ξ <sub>sp</sub>	0.70	$W_{n_{sp}}$ (rad/s)	0.45

Table 5.2: Estimation of Non-dimensional derivatives using Analytical Method

Non-dimensional Derivatives of different elevator control Inputs Multistep, doublet, and Pulse estimated using the Maximum likelihood algorithm and results were validated with analytical calculations derived in the above section as discussed in Table 5.3

-		Cmα	Cmq	CL0	Cd0	CLα	Μα	Mq	Ζα	Madot	Xu	Zu	ωsp	D.R sp
Signals														
M1	0.08	-0.41	-8.57	0.04	0.06	5.96	-4.19	-1.46	-63.13	-0.11	-0.05	-0.02	2.59	0.64
M2	0.08	-0.43	-8.11	0.08	0.05	5.69	-4.41	-1.38	-60.19	-0.11	-0.05	-0.05	2.59	0.61
M3	0.07	-0.35	11.10	-0.18	0.06	3.94	-3.60	1.89	-41.91	-0.11	-0.05	0.10	1.19	-0.26
M4	0.09	-0.64	-6.77	0.11	0.15	6.16	-6.62	-1.16	-66.08	-0.11	-0.13	-0.07	2.95	0.52
M5	0.08	-0.43	-11.61	0.23	0.04	6.46	-4.38	-1.98	-68.13	-0.11	-0.04	-0.13	2.85	0.70
D1	0.18	-0.51	-6.67	-0.44	0.22	3.75	-5.24	-1.14	-41.59	-0.11	-0.19	0.25	2.56	0.47
P1	0.10	-0.33	-8.67	-0.61	0.16	5.78	-3.39	-1.48	-62.30	-0.11	-0.14	0.35	2.44	0.68
P2	0.03	-0.27	-10.00	0.55	0.08	3.65	-2.78	-1.71	-39.13	-0.11	-0.07	-0.32	2.15	0.67

Table 5.3: Estimation of short-Period Damping ratio and frequency

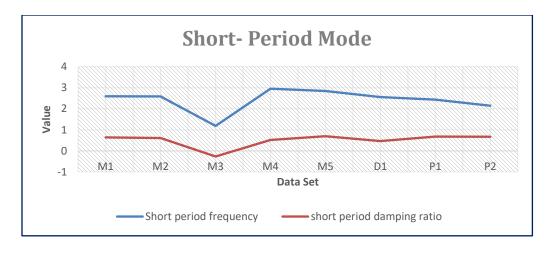


Fig 5.10 Short-period Frequency and Damping ratio

The short period frequency and damping ratio of different elevator inputs M1, M2, M3, M4, M5, D1, P1, and P2 is reflected in figure 5.10 and table 5.3 for assessment of flying handling quality. As the dynamic quality of the aircraft is closely related to its ability to fly, it is a difficult task for a flight control designer to create a controller with good dynamic properties (JAISWAL & PRAKASH, 2022) [ref]. When investigating pilot handling, the damping and frequency of both short- and long-term periods are crucial.

#### Lateral Stability

Aircraft Lateral stability also referred to as 'roll stability' is the tendency of an aircraft to attain a trim state about the longitudinal axis. Lateral Stability provides rolling motion by moving aircraft in forward and rearward directions. Ailerons are control surfaces that contribute lateral motion of an aircraft.

#### **Directional Stability**

The synonym term 'Yaw stability' is the tendency of an aircraft to attain a trim state about the normal axis. Directional Stability provides yawing motion by moving aircraft in the left and right directions. Rudders are control surfaces that contribute directional motion of an aircraft.

#### Lateral- Directional modes of motion:

#### **Spiral divergence**

It is a phenomenon that occurs when an aircraft is directionally stable but laterally unstable. This instability produces spiralling motion have characteristics of slowly convergent and divergent states. This spiral is sometimes difficult to handle if preventive measures are not taken at the right time by the pilot.

#### **Dutch-roll mode**

It is a coupled phenomenon of lateral-directional motion that combines the characteristics of rolling, yawing, and side-slipping. The lightly damped oscillations have low frequency with a period of 3-15sec. Iceskater is the perfect example to resemble its features.

#### **Rolling mode**

Directional divergence is a synonym for roll mode. This motion has characteristics of high convergence with low frequency. An ever-increasing sideslip angle should be avoided if disturbed from equilibrium. This instability mode is avoided by designing a proper vertical tail surface.

#### **5.3 LONGITUDINAL EQUATION IN WIND AXIS**

Derivation to establish state-space linearized longitudinal perturbation equation to estimate the aircraft transfer function(Klien & Morelli, 2006) (Jaiswal et al., 2020)

Aircraft sensors like pitot tube measure airspeed V rather than body-axes velocities u, v, and w. In the same manner, sensors attached in aircraft measure the angle of attack, and sideslip angle thus it is identified that non-dimensional aerodynamic coefficients are characterized as  $\alpha$ ,  $\beta$ , V having a relationship as:

$$\alpha = \tan^{-1} \frac{w}{u}$$
 5.24

$$\beta = \sin^{-1} \frac{v}{v}$$
 5.25

Where airspeed is denoted as  $V = \sqrt{u^2 + v^2 + w^2}$ 

$$v = V \sin \beta \tag{5.26}$$

$$w = V \sin \alpha \cos \beta$$
 5.27



Fig 5.11 Estimation of Variables $\alpha$ ,  $\beta$ , V from Wind-axis

Referring to the figure 5.11 in terms of  $\alpha$ ,  $\beta$ , V as

 $u = V \cos \alpha \cos \beta$  5.28

Differentiating equation, a and b to get a simplified equation as(Klien & Morelli, 2006):

$$\dot{V} = \frac{1}{V}(uu + v\dot{v} + w\dot{w})$$
5.29

$$\dot{\alpha} = \left(\frac{\dot{u}\dot{w} - w\dot{u}}{u^2 + w^2}\right)$$
 5.30

$$\dot{\beta} = \frac{(u^2 + w^2)\dot{v} - v(u\dot{u} + w\dot{w})}{V^2\sqrt{u^2 + w^2}}$$
5.31

Rewriting longitudinal force equation in wind axes by substituting values of  $\dot{u}, \dot{v}, \dot{w}$  from Appendix C 5.55- 5.57 and u, v, w from the above equations into above 5.29-5.31 to get expression in terms of  $\alpha, \beta, V$ 

$$\dot{V} = -\left\{\frac{\bar{q}.s}{m}\right\} C_D + g\left(\cos\phi\cos\theta\sin\alpha\cos\beta + \sin\phi\cos\theta\sin\beta - 5.32\right)$$

5.33

 $sin\theta \cos\alpha \cos\beta + \left\{\frac{T}{m}\right\} \cos\alpha \cos\beta$  $\dot{\alpha} = -\left\{\frac{\bar{q}\cdot s}{m\cdot V\cos\beta}\right\} C_L + q + \frac{g}{V\cos\beta} (\cos\phi\cos\theta\cos\alpha + \sin\theta\sin\alpha) - \left\{\frac{T}{m\cdot V\cos\beta}\right\} \sin\alpha - \tan\beta (p\cos\alpha + r\sin\alpha)$ 

Assuming  $\beta = \phi = 0$  for longitudinal motion and using trigonometric identities Sin(A-B), and Cos(A-B) as:

Force Equation(Klien & Morelli, 2006)

$$\dot{V} = -\left\{\frac{\bar{q}.s}{m}\right\} C_D + g \sin(\alpha - \theta) + \left\{\frac{T}{m}\right\} \cos\alpha \qquad 5.34$$

$$\dot{\alpha} = -\left\{\frac{\bar{q}.s}{m.v}\right\} C_L + q + \frac{g}{v} \cos(\alpha - \theta) - \left\{\frac{T}{m.v}\right\} \sin \alpha$$
 5.35

$$\dot{\theta} = q \tag{5.36}$$

Moment Equation(Klien & Morelli, 2006)

$$\dot{q} = \left(\frac{\bar{q}.s.c}{l_y}\right).C_m + \left\{\frac{T}{l_{YY}}\right\}l_{tz}$$
5.37

To analyse the aircraft dynamics, the aircraft is modelled in terms of mathematical equations as aerodynamic stability and control derivatives shown below(Nelson, 1998)

$$C_{L} = \{ C_{L_{0}} + C_{L_{\alpha}} \cdot \alpha + C_{L_{q}} \cdot \frac{q\bar{c}}{2U_{1}} + C_{L_{\delta_{e}}} \cdot \delta_{e} \}$$
5.38

$$C_D = \left\{ C_{D_0} + C_{D_\alpha} \cdot \alpha + C_{D_q} \cdot \frac{q\bar{c}}{2U_1} + C_{D_{\delta_e}} \cdot \delta_e \right\}$$
5.39

$$C_m = \left\{ C_{m_0} + C_{m_\alpha} \cdot \alpha + C_{m_q} \cdot \frac{q\bar{c}}{2U_1} + C_{m_{\delta_e}} \cdot \delta_e \right\}$$
5.40

Assumption: thrust setting angle = 0, Flight path  $\gamma$  = constant at cruise state, flight velocity = constant for short period mode

$$\dot{\alpha} = -\left\{\frac{\bar{q}.s}{m.v}\right\}C_L + q \tag{5.41}$$

$$\dot{\theta} = q \tag{5.42}$$

$$\dot{q} = \left(\frac{\bar{q}.s.c}{I_y}\right).C_m$$
5.43

Simplifying set of equations

$$\dot{\alpha} = q - \frac{\rho V S_w}{2m} \{ C_{L_0} + C_{L_{\alpha}} \cdot \alpha + C_{L_q} \cdot \frac{q\bar{c}}{2U_1} + C_{L_{\delta_e}} \cdot \delta_e \}$$
5.44

$$\dot{\theta} = q \tag{5.45}$$

$$\dot{q} = \frac{\rho V^2 S_w \bar{c}}{2Iy} \{ C_{m_0} + C_{m_\alpha} \cdot \alpha + C_{m_q} \cdot \frac{q\bar{c}}{2U_1} + C_{m_{\delta_e}} \cdot \delta_e \}$$
5.46

Substituting values of  $S_w$  ,  $\overline{c}$  , V ,  $\rho$  ,  $I_y$  & m from Table 5

$$\dot{\alpha} = q - \frac{0.96 X 36 X 12.47}{2 X 750} \left[ C_{L_0} + C_{L_{\alpha}} \cdot \alpha + C_{L_q} \cdot \frac{q(1.211)}{2 X 36} + C_{L_{\delta_e}} \cdot \delta_e \right]$$

 $\dot{\theta} = q$ 

$$\dot{q} = \frac{0.96 X (36)^2 X 12.47 X 1.21}{2 \times 907} \{ C_{m_0} + C_{m_\alpha} \cdot \alpha + C_{m_q} \cdot \frac{q(1.211)}{2 X 36} + C_{m_{\delta_e}} \cdot \delta_e \}$$

Substituting values of derivatives of S & C from ML method using multistep HALM5 Input (Refer Chapter 4, Table 4.3)

$$\dot{\alpha} = q - 0.0646 - 1.851 \cdot \alpha - 0.1793 \cdot q + 0.00562 \cdot \delta_e$$
  
$$\dot{\theta} = q$$
  
$$\dot{q} = 0.806 - 4.403 \cdot \alpha - 2.01 \cdot q - 8.95 \cdot \delta_e$$

Solving equation:

$$\dot{\alpha} = 0.8207.q - 1.851.\alpha + 0.00562.\delta_e - 0.0646$$
 5.47

$$\dot{q} = -2.01.q - 4.403.\alpha - 8.95.\delta_e + 0.806$$
 5.48

$$\dot{\theta} = q \tag{5.49}$$

Generalized State equation in Matrix form may be written:

$$\dot{x} = \mathbf{A} x + \mathbf{B} u \tag{5.50}$$

$$y = C x + D u$$
 5.51

To define A(plant matrix), B(control matrix), C(output matrix), and D(null matrix) as they are reflected in the above equation are compared with state space matrix form as A, B, C,& D.

$$\begin{bmatrix} \dot{\alpha} \\ \dot{q} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} -1.851 & 0.8207 & 0 \\ -4.403 & -2.01 & 0 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \alpha \\ q \\ \theta \end{bmatrix} + \begin{bmatrix} -0.0056 & -8.95 \\ -0.0646 & -0.806 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \delta \end{bmatrix}$$
 5.52

$$\begin{bmatrix} \theta \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \alpha \\ q \\ \theta \end{bmatrix} + \begin{bmatrix} 0 \end{bmatrix} \begin{bmatrix} \delta \end{bmatrix}$$
 5.53

The transfer function is required to construct a PID Controller. The transfer function of short period mode can be represented by using the formulae discussed below

$$T.F = \left| \frac{C A d j (I s - A)B}{I s - A} \right| + D$$

The following is a representation of the transfer function for the elevator deflection angle from the pitch angle: G(s)

$$G(s) = \frac{\theta(s)}{\delta(s)} = \frac{-\{8.95s + 16.5313\}}{s^3 + 3.861s^2 + 7.33141s}$$
5.54

Open loop Transfer function



Fig.5.12 Open Loop Control system of Hansa-III

The Open loop CS as illustrated in Fig.5.12 is independent of response in an action of control. The following is a representation of the estimated transfer function for the pitch angle to the elevator deflection angle G3(s)

$$G3(s) = \frac{\theta(s)}{\delta(s)} = \frac{-\{8.95s + 16.5313\}}{s^3 + 3.861s^2 + 7.33141s}$$
5.55

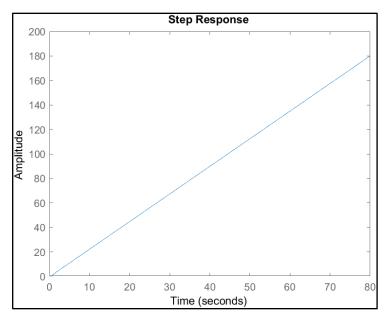


Fig.5.13 Open Loop Step Response of Hansa-III

The amplitude of the step response as displayed in Figure 5.13 of Open-loop CS is undamped which justifies to design of the controller in Closed-loop.

# Closed loop Transfer function

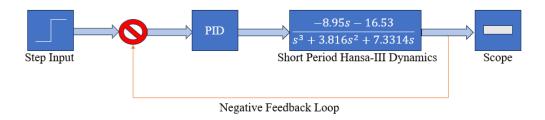


Fig. 5.14 Closed Loop Control system of Hansa-III

The controller of closed-loop CS displayed in Fig 5.14 depends on the output response termed feedback control system. The transfer function G4(s) is the output response of the input fed to the control system

$$G4(s) = \frac{\theta(s)}{\delta(s)} = \frac{\{55.94s + 103.3\}}{s^4 + 10.07s^3 + 31.18 + 101.8s + 103.3}$$
5.56

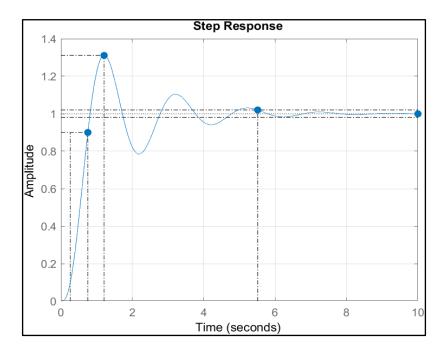


Fig. 5.15 Closed-loop Step- response of Hansa-III

The amplitude of the step response as displayed in Figure 5.15 of Closed-loop CS is damped and does not satisfy design requirements.

#### **5.4 PID TUNING METHODS**

#### **PID Controller**

PID stands for proportional, Integral, and derivative. This controller boosts the system's stability and reduces steady-state error. It is used in modern industry as an automatic process control for the flight control system. The three terms P, I, and D effectively control the system dynamics by calculating the error between the measured value and the desired value. The gain of these three parameters is tuned as per the system design requirements. The feedback control system uses a PID controller to precisely regulate the intended output. (Nelson, 1989)

$$u(t) = K_P e(t) + K_I \int e(t)dt + K_D \frac{d}{dt}e(t)$$
5.57

Taking Laplace transformation of the above equation and reducing it to

$$U(s) = [K_P + \frac{K_I}{s} + K_D s] E(s)$$
 5.58

The transfer function of the PID Controller  $G_{PID} = \frac{U(s)}{E(s)} = K_P + \frac{K_I}{s} + K_D s$ = $\left[\frac{K_P S + K_I + K_D S^2}{S}\right]$ 

PID tuning methods are used to compare the performance characteristics of the controller. Based on the control system response in terms of settling time, steady state error, percent overshoot, gain value and rise time the desirable methodology is adopted. These methods are listed into two categories

#### 1. Closed Loop Tuning Method

Closed-loop tuning methods are used when the control system is run in a closed loop and the controller is tuned automatically. Some closed-loop methods are: Ziegler Nicholas (ZN), Modified Ziegler Nicholas(MZN), Tyreus – Luyben(TL), Astrom – Hagglund (AH) (Mohammad Shahrokhi and Alireza Zomorrodi, 2005)

#### 2. Open Loop Tuning Method

Open-loop tuning technique is used when the control system is run in an open loop and the controller is tuned manually. Open-loop Ziegler Nicholas, CHR, Cohen and Coon, and Fertik are a few examples of open-loop techniques. (Mohammad Shahrokhi and Alireza Zomorrodi, 2005)

#### **5.4.1 CLOSED LOOP TECHNIQUES**

#### 1. Ziegler Nicholas

This trial and error technique was first put forward by Ziegler and Nicholas in 1942 for tuning gains of the PID Controllers. This approach was also used to tune PID Controller of a quadrotor helicopter for attitude determination(He & Zhao, 2014). Both open-loop and closed-loop control systems can make use of it and apply it when the mathematical model is unavailable(V. Kumar & Patra, 2016). This method determines gain by considering two parameters such as ultimate gain  $(K_u)$  and  $(T_u)$  as the period of oscillation at  $K_u$ . Process modelling is not required for this technique. Some consequences of ZN are time-consuming due to several iterations while estimating ultimate gain, and in-applicability for an open-loop unstable process. This tuning technique shows smooth transient behaviour. The block diagram shown in Figure 5.16 is used to estimate the gain parameters of PID while adopting various tuning techniques discussed in Table 5.4 using the software SIMULINK and algorithm (refer Appendix B 1). The steps followed to determine the value of  $K_u$  and  $T_u$  is stated below:

Step 1. Initializing  $K_I$  and  $K_D$  to be zero and the iterating numeric value of  $K_P$  to attain marginal stability curve in Scope

Step 2. Estimating the value of  $K_u$  and  $T_u$  from neutrally stable curve as displayed in the figure 5.17 (1-2)

Step 3. The gain of  $K_p$  becomes  $K_u$  when the system achieves neutral oscillation and  $T_u$  reflects the time- period of oscillations between one cycle occurring at an ultimate gain.

Step 4. The gain value for this research study is estimated are  $K_u = 1.3400$ ,  $T_u(s) = 1.5040$  s

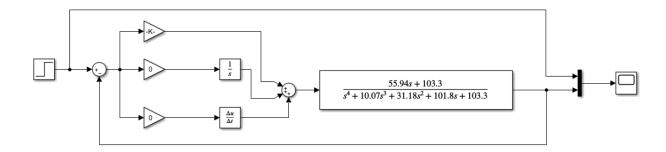
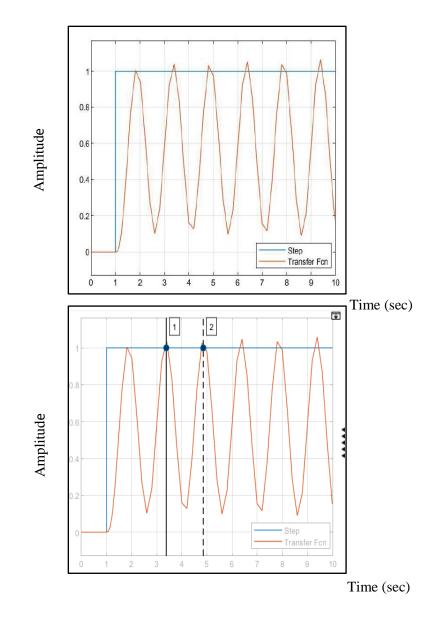
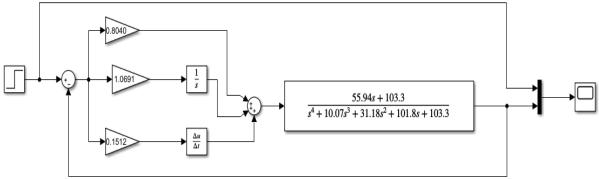


Fig 5.16 Simulink block diagram of estimating  $K_u$  and  $T_u$ 





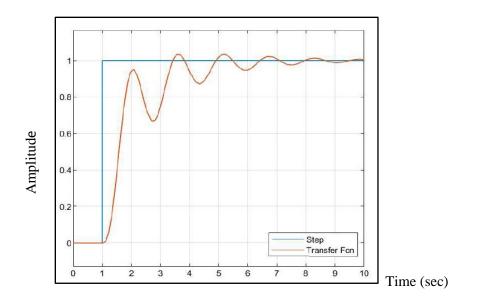


Fig 5.17(1-4) Estimation of KU ,TU , Step response and Simulink Block diagram of PID Controller: ZN

The step response in Fig 5.17(1-4) shows decayed oscillatory motion having damped amplitude signifies the stability of the pitch controller.

SNo	Methods	K <sub>P</sub>	K <sub>I</sub>	K <sub>D</sub>
1.	PID	0.6 <i>K</i> <sub>u</sub>	$(0.6K_u)(\frac{2}{T_u})$	$(0.6K_u)(T_u/8)$
2.	PD	$0.8K_u$	-	$0.1 * K_u * T_u$
3.	PI	0.45K <sub>u</sub>	$(0.45K_u)\left(\frac{1}{0.83T_u}\right)$	-

Table 5.4 Classical PID Tuning Parameters: ZN(Deepa & Sudha, 2016)

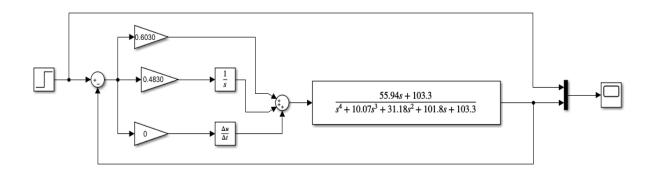


Fig 5.18 Simulink block diagram of PI Controller: ZN

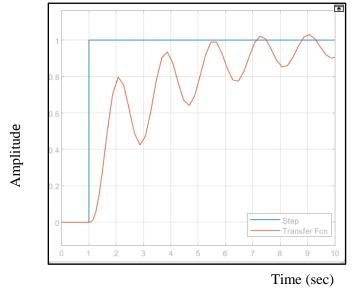


Fig 5.19 Step response of aircraft dynamics with PI Controller: ZN

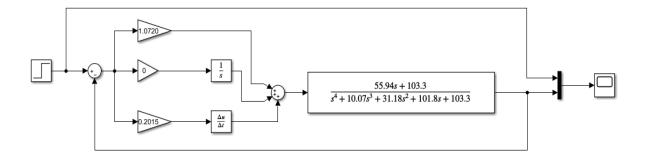


Fig 5.20 Simulink block diagram of PD Controller

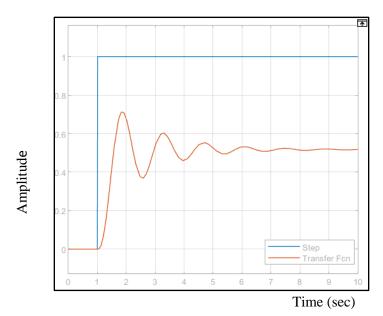


Fig 5.21 Step response of aircraft dynamics with PD Controller

S.No	Controller	K <sub>P</sub>	K <sub>I</sub>	K <sub>D</sub>
1.	Classic PID	0.8040	1.0691	0.1512
2.	PD	0.2015	-	1.0720
3.	PI	0.6030	48.117	-

Table 5.5 Classical PID, PD, PI Tuning Parameters Value: ZN

The gain parameters of PID, PD and PI while adopting ZN are discussed in Table 5.5 using Table 5.4 to illustrate the type of controller such as PID, PI, and PD have high  $K_I$  gain value that affects overall system performance &

The gain parameters of PID presented in Table 6 illustrate that all types of controller have high value of  $K_I$  which overall affects the system performance and leads to a responsive steady-state system.

#### 2. Modified Ziegler Nicholas

This method is utilised when it is difficult to quantify oscillation caused by a 1/4 decay ratio for some loops' and when set point changes for significant overshoots cannot be measured properly. This tuning technique shows smooth transient behaviour. The gain values  $k_P$ ,  $k_I$ ,  $k_D$  using modified Ziegler Nicholas setting is shown below(Basu et al., 2016)(Deepa & Sudha, 2016). The step response

illustrating aircraft	dynamics	are	shown	in	Fig	5.22	using	an	algorithm	(refer	to
Appendix B2)											

SNo	Methods	K <sub>P</sub>	K <sub>I</sub>	K <sub>D</sub>
1.	PID	00.33 <i>K</i> <sub>u</sub>	$0.5T_u$	0.33 <i>T</i> <sub>u</sub>
		0.4422	0.7520	0.4963

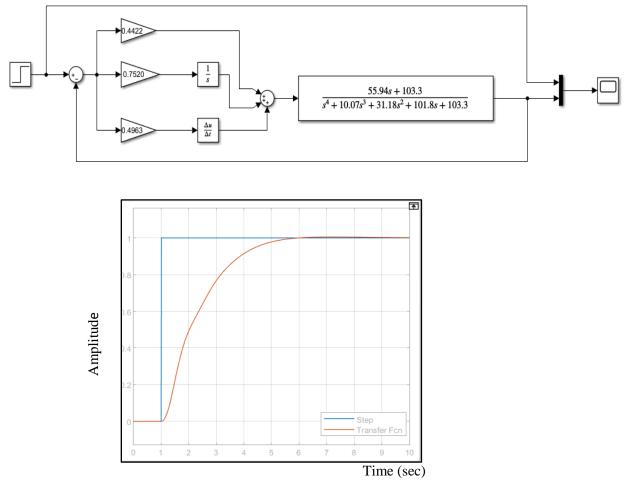


Fig 5.22 Step response and Simulink Block diagram of PID Controller using MZN

Figure 5.22-unit step response depicts an aperiodic, non-oscillatory motion of the pitch controller that is both highly stable and responsive in steady state.

#### 3. Tyreus Luyben

This technique is similar to Ziegler Nicholas and operates for PID and PI Controllers. The gain values  $k_P$ ,  $k_I$ ,  $k_D$  is different for this controller setting and mentioned below. It is time-consuming and attains marginal stability. This tuning technique shows smooth transient behaviour. The two characteristics of ultimate gain and the time-period is calculated using the same procedure as discussed in Ziegler Nicholas (Basu et al., 2016)(Deepa & Sudha, 2016). The step response illustrating aircraft dynamics is shown in Fig. 5.25 using algorithm (refer to Appendix B3)

S No	Methods	K <sub>P</sub>	K <sub>I</sub>	K <sub>D</sub>
1.	PID	<i>K<sub>u</sub></i> / 3.2	$(2.2T_u)$	$T_u/6.3$
2.	PI	$K_u/3.2$	$(2.2T_u)$	_

Table 5.7 Classical PIDTuning Parameters: TL

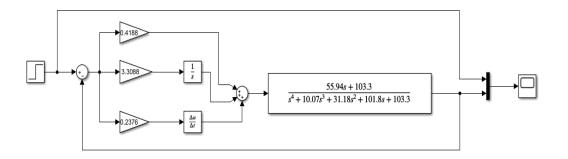


Fig 5.23 Simulink Block diagram of PID Controller using TL

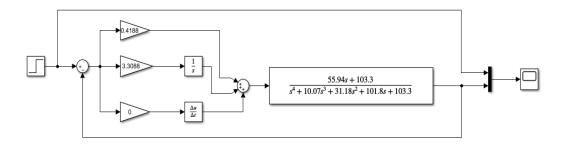


Fig 5.24 Simulink Block diagram of PI Controller using TL

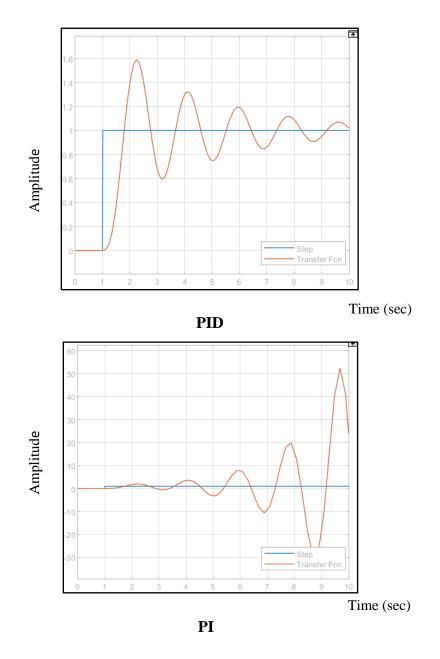


Fig 5.25 Step response of PID and PI Controller using TL  $\,$ 

	S.No	Methods	$K_P$	K <sub>I</sub>	K <sub>D</sub>
	1.	PID	0.4188	0.2376	3.3088
Γ	2.	PI	0.4188	3.3088	0

Table 5.8 Classical PID, PI Tuning Parameters Value: TL

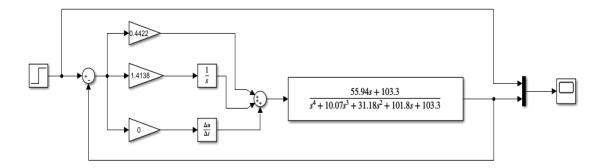
As discussed in Table 5.8, the unit step response in Fig. 12 illustrates an oscillatory motion of the pitch controller with a high amount of proportional gain, which causes the entire system to create constant steady state error and system sensitivity is reduced.

#### 4. Astrum-Haglund

This technique is initiated by Astrum-Haglund and uses non-linear feedback. The gain values  $k_P$ ,  $k_I$ ,  $k_D$  is different for this controller setting and are mentioned below. The two characteristics such as ultimate gain and the Time-period are calculated from limit cycle oscillation. This tuning technique shows oscillatory transient behaviour and does not involve a derivative filter (Basu et al., 2016)(Deepa & Sudha, 2016). The step response illustrating aircraft dynamics is shown in Fig 5.26 using an algorithm (Refer to Appendix B4)

S.No	$K_P$	K <sub>I</sub>	K <sub>D</sub>
1.	$0.32K_{pu}$	$0.94T_{u}$	0
2.	0.4422	1.4138	0

Table 5.9 Classical PID Tuning Parameters: AH



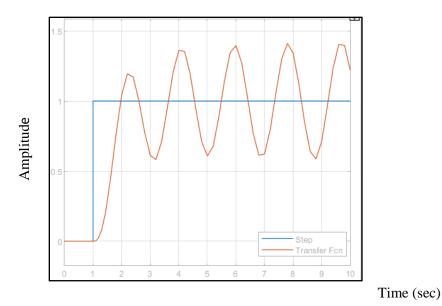


Fig 5.26 Step response and Simulink Block diagram of PID Controller: AH

The oscillatory motion in Fig.5.26 with the un-damped amplitude of the pitch controller indicates system instability in the unit step response. Table 5.9's PID gain parameters provide as an excellent example of steady-state performance.

In a similar pattern, all PID Closed-loop tuning approaches are applied to Multistep, Doublet, and Pulse Input datasets for gain optimization and results are compared using tabular and graphical representation in Appendix D1, D2.

#### **5.4.2 OPEN-LOOP TECHNIQUE**

#### 1. Open-loop Ziegler Nicholas

This method is similar to Ziegler Nicholas but the dynamics of the plant are modelled by the dead time model plus the first-order model given by expression (Basu et al., 2016)

$$G_m(s) = \frac{k_m e^{-ds}}{\Omega_m s + 1}$$
5.59

Where  $\Omega_m$  is dead time model, and  $k_m$  is the model gain. The gain parameters  $k_P, k_I, k_D$  is obtained by using Table 5.10

SNo	Methods	K <sub>P</sub>	K <sub>I</sub>	K <sub>D</sub>
1.	PID	$1.2 \Omega_{pn}$	2 <i>d</i>	0.5d
		$\overline{k_m} d$		
2.	Р	$1 \ \Omega_m$	-	-
		$\overline{k_m} d$		
3.	PI	$0.9\Omega_m$	d	-
		$\overline{k_m} d$	0.3	

Table 5.10 Classical PIDTuning Parameters: Open-loop ZN(Mohammad Shahrokhi and Alireza Zomorrodi, 2005)

#### 2. CHR Method

With the 20% overshoot and no overshoot options offered by this CHR (Chien, Hrones, and Reswich) technique provides the fastest response. This methodology is a modification of the Open-loop ZN technique(Mohammad Shahrokhi and Alireza Zomorrodi, 2005)(Ahn et al., 2009). The parameters obtained using the dead time model plus the first-order model are shown in Table 5.11

SNo	Methods	K <sub>P</sub>	K <sub>I</sub>	K <sub>D</sub>
1.	PID	$0.95\Omega_m$	2.4d	0.42 <i>d</i>
		$\overline{k_m} d$		
2.	Р	$0.3 \Omega_m$	-	-
		$\overline{k_m} d$		
3.	PI	$0.6 \Omega_m$	4 <i>d</i>	-
		$\overline{k_m} d$		

Table 5.11 Classical PIDTuning Parameters : CHR (Mohammad Shahrokhi and Alireza Zomorrodi, 2005)

#### 3. Cohen-coon Method

This technique involves process reaction curve as the first step and secondly estimating parameters by approximating the dead time model plus first-order model using the following relationship [ref](Mohammad Shahrokhi and Alireza Zomorrodi, 2005)

$$\Omega_m = \frac{3}{2} (t2 - t1)$$
 5.60

$$d_m = \Omega_2 - \Omega_m \tag{5.61}$$

Where t1, t2= time at  $\Delta c = 0.283\Delta c_s$ ,  $\Delta c = 0.632\Delta c_s$ , and C is plant output. Once  $\Omega_m$ ,  $d_m$ , and  $k_m$  is known then tuning parameters are estimated using the dead time model plus the first order model is shown in Table 5.12

SNo	Methods	K <sub>P</sub>	K <sub>I</sub>	K <sub>D</sub>
1.	PID	$\frac{1}{k_m}\frac{\Omega_m}{d}(\frac{4}{3}+\frac{d}{4\Omega_m})$	$d\frac{32+6d/\Omega_m}{13+8d/\Omega_m}$	$drac{4}{11+2d/\Omega_m}$
2.	Р	$\frac{1}{k_m}\frac{\Omega_m}{d}(1+\frac{d}{3\Omega_m})$	-	-
3.	PI	$\frac{1}{k_m} \frac{\Omega_m}{d} \left(\frac{9}{10} + \frac{d}{12\Omega_m}\right)$	$d\frac{30+3dm/\Omega_m}{9+20dm/\Omega_m})$	-
4.	PD	$\frac{1}{k_m}\frac{\Omega_m}{d}(\frac{5}{4} + \frac{d}{6\Omega_m})$		$d\frac{6-2d/\Omega_m}{22+3d/\Omega_m}$

Table 5.12 Classical PIDTuning Parameters: Cohen - Coon(Mohammad Shahrokhi and Alireza Zomorrodi, 2005)

#### 4. Fertick Method

This technique is used in open-loop and uses the dead time model plus first-order model for the model using expression

$$G_m(s) = \frac{ke^{-ds}}{\Omega s + 1}$$
5.62

$$\alpha_F = \frac{d}{d+\Omega} = \frac{T_d}{T_{ps}}$$
 5.63

Where  $\alpha_F$  is fertick controllability,  $T_d = d$ ,  $T_{ps} = d + \Omega$ . PID Controller is not applicable for plant whose  $\alpha_F > 0.5$ 

#### 5.5 CLASSICAL CONTROL APPROACH

#### **Root Locus**

The methodology to design flight control laws includes classical and modern control theory. In the past few decades, the FCS flight control system has been designed by making use of the root locus (Time- domain technique), or frequency domain technique. One of the best classical control techniques is the root locus introduced by W.R. Evan in 1948(Stojiljković et al., 2009) (Nelson, 1989). This methodology is simple, handy, and has system transparency as engineers can identify the gaps and modify them as per design requirements. It is also applied to design pitch attitude CS of F-104A aircraft(Stojiljković et al., 2009). The dynamics of the physical system are visible while operating. It is a graphical representation to analyse control systems. The necessary points to be noted while defining the stability of closed-loop systems are:

- 1. The closed-loop poles must be located in the left half of the complex plane.
- 2. The wider the gap of closed-loop poles from imaginary axes more system stability.

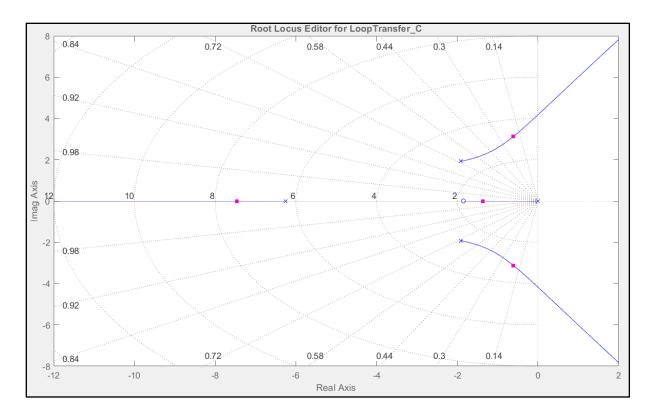


Fig 5.27 Root-Locus of Uncompensated Controller

As per the figure, the poles and zeroes lie at the left half of the complex plane which suggests the system stability is calculated using closed-loop TF G3

$$G3 = \frac{55.94s + 103.3}{s^4 + 10.07 \, s^3 + 31.18 \, s^2 + 45.82s}$$

Control system Toolbox is used to model, analyse, and design control systems in the time and frequency domain. The Root locus is viewed and the controller structure is manipulated in this toolbox. This toolbox is used to adjust the location of poles to attain desired system performance by varying system parameters in realtime. This technique also depicts system stability by having knowledge of pole location and estimating the natural frequency  $(w_n)$ , and damping ratio ( $\zeta$ ) of the system. At a similar time, the bode plot, Nyquist plot, step response, gain, and phase margin are also viewed to modify the controller structure. Classical methods are limited to SISO systems while modern control theory has the scope of MIMO system designs thus modern approaches are also covered in this study in the next section.

#### **Bode Plot**

This graphical method is introduced by the bode for stability analysis in the frequency domain. It contains two plots such as magnitude as well as phase plots which are plotted with logarithm values of frequency to give system information thus termed logarithm plots. Magnitude in decibels and phase angle in the degree of the LTI system are plotted for frequency.

Gain Margin: The gain at which the system stabilizes. It occurs at  $\omega_{pc}$  (phase crossover frequency) which is defined as frequency at -180° phase angle. If the magnitude in decibels of G( $j\omega$ ) at  $\omega_{pc}$  is positive then the gain margin will be negative and vice-versa. G.M= Gain at -180° phase.

Phase Margin: The phase angle at which the system becomes stable. It occurs at  $\omega_{gc}$  (gain cross-over frequency) It is characterized as the frequency at zero decibel gain. If the phase in degrees  $\phi_{gc}$  is positive than -180° then the phase margin will be negative and vice-versa.

 $P.M = 180^{\circ} + Phase at Odb$ 

The stability criterion is determined by estimating the Gain Margin and phase margin from the Bode Plot. The system will be stable if the Gain Margin and Phase Margin are both bigger than zero.; If the gain margin is infinite and the phase never crosses -180° then too system attains stability.

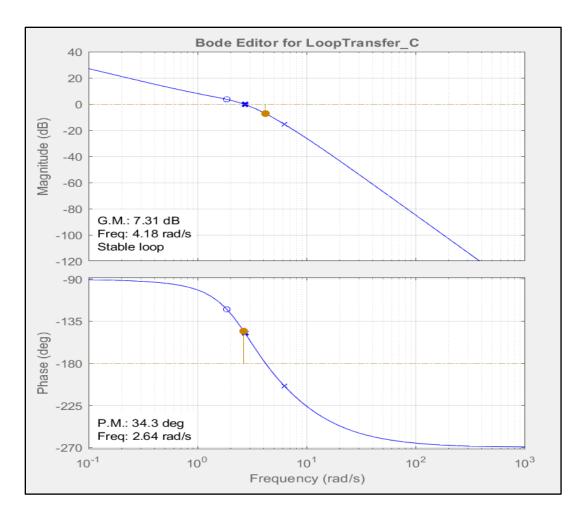


Fig 5.28 Bode-Plot of Uncompensated Controller

As per Figure 5.28, the value of the Gain margin and phase margin is positive which is calculated using closed-loop TF G3 as discussed in the above section concludes the system stability.

# 5.5.1 PD COMPENSATED CONTROLLER USING ROOT LOCUS TECHNIQUE

#### **Derivative Controller**

This controller produces an output that is derivative of the error signal. This controller improves system stability

The transfer function of the derivative Controller  $G_D = \frac{U(s)}{E(s)} = K_D s$ 

#### **Integral Controller**

The output of this controller is integral to the error signal. This will raise the system's type number which decreases steady state error but stability is decreased.

The transfer function of the Integral Controller  $G_I = \frac{U(s)}{E(s)} = \frac{K_I}{S}$ 

#### **PD** Controller

PD stands for proportional, and derivative. The derivative filter is used for transient response analysis. The two terms proportional, and derivative effectively control the plant dynamics by producing output which is the combination of output P and D Controller. The system's stability will be improved by this combination without having an impact on steady-state error.

The transfer function of the PD Controller  $G_{PD} = \frac{U(s)}{E(s)} = K_P + K_D s = K_P (1 + \frac{K_D}{K_P} s)$ where  $\frac{K_D}{K_P}$  denotes  $T_D$ .

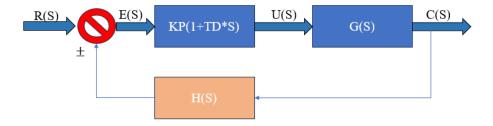


Fig 5.29 Schematic Diagram of PID Controller

# METHODOLOGY

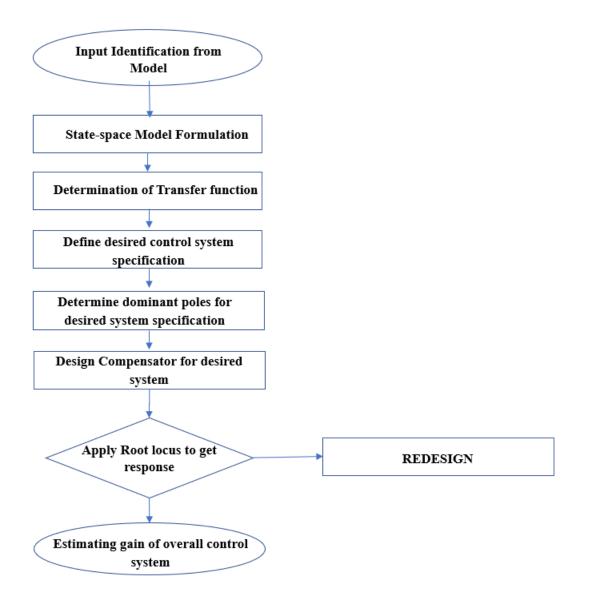


Fig 5.30 Flowchart to design aircraft Pitch Controller

#### **Control System Design Specification**

- 1. Settling Time<10sec
- 2. Peak Overshoot<20%
- 3. Steady State Error<1%
- 4. Rise Time<2sec
- 5. Gain Margin>6Db

6. Phase Margin>45°

# 5.5.2 UNCOMPENSATED FEEDBACK CONTROL SYSTEM

STEP1: Dynamics of an uncompensated feedback control system are analysed in MATLAB using the control system toolbox. The architecture used while designing the compensator is reflected in Fig 5.31

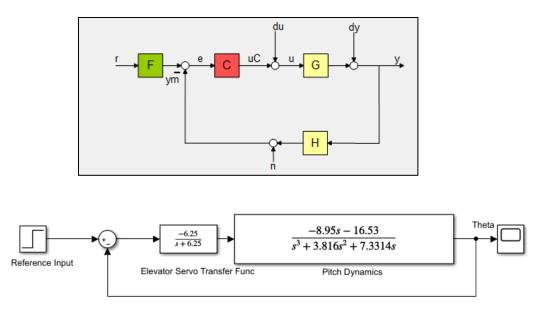


Fig 5.31 Uncompensated Feedback Control System

The uncompensated feedback control system includes elevator servomotor, Hansa-III pitch dynamics, reference input signal, and scope

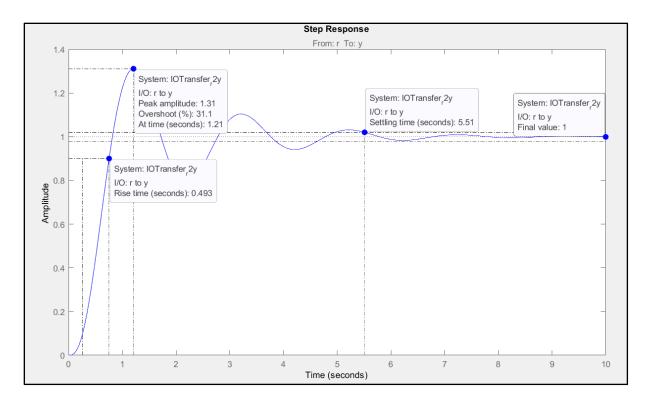
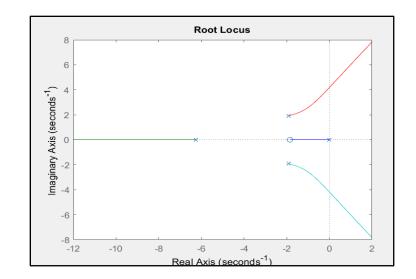


Fig 5.32 Step- Response of Uncompensated Feedback Control System

The uncompensated controller's step response as shown in above figure 5.32 explains the damping of the uncompensated pitch attitude system overshoots with 31.1% of amplitude 1.31. (It is required to drop down the value of overshoot by 20% as per design requirements). The oscillations damped gradually with the settling time of 5.51 seconds and experienced zero steady-state error which illustrates that the Integral controller is not required so a PD controller is designed.



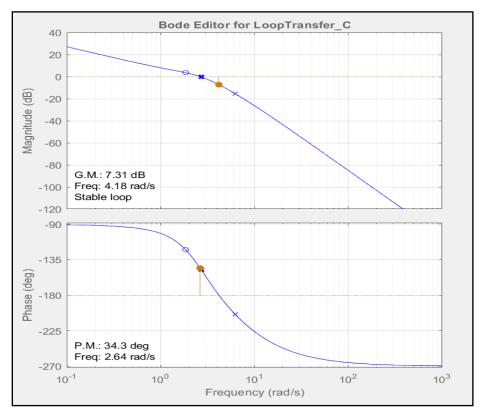


Fig 5.33 Root-Locus and Bode-Plot of Uncompensated Feedback Control System

The root-locus and bode-plot in fig 5.33 depicts the zeroes and poles of the control system whereas positive value of the phase margin in the bode plot signifies the system stability

# 5.5.3 DESIGN ALGORITHM OF PD COMPENSATED CONTROLLER

- 1. Define desired control system design specification
- 2. Determine dominant poles for desired design specification.
- 3. Design Compensator for the controller
- 4. Estimate the gain of the control system
- 5. Validate the result through SIMULINK software.

#### **STEP 1: Control System Design Specification**

- 1. Settling Time<10sec
- 2. Peak Overshoot<20%
- 3. Steady State Error<1%
- 4. Rise Time<2sec

# **STEP 2: Determination of Closed Dominant Pole**

Figure 5.34 below displays the uncompensated controller's root locus which states that damping  $\zeta = 0.456$  at 20% overshoot thus by visualizing the above figure the closed dominant pole is located at -3.74+7.3i and the gain of the system is 1

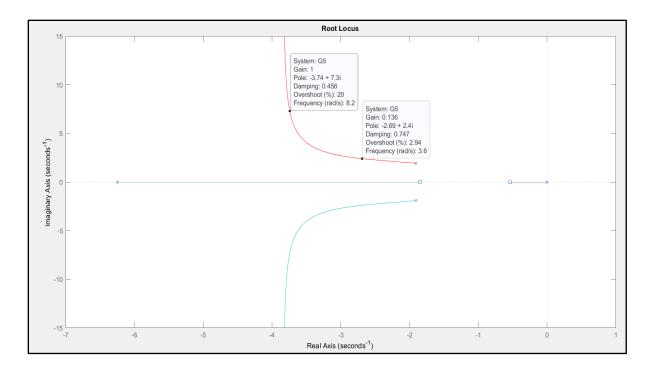


Fig 5.34 Location of Closed Dominant Pole

As per design specifications, settling time Ts < 10 sec as  $\zeta \omega_n = \frac{4}{Ts}$  thus  $\zeta \omega_n = 0.4$ . The damping ratio of SP mode is calculated by relationship as  $\Theta = \cos^{-1} \zeta$ . Consider  $\zeta$  as 0.456 from the above figure as satisfying the design requirements. The estimated angle is found to be 62.87°

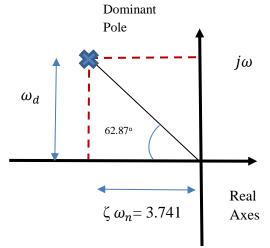


Fig 5.35 Determination of Damping Ratio

Tan(62.87°) =  $\frac{7.3}{\zeta \omega_n}$  thus  $\zeta \omega_n = \frac{7.3}{1.951} = 3.741$  as per the given figure 5.35, the closed dominant poles from origin to s-plane is  $-3.741 \pm 7.3$  j which validates the point reflected in the above figure.

### **STEP 3: Design of PD Compensated Controller**

The controller has two complex poles, two real poles, and one zero as shown below

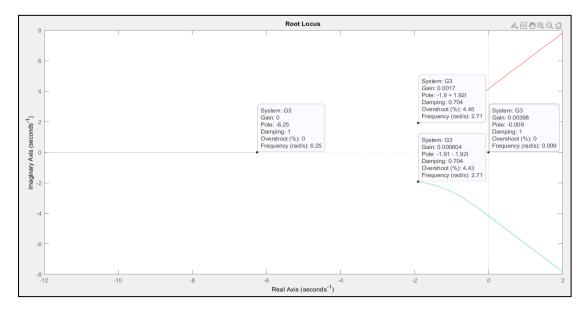


Fig 5.36 Root-Locus of PD Compensated Controller

The compensator can be designed by applying the root locus algorithm which is estimated by calculating angles from complex poles which is given by  $A=180^{\circ}$ -(Summation of angles made by complex dominant pole to other poles) + (Summation of angles made by complex pole to other zeros)

As reflected below Figure 5.36; the controller has two poles and one zero in Real axes thus A is estimated using the following expression as  $A = 180^{\circ}$ - (Summation of angles made by complex dominant pole to other poles)

A =  $180^{\circ}$  - ( $\theta_1 + \theta_2 + \theta_3 + \theta_4$ ) + $\theta_5$ (Nagoor Kani - Control System 5.64 Engineering-RBA (2013).Pdf, n.d.)

$$\tan\left(\theta_{1}\right) = \frac{y^{2} - y_{1}}{x^{2} - x_{1}} = \frac{0 - 7.3}{0 - -3.74} = -1.95$$

$$\theta_{1} = 180^{0} - tan^{-1}(-1.95) = -62.87^{0} = 117.13^{0}$$

$$tan (\theta_{2}) = \frac{y^{2} - y^{1}}{x^{2} - x^{1}} = \frac{0 - 7.3}{-6.25 - -3.74} = 2.9083$$

$$\theta_{2} = 180^{0} - tan^{-1}(2.9083) = 70.992^{0}$$

$$Complex \ pole \ (-1.91 + 1.92i)\theta_{3} = 180^{0} - tan^{-1}\frac{7.3 - 1.92}{3.74 - 1.91} = 108.791^{0}$$

$$Complex \ pole \ (-1.91 - 1.92i)\theta_{4} = 180^{0} - tan^{-1}\frac{7.3 + 1.92}{3.74 - 1.91} = 101.227^{0}$$
Summation of angles made by complex dominant pole to other poles

$$X = 180^{0} - (\theta_{1} + \theta_{2} + \theta_{3} + \theta_{4})$$
 5.65

 $A = 180^{0} - (117.13^{0} + 71^{0} + 108.791^{0} + 101.227^{0})$ 

Summation of angles made by complex dominant pole to other zeros

$$Y = \theta_5$$
 5.66  
 $\theta_5 = 180^{0} - tan^{-1}(-3.8624) = 104.516^{0}$   
 $A = X + Y$  5.67  
 $A = -113.627^{0}$ 

Now the angle measured by PD Compensated zero  $Z_c$  as reflected in the figure 5.4.26 mentioned below is calculated using a trigonometric relationship

$$\tan(180^0 - 113.627^0) = \frac{7.3}{3.74 - Z_C}$$
 5.68

$$2.285 = \frac{7.3}{3.74 - Z_C}$$
$$Z_C = 0.5453$$

## **STEP4: Gain Estimation**

Thus, the value of compensated zero is given by  $Z_c$  as 0.5453. It is possible to write the transfer function of compensated zero as K(S+0.5453) where K is the system's loop gain.

The transfer function of the PD Controller  $G_{PD} = \frac{U(s)}{E(s)} = K_P + K_D s = K_P (1 + \frac{K_D}{K_P} s)$ where  $\frac{K_D}{K_P}$  denotes  $T_D$ .

$$G_{PD} = \frac{U(s)}{E(s)} = K_P + K_D s = K_P (1 + \frac{K_D}{K_P} s) = 0.5453(1 + 1.8s)$$
 5.69

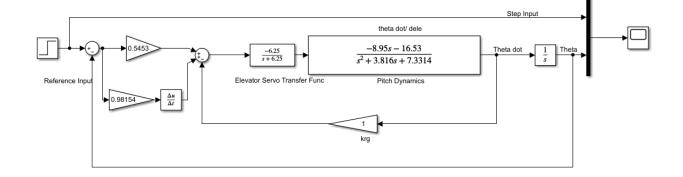
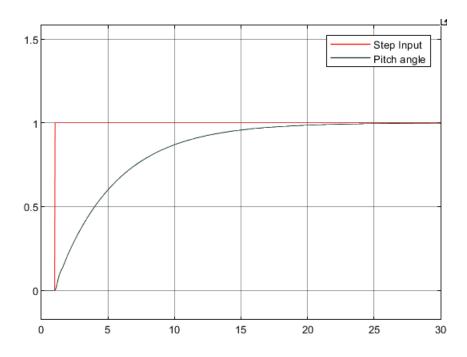
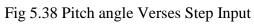
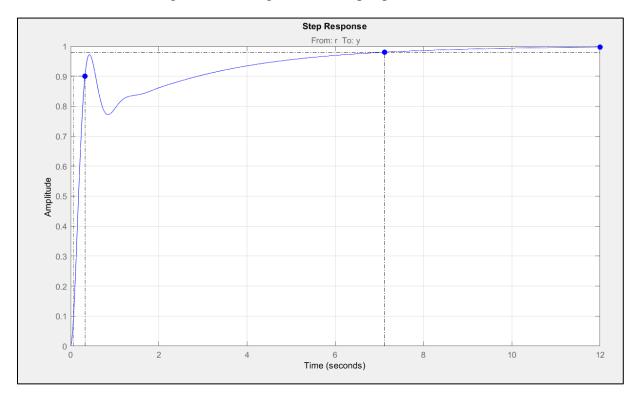


Fig 5.37 Pitch Attitude Control System







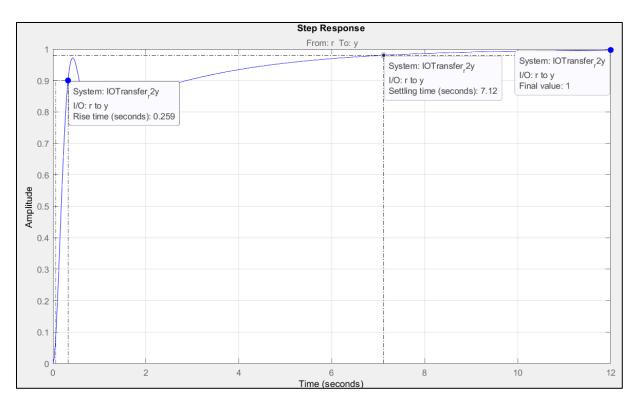


Fig 5.39 Step Response of the Pitch Angle

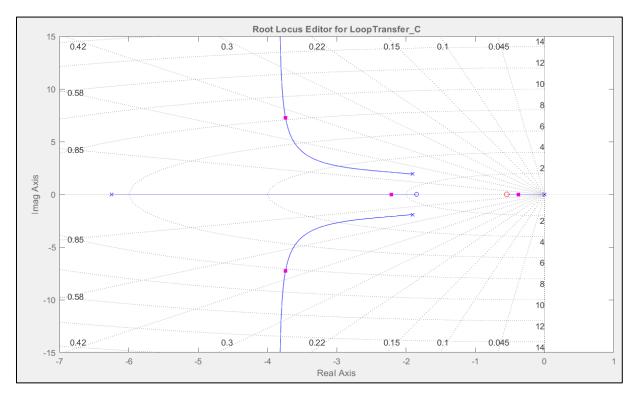


Fig 5.40 Root-Locus Plot compensated Controller

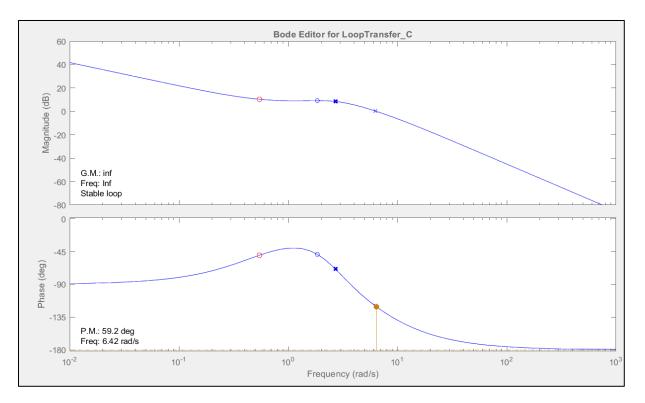
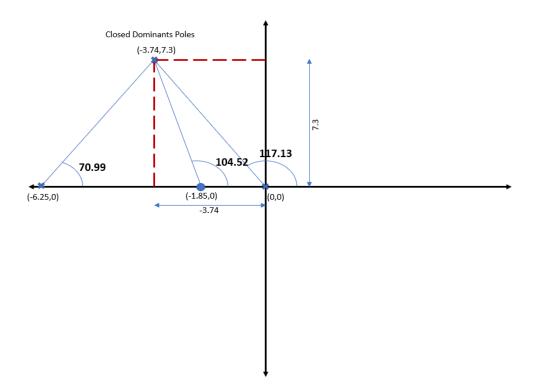


Fig 5.41 Bode Plot of compensated Controller



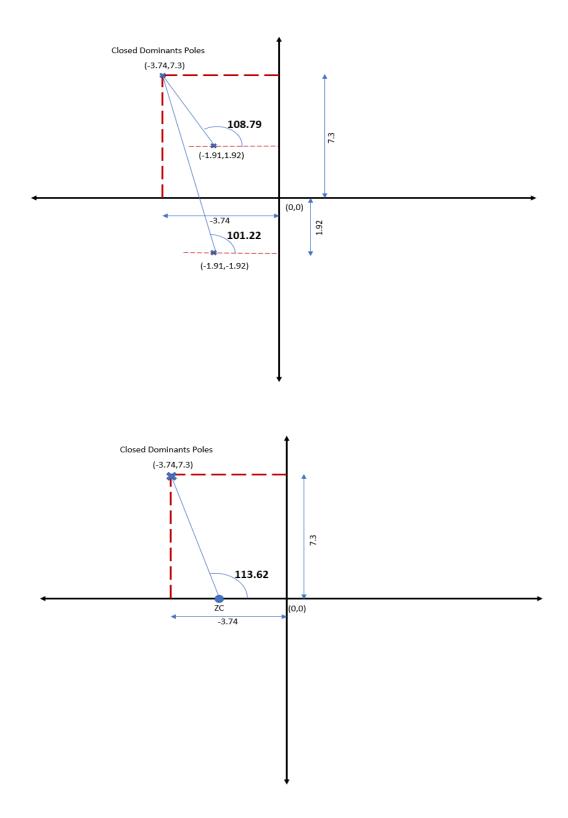


Fig 5.42(1-3): Compensator Diagram

The Time-domain characteristics with and without controller is displayed below in Tabulated and pictorial representation

S. No	Time Domain Characteristics	Without Controller	With Controller
1.	Settling Time<10sec	5.51	7.12
2.	Peak Overshoot<20%	31.1	0
3.	Steady State Error<1%	1	1
4.	Rise Time<2sec	0.493	0.259

S. No	Frequency Domain Characteristics	Without Controller	With Controller
1.	Gain Margin>6Db	7.31	$\infty$
2.	Phase Margin>45°	34.3	59.2

# Table 5.13 Hansa-III Pitch Attitude Characteristics

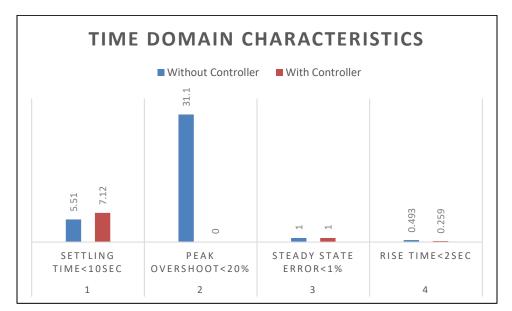


Fig 5.43 Bar Pictorial Representation with and without Controller in Time-Domain

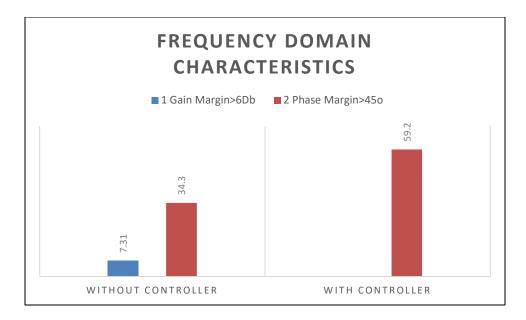


Fig 5.44 Bar Pictorial Representation with and without Controller in Frequency-Domain

All time-domain characteristics satisfying design requirements as displayed in Table 5.13. The stability criterion is determined by estimating Gain Margin and phase margin from Bode Plot. The system will be stable if the Gain Margin and Phase Margin are both bigger than zero.; If the gain margin is infinite and the phase never crosses -180° then too system attains stability. Table 5.13 and Figure 5.44 demonstrates that gain margin of the system with controller is infinite shows stable characteristics of Pitch attitude of RCT Aircraft.

### **5.6 MODERN CONTROL METHODS**

Recent advancements in technology evolved novel approaches to design control systems termed modern control theory. Classical methods are limited to SISO systems while modern control theory has the scope of MIMO, time-variant, linear or non-linear systems. High-order systems are replaced by first-order differential equations to reduce system complexity. Optimization techniques are easily applicable to solve optimal control problems using this approach. A recent study on modern control theory had a significant impact on the aerospace sector(Nelson,

1989). Approaches such as guaranteed dominant pole placement, and LQR to design PID Controller of UAV(Debaleena et al., 2016). LQR and LQG Controller to study longitudinal and lateral flight dynamics is discussed and implemented for optimal estimation(Chrif & Kadda, 2014). Fuzzy PID Controller, Sliding mode controller, PID Controller to study pitch dynamics(Khalid et al., 2019)(Kisabo, 2012) as well as LQR and fuzzy logic to design aircraft roll, and yaw controllers are also discussed(Usta et al., 2011)(George, 2012). The Pitch attitude control system of F-4 fighter jet aircraft is designed using PID, fuzzy logic PID(BOSSERT DAVID E & KELLY, 2002). The two methodologies such as pole placement and LQR are proposed to estimate the gain matrix for designing the PID Controller of Hansa-III. The state feedback control system's block diagram is displayed in Figure 5.45

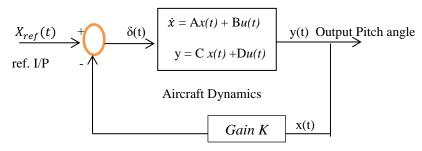


Fig 5.45 Feedback Control Design

### **5.6.1 POLE PLACEMENT TECHNIQUE**

The Pole placement technique calculates the gain matrix to guarantee system stability. The Controller has to modify the A matrix to change system dynamics. The eigenvalue of A matrix indicates the system's poles whereas the location of poles dictates system stability thus desired pole location is an important feature of this technique satisfying all design requirements. The closed-loop dominant poles have faster system response as compared to other poles.

Generalized State equation in Matrix form may be written:

$$\dot{x} = \mathbf{A} x + \mathbf{B} u \tag{5.70}$$

$$y = C x + D u$$
 5.71

To define A(plant matrix), B(control matrix), C(output matrix), and D(null matrix) as they are reflected in the above equation are compared with state space matrix form 5.27 as A, B, C,& D.

$$\begin{bmatrix} \dot{\alpha} \\ \dot{q} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} -1.851 & 0.8207 & 0 \\ -4.403 & -2.01 & 0 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \alpha \\ q \\ \theta \end{bmatrix} + \begin{bmatrix} -0.00562 \\ -8.95 \\ 0 \end{bmatrix} \begin{bmatrix} \delta \end{bmatrix}$$
 5.72

$$\begin{bmatrix} \theta \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \alpha \\ q \\ \theta \end{bmatrix} + \begin{bmatrix} 0 \end{bmatrix} \begin{bmatrix} \delta \end{bmatrix}$$
 5.73

The open loop poles of matrix A are 0,  $-1.9305 \pm 1.8993i$ 

$$u = I.k_r - k * x$$

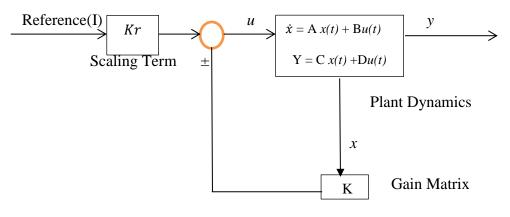


Fig 5.46 Pole Placement

The steps followed in the pole-placement technique are discussed as:

- 1. Check system state controllability
- 2. Choose closed-loop poles using the Butterworth methodology
- 3. Determine the Feedback gain matrix using Ackermann's theorem

### STEP-I

If the states of the dynamic system affect the control input, controllability difficulties may arise. If the system state is unaffected then the system is uncontrollable. The sufficient condition for the system controllability test is the rank of the system is the same as the controllability matrix which is measured by  $V = [B AB A^2*B]$  for third order system and in MATLAB scripted as V = ctrb(A, B)

 $V = \begin{bmatrix} 0.0056 & 7.3349 & -28.3611 \\ 8.9500 & -18.0142 & 3.9132 \\ 0 & 8.95 & -18.0142 \end{bmatrix}$ 

The rank of R1 = rank(V) = 3

The system states controllable as the rank of V is of the same order as the system.

### **STEP-II**

Closed-loop poles must lie at the desired location. All poles including dominant poles must lie at a specific location. It is required to avoid choosing closed-loop poles far away from open-loop poles. The value of closed-loop poles must not be highly negative as the system response will be too fast. The approach used in closed-loop pole selection employing the Butterworth polynomial equation for pole placement is dictated in equation 5.74 (Radhakant Padhi, n.d.)

Butterworth Polynomial equation can be rewritten as:

$$\left(\frac{S}{W_0}\right) = \left(-1\right)^{\frac{n+1}{2n}} \left[\frac{e^{j(2k+1)\pi}}{-1}\right]^{\frac{n+1}{2n}}$$
5.74

where k = 0, 1, 2---- so on

 $w_0$  = natural frequency

n= system order which states number of closed-loop poles

As per trigonometric identity:

$$e^{j(2k+1)\pi} = \cos(2k+1)\pi + j\sin(2k+1)\pi)^n$$

$$= \cos(2k+1)\pi + j\sin(2k+1)\pi$$
As matrix A is of order three thus substituting n=3 in the above equation

As matrix A is of order three thus substituting n=3 in the above equation

$$\frac{n+1}{2n} = \frac{2}{3} \quad s = w_0 [\cos(2k+1)2\pi/3 + j\sin(2k+1)2\pi/3]$$
Case I:  
K=0;  $w_0 = 2.7$   
S<sub>1</sub>=  $w_0 [\cos 2\pi/3 + j\sin 2\pi/3] = (-1/2+j\sqrt{3/2})*2.7=-1.35+2.338j$   
Case II:  
K=1;  $w_0 = 2.7$   
S<sub>2</sub>=  $w_0 [\cos 2\pi + j\sin 2\pi] = -2.7$   
Case III:  
K=2;  $w_0 = 2.7$   
S<sub>3</sub>=  $w_0 [\cos 10\pi/3 + j\sin 10\pi/3] = (-1/2-j\sqrt{3/2})*2.7 = -1.35-2.338j$   
Case IV:  
K=3;  $w_0 = 2.7$   
S<sub>4</sub>=  $w_0 [\cos 14\pi/3 + j\sin 14\pi/3] = (-1/2+j\sqrt{3/2})*2.7 = -1.35+2.338j$   
Case V:  
K=4;  $w_0 = 2.7$   
S<sub>5</sub>=  $w_0 [\cos 6\pi + j\sin 6\pi] = -2.7$   
Case VI:  
K=5;  $w_0 = 2.7$   
S<sub>6</sub>=  $w_0 [\cos 22\pi/3 + j\sin 22\pi/3] = (-1/2-j\sqrt{3/2})*2.7 = -1.35-2.338j$ 

Desired closed-loop pole roots S1, S2, S3 are -1.35 $\pm$  2.338j, -1.3

### **STEP III**

The feedback gain matrix 'K' using the pole-placement technique is estimated using Ackermann's method. The algorithm to estimate the gain matrix is presented in Appendix B5. This method solves the pole placement problem while designing the control system for time-invariant systems represented by the equation as(Nelson, 1998)(Radhakant PadhiDepartment of Aerospace Engineering, n.d.)

$$u(t) = -kx(t) \tag{5.76}$$

The modified system equation is expressed as  $\dot{x} = (A - Bk)x$ ; let us define  $A^* = A - Bk$  since the Cayley-Hamilton theorem states that  $A^*$  satisfies own characteristic equation thus

$$\phi \quad (A^*) = A^{*n} + \alpha_1 A^{*n-1} + \dots - \dots - \alpha_{n-1} A^* + \alpha_n \quad (\text{Radhakant} \quad 5.77)$$

PadhiDepartment of Aerospace Engineering, n.d.)

Consider trigonometric Identities as I=I;  $A^* = A - Bk$ ;  $A^{*2} = (A - Bk)^2$ ;  $A^{*3} = (A - Bk)^3$ 

The system is states controllable as explained in step I thus pre-multiplying both sides of the equation by the inverse of the controllability matrix (Radhakant PadhiDepartment of Aerospace Engineering, n.d.)

$$C^{-1}\phi(A^{*}) = \begin{bmatrix} \alpha_{2}k + \alpha_{1}kA^{*} + k{A^{*}}^{2} \\ \alpha_{1}k + kA^{*} \\ k \end{bmatrix}$$
 5.78

Now pre-multiplying both sides of the equation by [0 0 1] matrix to obtain Ackermann's equation

Where k is the feedback vector,  $\phi$  (*A*<sup>\*</sup>) is desired characteristic equation of matrix A, and C is the controllability matrix

$$\phi(A^*) = \det(SI - (A - BK))$$
 5.81

The closed loop poles of matrix  $\phi(A^*)$  are:

-1.3000 + 0.0000i

- -1.3500 + 2.3380i
- -1.3500 2.3380i

The gain K as shown in the figure 5.47 is also determined using MATLAB function as 'acker' thus Gain K = acker (A, B, S);  $K = [-0.2612 \quad 0.0157 \quad 0.5728]$ 

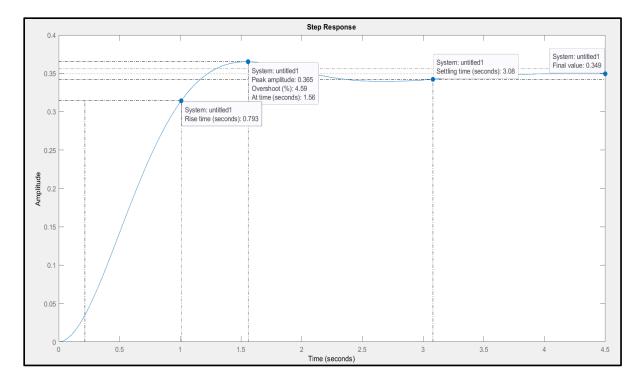
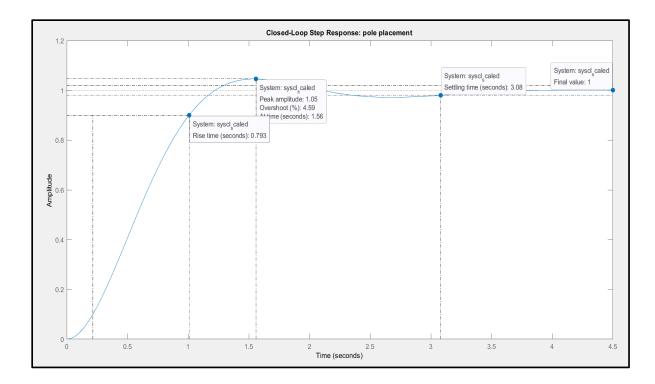


Fig 5.47 Step Response using pole placement without scaling effect

The scaling effect  $\overline{N} = 0.5728$  compensates steady-state error to 0.01 of the system as shown in the above figure 5.47



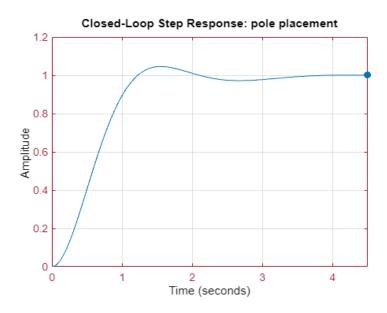


Fig 5.48 Closed-Loop Step Response using pole placement with scaling effect

The Time-domain characteristics with and without scaling effect is displayed below in Table 5.14

S.No	Closed loop Time-	Design	Pole-placement	Pole-placement
	domain response	Specification	with Scaling	without Scaling
			effect	effect
1.	Steady-state error	<1%	1	0.349
2.	Peak overshoot	<20%	4.59	4.59
3.	Settling Time (sec)	<10sec	3.08 s	3.08 s
4.	Rise Time (sec)	<5sec	0.793 s	0.793 s

 Table 5.14 Time domain Performance characteristics using Pole-Placement

 Technique

The pitch angle response utilizing the pole assignment technique shown in Figure 5.47,5.48 depicts zero steady state error while compensating for steady state error from 0.349 to 0.01 with a scale factor N = 0.5728.

#### **5.6.2 LINEAR QUADRATIC REGULATOR**

The system performance in the time and frequency domain is measured in the form of settling time, rise time, peak time, Gain Margin, Phase Margin, and Bandwidth. Traditional methods cannot handle the problem of designing an aircraft attitude control system that requires pleasing design criteria. An advanced approach known as optimal control made it feasible to solve complex system problems. LQR is an optimal modern control approach that solves optimization problems by keeping the cost function minimal with subjected to a given set of constraints(Haddar et al., 2021). This method is comparable to pole placement since gain K is implemented similarly, as seen in Fig. 5.45, but gain K's value is selected using a different process. By selecting closed-loop characteristics with the help of the cost function, optimal gain K is computed. (Wahid & Rahmat, 2010)(Ashraf et al., 2018)(JAISWAL & PRAKASH, 2022).

### PROCEDURE TO SOLVE LQR PROBLEM

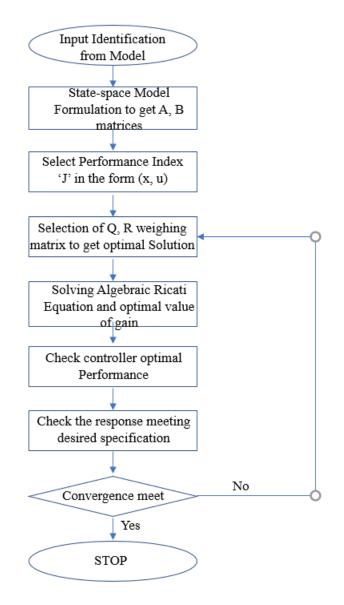
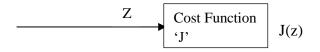


Fig 5.49 Flowchart of Linear Quadratic Regulator

The objective of this theory helps in satisfying all physical constraints and minimizes performance Index 'J'



J(z) = Cost function that measures how much solution z costs. The set to solve optimization problem includes feasible sets  $z = \{z_1, z_2, z_3 - \dots - z_5\}$ 

$$J_3(z) = Q J_1(z) + R J_2(z)$$

The minimal value of the cost function gives an optimal solution. The performance Index can be rewritten as(Nelson, 1998):

$$J = \int_0^\infty \{ x^T Q x + u^T R u \} dt$$
 5.82

Q, and R are known as scaler weights as well as the weighted squares of deviation of state from target and weighted square of control activity, x as a state vector, u as input vector. The Q term measures performance characteristic such as settling time (ST), rise time (RT), and peak time (PT) and the R term penalize actuator effort. The integrand function depicts the area under the curve. Q measures the convergence rate (Settling and Rise time), and R penalizes aggressive Input. The Q and R allow a trade-off between the rate of convergence and input activity.

Rise and Settling time implicit in  $x^TQx$  term. Damping ratio, overshoot, oscillations implicit on square functions. The positive and negative error is penalized using square functions. The peak value of the function is penalized using a square.

To penalize the negative values of the linear function, the states are squared and hence termed as a Linear quadratic function. These functions have a definite minimum value. The square is used because it leads to an easier analysis of the system.

Optimizing performance Index concerning parameters of state feedback and subject to given dynamics

$$\min \mathbf{J} = \int_0^\infty \{ x^T Q x + u^T R u \} d\mathbf{t} \longrightarrow \dot{x} = \mathbf{A} x + \mathbf{B} u; \ u = -k \mathbf{x} \longrightarrow \dot{x} = (\mathbf{A} \cdot \mathbf{B} \mathbf{k}) x$$

whereas,  $x(t) = n \times 1$  state vector,  $Q = n \times n$  symmetric positive semi-definite matrix,  $u(t) = m \times 1$  control vector,  $R = m \times m$  symmetric positive semi-definite matrix as a result, J will be positive.

#### **STEPS FOR K DETERMINATION**

STEP 1: Formulate a linear state-space model to get Matrices A and B from plant dynamics

Generalized State equation in Matrix form is written as:

$$\dot{x} = \mathbf{A}x + \mathbf{B}u \tag{5.83}$$

To define A(plant matrix), and B(control matrix), as they are reflected in the above equation are compared with state space matrix form

$$\begin{bmatrix} \dot{\alpha} \\ \dot{q} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} -1.851 & 0.8207 & 0 \\ -4.403 & -2.01 & 0 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \alpha \\ q \\ \theta \end{bmatrix} + \begin{bmatrix} -0.00562 \\ -8.95 \\ 0 \end{bmatrix} \begin{bmatrix} \delta \end{bmatrix}$$
 5.84

STEP 2: Choose weighing matrices Q, and R to get a minimal value of performance Index for an optimal solution. Start with  $Q = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ , R=  $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ 

 $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  and iterate as per design requirements.

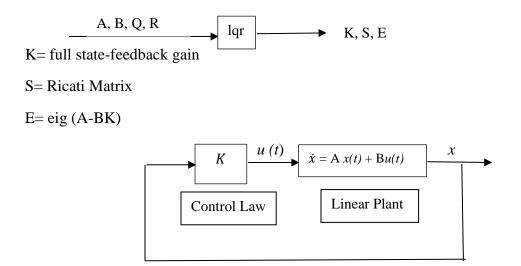
For SISO systems, R can be left at unity and Q33 weighs the most important state from the response of the system and leaves other weights at unity(Sushamshushekar Doddabasappa, 2019). Initializing x = 400,  $Q = x C^{T*}C$ 

 $C = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix} Q = \begin{bmatrix} 0 & 0 & 0; 0 & 0 & 0; 0 & 0 & x \end{bmatrix} \quad R = \begin{bmatrix} 1 \end{bmatrix}$ 

STEP 3: Solve non-linear Algebraic Riccati Equation for determining matrix S which indicates the solution by using MATLAB function 'CARE'

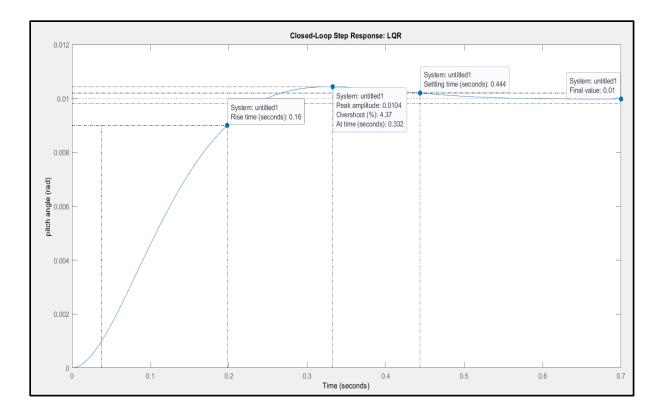
STEP 4: The optimal control law solves the algebraic Riccati equation for S as  $A^{T}S$  +SA-SBR<sup>-1</sup>B<sup>T</sup>S +Q=0. The control law is stated as u = - k x where k = R<sup>-1</sup>B<sup>T</sup>S thus

determining gain by swapping all values for A, B, Q, R, and S. The Gain K is also obtained using lqr MATLAB function as [K] = lqr (A, B, Q, R)



STEP 5: Choose the K solution that yields a stable system. The estimated value of optimal gain  $K = [-0.4717 \ 1.88 \ 20.00]$  using algorithm discussed in Appendix B6

STEP 6: The closed-loop step response provides information on performance characteristics like settling time, peak time, SSE



To reduce steady-state error, a scale factor should be added to compensate for the error but for this controller design, the gain value is found to be unity which concludes that K itself stabilizes the system and steady-state error approaches 0.01 as per design requirement. Figure 5.50 displays the closed-loop step and pitch angle response using LQR controller.

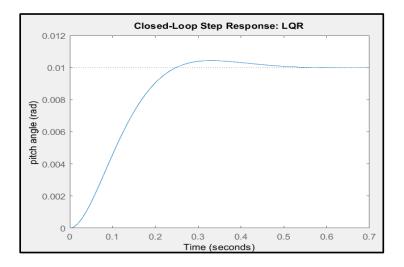


Fig 5.50 Closed Loop Step Response using LQR Controller

The Time-domain characteristics without scaling effect is displayed below in Table 5.15

S. No	Closed loop Time-domain	Design	LQR without
	response	Specification	Scaling effect
1.	Steady state error	<1%	1
2.	Peak overshoot	<20%	4.37
3.	Settling Time	<10sec	0.444 s
4.	Rise Time	<5sec	0.16 s

# Table 5.15 Time domain characteristics using LQR

The pitch angle response utilizing LQR is shown in Fig.5.50, where the gain value is determined to be unity, concluding that K stabilizes the system by itself and that steady-state error approaches the design requirement of 0.01

# Remark:

- 1. The optimal state feedback system is guaranteed to be stable if the system is fully controllable.
- 2. More the value of R, the lesser the the input activity but slow state behavior leads to poor performance thus system has poor controllability.
- 3. In a Controllable system, every coefficient of a closed-loop pole polynomial can be defined as desired closed-loop poles using state feedback
- Optimal state feedback shows better performance than pole placement by enabling more systematic tuning/ trade-off between tracking and control activity.

#### **5.7 VALIDATION**

Controller Design is an Intermediate stage of the research study moreover, validation is a proof-match exercise that needs to be executed for result authentication. Results are validated in terms of time and frequency domain characteristics of classical and modern control methodologies for optimization of PID parameters of Hansa-III for pitch control

The outcomes of different varieties of the PID tuning method are analysed in the form of gain K  $_{p}$ , K<sub>i</sub>, K  $_{d}$ . The gain K  $_{p}$  improves the accuracy of steady-state tracking, decreases system sensitivity, and creates a constant steady-state error. The gain K  $_{d}$  has a poor steady-state response but leads to system stability moreover Ki has a good steady-state response but leads to system instability. The Transfer function of the Pitch controller has two zeros in the numerator, one pole at the origin, and a denominator that makes the system highly stable.

The PID tuning techniques are applied and results are compared in the Tabulated and graphical figure presented below which concludes that modified ZN proclaims the finest result as Astrum -Hagglund did not have a derivative component that leads to system instability and the response is undamped oscillatory motion. The gain values using a technique such as ZN and MZN are compared and have a feature of stability and approach steady-state error frequently but MZN satisfies controller design requirements. The tuning approach TL manifests a larger value of K d that increases aircraft stability despite that steady-state error is difficult to attain and thus unable to accomplish design requirements.

Method	General Aviation Airplane(Deepa & Sudha, 2016)	Hansa-III Aircraft
Modified ZN		
KP	0.6171	0.4422
KI	0.61	0.752
KD	0.406	0.4963
Ziegler Nicholas		
KP	1.122	0.804
KI	1.833	1.0691
KD	0.1711	0.1512
Tyreus- Luyben		
KP	0.8415	0.4188
KI	2.684	0.2376
KD	0.193	3.3088
Astrum- Hagglund		
KP	0.5984	0.4422
KI	0.94	1.4138
KD	0	0

Table 5.16 Result Validation of PID Tuning Techniques with general aviationairplane(Deepa & Sudha, 2016)

The results of different PID tuning Techniques in form of gain K  $_p$ , K<sub>i</sub>, K  $_d$  is validated with general aviation airplane (Deepa & Sudha, 2016)

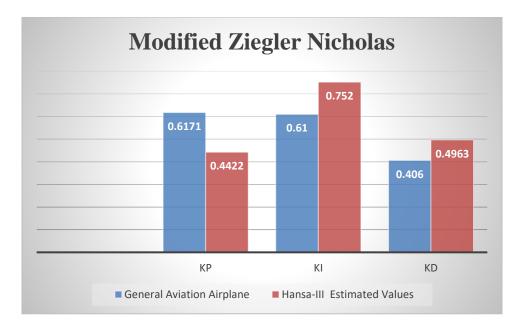


Fig 5.51 Result of Hansa-III with general aviation Airplane using MZN (Deepa & Sudha, 2016)

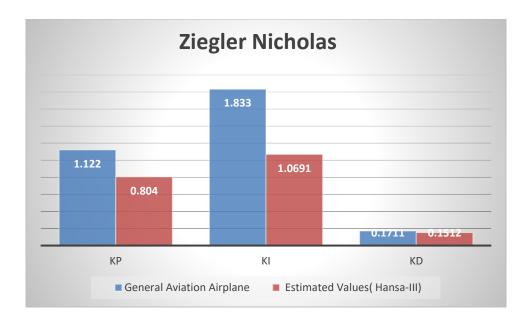


Fig 5.52 Result of Hansa-III with general aviation Airplane using ZN (Deepa & Sudha, 2016)

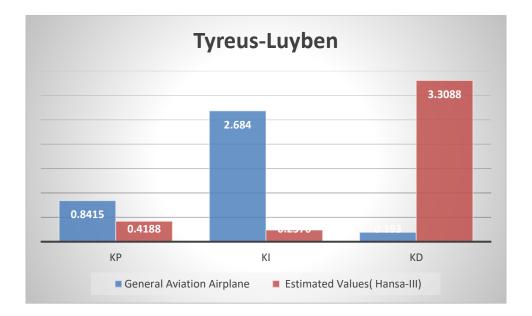


Fig 5.53 Result of Hansa-III with general aviation Airplane using TL (Deepa & Sudha, 2016)

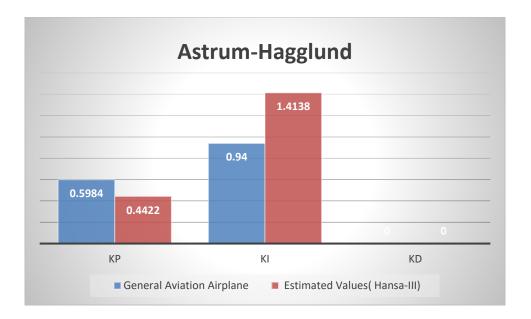


Fig 5.54 Result of Hansa-III with general aviation Airplane using AH (Deepa & Sudha, 2016)

a) The second traditional approach to estimating gain values of K<sub>p</sub>, K<sub>i</sub>, and K<sub>d</sub> is designing a compensator using a Root-locus Algorithm. The transfer function of compensated zero can be written as K(S+0.5453) where K is the loop gain of the system which is briefly discussed in root-locus section. The compensated controller's transfer function is provided as

$$G_{PD} = \frac{U(s)}{E(s)} = K_P + K_D s = K_P (1 + \frac{K_D}{K_P} s) = 0.5453(1+1.8s)$$

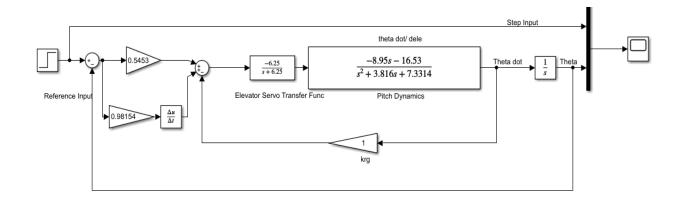


Fig 5.55 Simulink block diagram of Attitude Controller of Hansa-III

The Simulink block diagram of the Attitude Controller of Hansa-III is represented pictorially in Figure 5.55

The result in form of design specifications with and without the controller of Hansa-III is displayed in Table 5.17

S.	Time Domain Characteristics	Without Controller	With Controller
No			
1.	Settling Time<10sec	5.51 s	7.12 s
2.	Peak Overshoot<20%	31.1	0
3.	Steady State Error<1%	1	1
4.	Rise Time<2sec	0.493 s	0.259 s

Table 5.17 Time Domain Characteristics with & without Controller of Hansa-III

**b**) Modern control Techniques like pole placement and the linear quadratic regulator are used to estimate the gain matrix, and results are obtained in the form of Time-domain characteristics as displayed in Table 5.18 It is noted that the settling time is too fast for the LQR controller as compared to pole placement and LQR has an outstanding feature of approaching zero steady-state error.

S. No	Closed loop Time-	Design	Pole-placement	LQR
	domain response	Specification	without Scaling	without Scaling
			effect	effect
1.	Steady-state error	<1%	0.349	0.01
2.	Peak overshoot	<5%	4.59	0.332
3.	Settling Time	<5sec	3.08 s	0.44 s
4.	Rise Time	<2sec	0.793 s	0.16 s

Table5.18 Comparison of Time domain characteristics

The LQR Controller is chosen among traditional and modern approaches and the results obtained in the form of performance characteristics is validated with general aviation aeroplane (Wahid & Hassan, 2012)

S. No	Performance Characteristics	Hansa-III	General Aviation Airplane (Wahid & Hassan, 2012)
1.	Steady-state error	0.01	0.01
2.	Peak overshoot	0.332	4.35
3.	Settling Time	0.44 s	0.3655 s
4.	Rise Time	0.16 s	0.1335 s

 Table5.19 LQR Result Validation of Time domain characteristics with General

Aviation Airplane(Wahid & Hassan, 2012)

The performance characteristics of Hansa-III compared with General Aviation Airplane as shown below

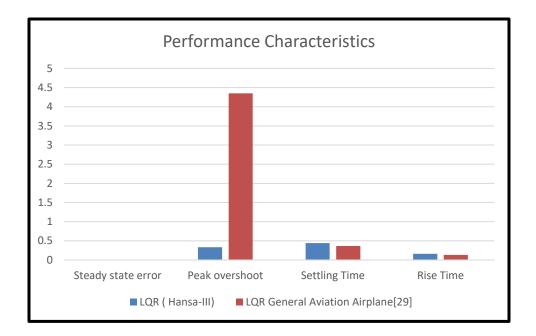


Fig 5.56 LQR Result of Hansa-III with general aviation Airplane (Wahid & Hassan, 2012)

# SUMMARY

In this chapter, the basics of an automatic control systems, aircraft stability and Control systems, Aircraft axes systems, and reference frames for the formulation of longitudinal force and moment equations in wind axes were addressed. This chapter focuses on longitudinal stability, and longitudinal modes (short-period, Long-period) for assessing flying handling qualities in terms of damping ratio and frequency. The Longitudinal equations were used to formulate a state–space matrix representation to deduce the transfer function for solving pitch control problems. The gain parameters using different approaches such as closed-loop PID Tuning techniques: ZN, MZN, AH, and TL were used for gain estimation. PID Tuning approaches were also applied to different datasets Multistep, Doublet, and Pulse (refer Appendix D1, D2) for comparison of approaches. Classical approaches such as Root-locus, and modern control approaches such as Pole-Placement, and LQR are discussed and results are compared for gain optimization. It is observed that the LQR Controller shows the best optimal result amidst classical and modern approaches. The FSFC (full state feedback controller) is designed and optimal control law for pitch control is developed.

# **CHAPTER -6**

# AIRCRAFT NAVIGATION SYSTEM

Research and Development in the field of Aircraft Navigation is always fascinating as it applies to finding the exact position, orientation, and velocity of aircraft. This study investigates the problem statements related to parameter estimation for aircraft positioning systems based on inertial sensor measurements provided by Hansa-III aircraft. Attitude and position can be resolute by an accelerometer and gyroscope. M. Jayachandran presented an approach to DR to measure aircraft position. When the GPS is not working, this procedure is useful for navigating. The Navigational algorithm is implemented within the display system of aircraft that receives information about attitude. and position(Jayachandran et al., 2009). Dead Reckoning is applied in numerous navigation applications such as aircraft navigation, automotive navigation, surveillance, mobile robots, and marine navigation. Zeev Berman discussed future aspects of aviation navigation systems as the Dead reckoning system. He presented an actual statistical model and varied wind vectors to match actual data. To measure the horizontal positioning error, he compared the dead reckoning system, standalone inertial sensors, and inertial sensors integrated with the DR system. (Berman, 1998). Parinaz estimated navigational parameters such as position using PDR (Pedestral Dead Reckoning) of mobile robots. The PDR algorithm was designed to get more accurate gait parameters which will improve the accuracy of position estimates (Kasebzadeh, 2017). Philips integrated GPS and DR sensors to track and navigate low-cost vehicles. Results for GPS, tightly coupled DR, and loosely coupled DR are compared and explained. Tightly coupled DR gives the best optimum result as compared with all three.(G.Mattos,

1994)

Pure Dead Reckoning Technology is economical, cheaper and generate systematic inaccuracies, making it impractical to employ where a precise position-based radio-signal navigation system is needed. The study investigates the performances of tightly coupled INS/GPS, loose couple INS/ GPS, and INS using SIMULINK. Tightly coupled INS/GPS gives better performance than loosely coupled integration as proposed by T. Mahmoud(Mahmoud & Trilaksono, 2018). The DR approach is mitigated in a quad-rotor navigation system for better reliability and accuracy. It enables the quadrotor to estimate the distance from peak to peak. The simulated result shows the accuracy of the navigation solution while comparing INS and QDR approaches. QDR navigation solution is bounded while the INS solution diverges as proposed by A. Shurin (Shurin & Klein, 2020). Integration of the INS-GPS-GLONASS system to enhance systems accuracy is applied for combat aircraft, ships, and long-range missiles is discussed by G.S. Reddy (Reddy & Saraswat, 2013). Dead Reckoning approach is used in UAV as proposed by Lorenzo Fusini using XKF and NLO. IMU sensors such as (acceleration, rate gyros, inclinometer); altimeters; and cameras are used. Position, velocity, and altitude are used as observed states. XKF gives the best optimum result as compared with NLO(Fusini et al., 2017)

The selection of an accurate navigational coordinate estimation method is a big challenging issue for real-time navigation. Some methods like the GNSS Global Navigation satellite system are based on signal transmission through satellite but the challenge faced by these systems is loss of signal connectivity which is handled by using Dead reckoning(Kasebzadeh, 2017). Hansa-III, flight test is regulated and real flight data is gathered using a data acquisition system. Integration of the dead reckoning approach in Hansa-III aircraft is used for the estimation of latitude, longitude, and altitude ( $\varphi$ ,  $\theta$ , h) for future navigation prediction. Comparative assessment between dead reckoning and exponential smoothing is presented in tabulated and graphical form.

#### **6.1 DEAD RECKONING**

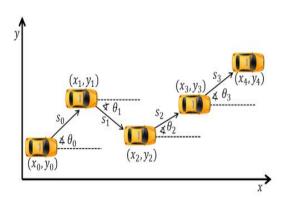
The Dead Reckoning methodology proposed for this study predicts the current location and velocity measurements by using previously determined locations over time elapsed on estimated speed. Pure Dead Reckoning is economical, and cheaper 8 Inertial measurement sensors including accelerometers, magnetometers, and gyroscopes are used for navigation through Dead Reckoning(Reddy & Saraswat, 2013). An accelerometer measures acceleration acting on the moving object to detect position whereas the magnetometer provides information about the direction and estimates magnetic induction. The gyroscope sensor measures the orientation and assesses the angular velocity (p, q, r) of an aircraft and provides position information, and orientation.

As per Figure 6.1, the absolute heading is measured by using sensors (gyroscope, digital compass). An odometer is used to measure the distance  $S_i$ .

The set of equations provides the DR solution

$$x_i = x_0 + \sum_{i=0}^{k-1} S_i Cos\theta_i \tag{6.1}$$

$$y_i = y_0 + \sum_{i=0}^{k-1} S_i Sin \Theta_i$$



6.2

Fig 6.1 Dead Reckoning (Pedro Paulo Liborio Lima do Nascimento,Leandro Aparecido Villas,Bruno Yuji Lino Kimura, 2018)

The heading of the vehicle is the same as the INS heading as a heading is measured from the INS sensor thus  $\theta_{\nu} = \theta_{INS}$ 

The NED coordinate system measures vehicle velocities in the North, East, and Down directions.  $V_N = V_C \cos \theta$ ,  $V_E = V_C \sin \theta$ ,  $V_{D=}$  -Altitude. The velocities are integrated to get the distance in the North, and East directions which state  $S_E = V_E$  $\Delta t$ ,  $S_N = V_N \Delta t$  where  $\Delta t$  is the sampling time.

#### **Dead Reckoning Algorithm**

The approach used to get an accurate navigational parameter using the DR algorithm is explained through a flowchart discussed in Fig 6.2

Block 1 explains the NED North, East, and Down coordinate systems used to determine aircraft velocity in the NED direction.

Block 2 estimates  $V_N$ ,  $V_E$ ,  $V_D$  using expression as  $V_N = V_C \cos \theta$ ,  $V_E = V_C \sin \theta$ ,  $V_{D=}$  -Altitude

Block 3 estimates  $S_N$ ,  $S_E$ , using expression as  $S_E = V_E \Delta t$ ,  $S_N = V_N \Delta t$  and X, Y, and Z coordinate is calculated as  $X(K) = X(K-1) + Se \cos \theta$ ,  $Y(K) = Y(K-1) + Sn \sin \theta$ , Z = -h

Block 4 depicts aircraft position in X, Y, and Z direction using expression as  $X(K) = X(K-1) \pm \Delta X$ ,  $Y(K) = Y(K-1) \pm \Delta Y$ ,  $Z(K) = Z(K-1) \pm \Delta Z$ 

Block 5 predicts the value of heading, and altitude based on existing values to predict measurements.

Block 6 Aircraft position in X, Y, and Z direction from block 4 is converted to geodetic coordinates as latitude, longitude, and altitude for determination of geographical location.

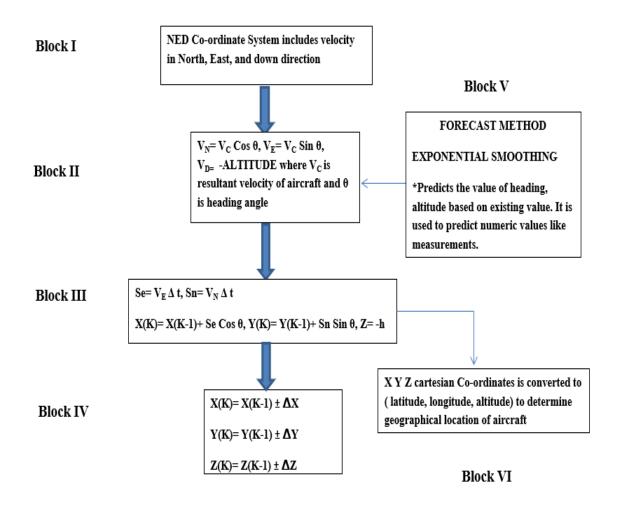


Fig 6.2 Flow chart of Dead Reckoning

# ROAD MAP TO ESTIMATE GEODETIC CO-ORDINATES

The road map for geodetic co-ordinate Estimation is shown in Fig 6.3 followed by steps I, II, and III

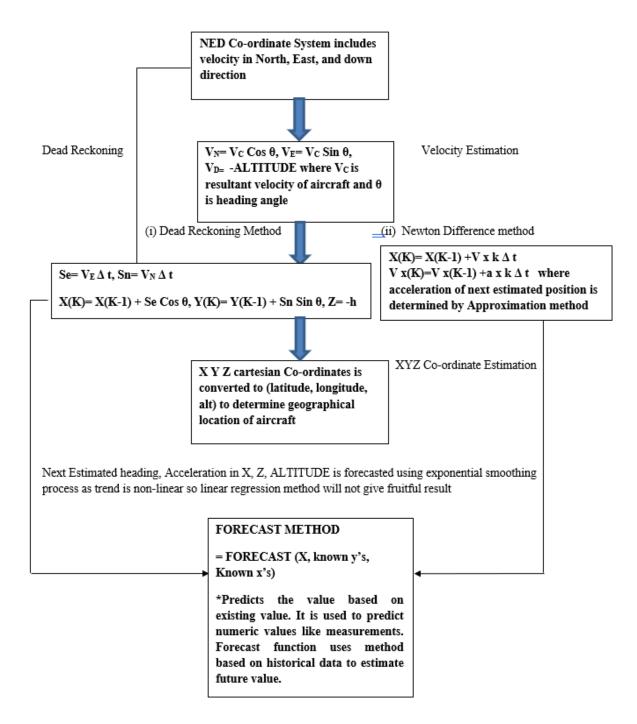
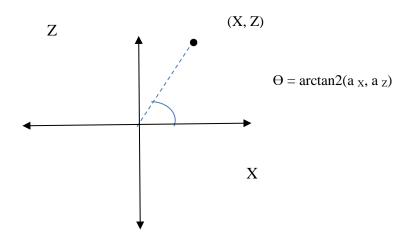


Fig 6.3 RoadMap for geodetic co-ordinate Estimation

STEP1: Heading angle is calculated using formulae ATAN2  $(a_x, a_z)$  as shown in Figure 6.4 where the initial value of  $(a_x, a_z)$  is fetched from flight data refer to (Appendix D3) for forecast prediction.



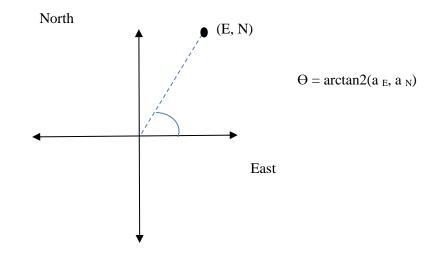
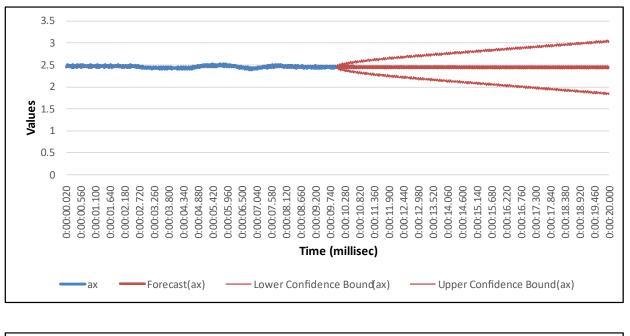
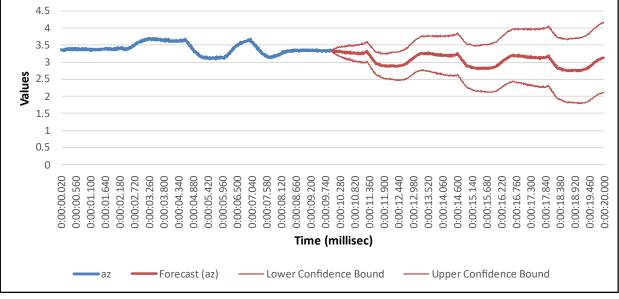


Fig 6.4 NED Coordinate System

A forecast sheet is used in Excel to predict the future value of the heading based on existing value. The flight test of Hansa-III aircraft with a time interval of 10 sec is gathered using a data acquisition system. X-axes resemble Time in (millisec) and Y-axes state the value of acceleration in the X-direction. The blue line in the below figure indicates real flight data and bold red line as forecast value and the light red line as lower and upper bounds of the ax.





X-axes resemble Time in (milli-sec) and Y-axes state the value of acceleration in the Z direction, the blue line in the above figure indicates real flight data and bold red line as forecast value, and the light red line as lower and upper bounds of az.

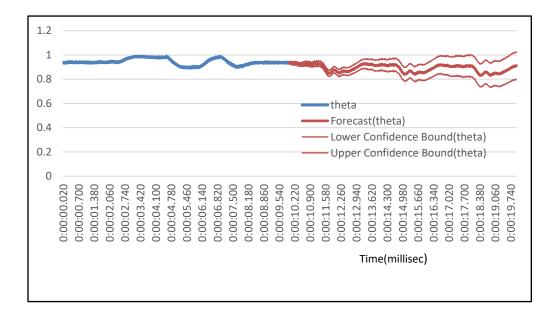


Fig 6.5 Forecast of Acceleration X, Z, and Heading angle

X-axes resemble Time in (milli-sec) and Y-axes state the value of the heading angle in radians where red lines in the curve depict the forecasted heading angle in Fig 6.5. The upper, and lower bounds explain the maximum, and minimum range of the heading angle.

STEP2: Dead Reckoning algorithm used to determine XYZ co-ordinates

$$\begin{split} V_N &= V_C \cos \theta, \, S_N = V_N * \Delta t \\ V_E &= V_C \sin \theta, \, S_E = V_E * \Delta t \\ V_{D=} - Altitude \\ X(K) &= X(K-1) + Se \cos \theta \\ Y(K) &= Y(K-1) + Sn \sin \theta \\ Z &= -h \\ X(K) &= X(K-1) \pm \Delta X \\ Y(K) &= Y(K-1) \pm \Delta Y \\ Z(K) &= Z(K-1) \pm \Delta Z \end{split}$$

STEP3: Conversion of X, Y, and Z Co-ordinate to geodetic Co-ordinate

(Latitude, longitude, and Altitude) using MATLAB code is displayed in Table

6.1 (refer Appendix B7)

The file xyaS2 contains XYZ Cartesian co-ordinates of 10 sec as mentioned in the code

X=xyaS2(:1); Y=xyaS2(:2); Z=xyaS2(:3); X=X {:1}; Y=Y {:1}; Z=Z {:1}; Origin = [80.232293, 26.518886,126.63]; [Lat, Lon] =local2latlon (X, Y, Z, origin); zoom level=12; player = geoplayer (Lat (1), Lon (1), zoom Level); plot Route (player, Lat, Lon);



Fig 6.6 Geographical co-ordinates at Initial phase of Flight test, IIT Kanpur (80.232293, 26.518886, 126.63)

X(T)	Y(T)	LONGITUDE	LATITUDE
0.586526	0.318894	80.2323	26.5189
1.174282	0.636558	80.2323	26.5189
1.759109	0.957151	80.2323	26.5189
2.340916	1.280764	80.2323	26.519
2.92379	1.60331	80.2323	26.519
3.512289	1.920231	80.2323	26.519
4.095947	2.241993	80.2323	26.519
4.678165	2.565195	80.2323	26.519
5.257532	2.891248	80.2323	26.519
5.839366	3.214834	80.2323	26.5191

The tabulated form and graphical representation in form of XY coordinate and longitude, latitude is displayed below

Table 6.1 Conversion XY coordinate to Latitude and Longitude

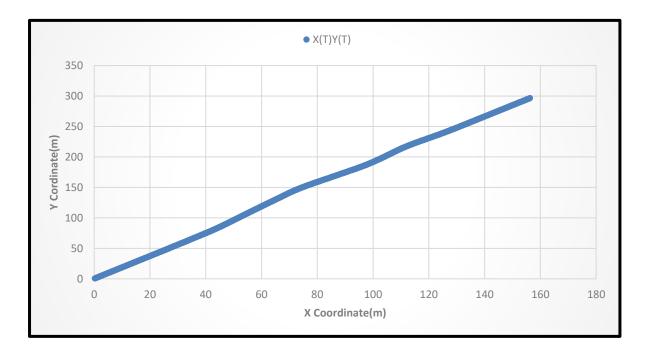


Fig 6.7 Forecasted Value of X, Y Aircraft Coordinates using DR

X-axes resemble X coordinates in (m) and Y axes state the value of Y coordinates in (m) in Fig 6.7. The blue line in the above figure indicates the XY

coordinate of the aircraft for the next 10 sec.

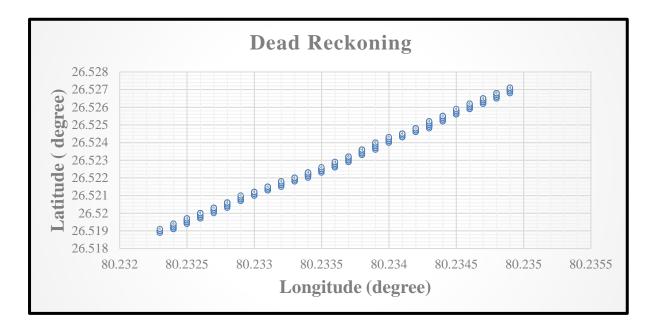


Fig 6.8 Forecasted Value of Longitude, Latitude in degrees using DR

Fig 6.8 axes resemble Longitude in (degrees) and Y axes state value of Latitude in (degrees). The blue line in the above figure indicates the aircraft position for the next 10 sec in form of (Longitude, Latitude)

## **6.2 NEWTON DIFFERENCE**

This equation predicts the current location based on a previously determined equation in the discrete-time interval which is the concept of the dead reckoning approach.

The Inertial Measurement Unit includes an accelerometer that measures 3-axis translational  $a_x$ ,  $a_y$ ,  $a_z$ . The gyroscope measures 3-axis rotational p, q, and r values, and the air data sensor measures airspeed. Refer to Appendix D3. The acceleration of the object is the time rate of change of the body's momentum, according to Newton's second law of motion.

$$\frac{dV_x}{dt} = a_x , \frac{V_x(t+\Delta t) - V_x(t)}{\Delta t} = a_x , V_x(t+\Delta t) = V_x(t) + a_x \Delta t$$

$$X(K) = X(K-1) + V_x(k) * \Delta t$$

$$V_x(K) = V_x (K-1) + a_x(k) * \Delta t$$

$$c(K) = z(K-1) + V_z(k) * \Delta t$$

$$6.5$$

$$V_{z}(K) = V_{z}(K-1) + a_{z}(k)^{*}\Delta t$$
 6.6

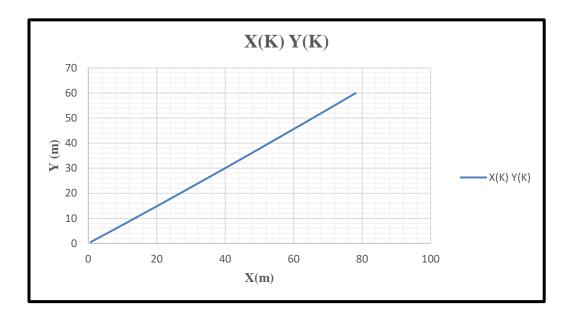
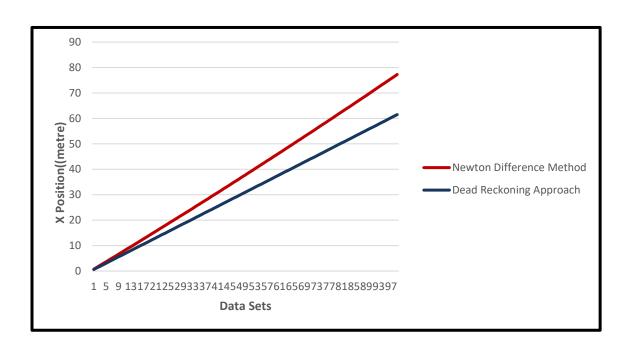


Fig 6.9 Forecasted Value of X, Y Aircraft coordinates using Newton-Difference Method

X-axes resemble X coordinates in (m) and Y-axes state the values of Y coordinates in (m). The blue line in figure 6.9 indicates XY coordinate of the

aircraft for the next 10 sec using newton-difference formulae



# Comparison of Dead Reckoning and Difference formulae in terms of X, Y Coordinates

Fig 6.10 Comparison of Forecasted Value of X Position of aircraft using DR and Newton-Difference Method

X-axes resemble 100 datasets and Y-axes state value of X coordinates in (m). The blue line and red line in figure 6.10 indicate the X position of the aircraft for the next 10 seconds using the DR and Newton Difference method.

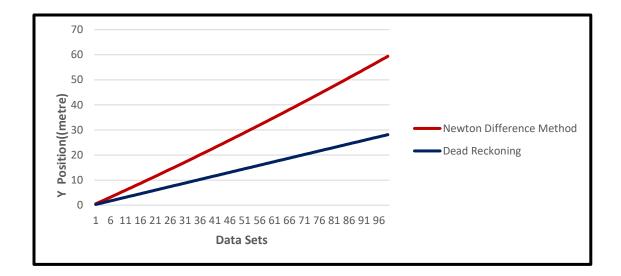
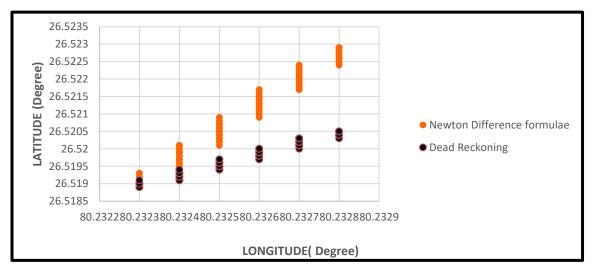
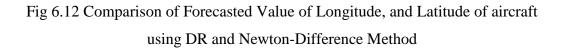


Fig 6.11 Comparison of Forecasted Value of Y Position of aircraft using DR and Newton-Difference Method

X-axes resemble 100 datasets and Y-axes state the values of Y coordinates in (m). The blue line and red line in above figure 6.11 indicate the Y position of the aircraft for the next 10 seconds using the DR and Newton Difference method







X-axes resemble Longitude in (degrees) and Y-axes state the value of Latitude in (degrees). The black line and orange line in above figure 6.12 indicate (the longitude and latitude) of the aircraft for the next 10 seconds using the DR and Newton Difference method.

LONGITUDE (N.D)	LATITUDE (N.D)	LONGITUDE (D.R)	LATITUDE (D.R)	%Error (LON)	%Error (LAT)
80.2323	26.519	80.2323	26.5189	0	-0.00038
80.2323	26.5193	80.2324	26.5191	0.000125	-0.00075
80.2324	26.5201	80.2325	26.5194	0.000125	-0.00264
80.2325	26.5208	80.2326	26.5197	0.000125	-0.00415
80.2326	26.5217	80.2327	26.52	0.000125	-0.00641
80.2328	26.5224	80.2327	26.5203	-0.00012	-0.00792

Table 6.2: Estimation of Percentage Error

It is found that there is a slight variation in the values of latitude but the values of longitude are quite similar for both techniques. The percentage error is quite small for longitude and latitude as shown in Table 6.2

## **6.3 VALIDATION**

Statistical Technique in Time Series for validating the result using the Dead Reckoning approach is discussed below:

**Exponential smoothing** is used to study trend analysis of the non-linear irregular patterns of aircraft location. The Longitude of the next 5 sec is forecasted in the below section using exponential smoothing time series analysis. The exponential smoothing formulae

$$F_t = \alpha . M_{t-1} + (1 - \alpha) F_{t-1}$$
 6.7

 $\alpha$  is the smoothing constant which lies in the range  $0 \le \alpha \le 1$ ;  $F_t$  is the forecasted value for time t;  $F_{t-1}$  is the previous forecasted value for time (t-1);  $M_{t-1}$  is the previously measured value of the physical quantity that needs to be forecasted at the time (t-1). It is also expressed in term of Damping factor as  $\zeta = 1 - \alpha$ ;  $\zeta = 0.7$  as calculated by (JAISWAL & PRAKASH, 2022)

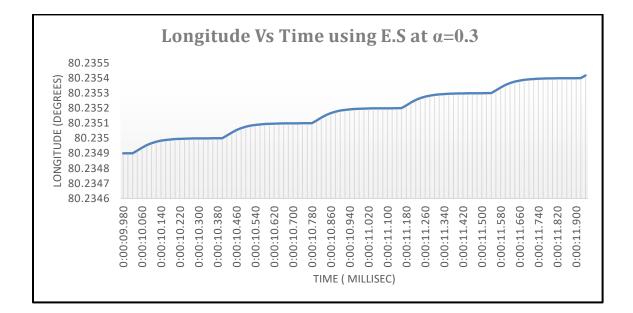


Fig 6.13: Forecasted Value of Longitude using Exponential Smoothing Technique

The Longitude of Fig 6.13 of the next 10 sec is forecasted in the above section using exponential smoothing time series analysis for  $\alpha=0.3$ 

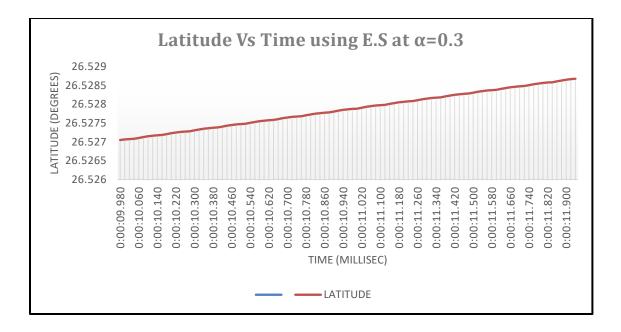


Fig 6.14 Forecasted Value of Latitude using Exponential Smoothing Technique

The Latitude of Fig 6.14 of the next 10 sec is forecasted in the above section using exponential smoothing time series analysis for  $\alpha$ =0.3

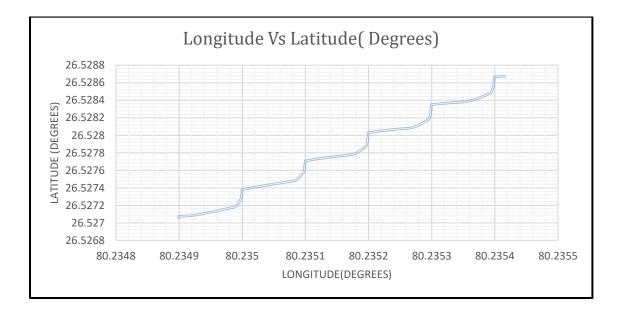


Fig 6.15 Forecasted Value of Longitude, Latitude in degrees using Exponential Smoothing Technique

The Longitude and Latitude of the next 10 sec are forecasted in the below section using exponential smoothing time series analysis for  $\alpha$ =0.3 and results are compared with Newton Difference and Dead Reckoning.

Dead Reckoning		Newton Difference		Exponential Smoothing alpha 0.3	
LONGITUDE	LATITUDE	LONGITUDE	LATITUDE	LONGITUDE	LATITUDE
80.2323	26.5189	80.2323	26.5189	80.2323	26.519
80.2323	26.5189	80.2323	26.519	80.2323	26.519
80.2323	26.5189	80.2323	26.519	80.2323	26.519
80.2323	26.519	80.2323	26.519	80.2323	26.519
80.2323	26.519	80.2323	26.5191	80.2323	26.519
80.2323	26.519	80.2323	26.5191	80.2323	26.519
80.2323	26.519	80.2323	26.5192	80.2323	26.519
80.2323	26.519	80.2323	26.5192	80.2323	26.519
80.2323	26.519	80.2323	26.5192	80.2323	26.519
80.2323	26.5191	80.2323	26.5193	80.2323	26.519
80.2324	26.5191	80.2323	26.5193	80.2323	26.519
80.2324	26.5191	80.2324	26.5194	80.2324	26.519
80.2324	26.5191	80.2324	26.5194	80.2325	26.519
80.2324	26.5191	80.2324	26.5194	80.2325	26.519
80.2324	26.5191	80.2324	26.5195	80.2325	26.519
80.2324	26.5192	80.2324	26.5195	80.2325	26.519
80.2324	26.5192	80.2324	26.5195	80.2325	26.519
80.2324	26.5192	80.2324	26.5196	80.2325	26.519
80.2324	26.5192	80.2324	26.5196	80.2325	26.519
80.2324	26.5192	80.2324	26.5197	80.2325	26.519
80.2324	26.5192	80.2324	26.5197	80.2325	26.519
80.2324	26.5193	80.2324	26.5197	80.2325	26.520
80.2324	26.5193	80.2324	26.5198	80.2325	26.520
80.2324	26.5193	80.2324	26.5198	80.2325	26.520
80.2324	26.5193	80.2324	26.5199	80.2325	26.520
80.2324	26.5193	80.2324	26.5199	80.2325	26.520
80.2324	26.5193	80.2324	26.5199	80.2325	26.520
80.2324	26.5194	80.2324	26.52	80.2325	26.520
80.2324	26.5194	80.2324	26.52	80.2325	26.520
80.2325	26.5194	80.2324	26.5201	80.2325	26.520
80.2325	26.5194	80.2324	26.5201	80.2325	26.520
80.2325	26.5194	80.2325	26.5201	80.2326	26.520
80.2325	26.5194	80.2325	26.5202	80.2326	26.520
80.2325	26.5195	80.2325	26.5202	80.2326	26.520

80.2325	26.5195	80.2325	26.5203	80.2326	26.520
80.2325	26.5195	80.2325	26.5203	80.2326	26.520
80.2325	26.5195	80.2325	26.5203	80.2326	26.520
80.2325	26.5195	80.2325	26.5204	80.2326	26.520
80.2325	26.5195	80.2325	26.5204	80.2326	26.520
80.2325	26.5196	80.2325	26.5205	80.2326	26.520
80.2325	26.5196	80.2325	26.5205	80.2326	26.520

Table 6.3: Comparison of values of Longitude, Latitude using ExponentialSmoothing, Newton Difference Method, and Dead Reckoning Technique

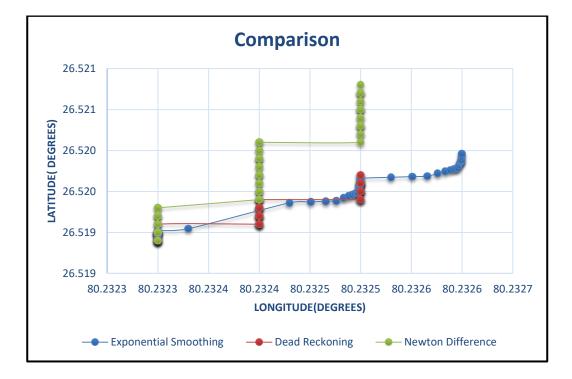


Fig 6.16 Graphical Representation of Longitude, Latitude using (D.R, ES, ND)

In contrast to the latitude of Newton difference, which is fairly distant from DR and ES, the values of longitude and latitude of dead reckoning superimpose with exponential smoothing in figure 6.16 given. As a consequence, exponential smoothing supports the outcome obtained through DR methodology. The latitude and longitude error percentages are seen to be quite low, which strongly supports the geodetic navigational conclusion.

## SUMMARY

The Dead Reckoning algorithm is used in this chapter to forecast Hansa-III's current location based on its prior location over elapsed time on estimated speed. The Newton-Difference method and Exponential Smoothing Technique are used to compare and validate the Dead Reckoning data in the form of longitude, latitude, and altitude.

# CHAPTER-7

# **CONCLUSION AND FUTURE WORK**

An autopilot is a system that controls the vehicle trajectory without manual controls. The research work emphasizes the parameter estimation of research cum trainer aircraft along with the autopilot design for pitch control of the aircraft in addition to the Integration of the Dead Reckoning approach to estimate the position of Hansa-III Aircraft for future prediction.

There is a lot of research on parameter estimation. A large researcher focused their work on parameter estimation by estimating parameters using several methodologies including OEM, FEM, and EEM, however, the study expanded not only in the parameter estimation area but also on the application side. To make the study stand out, the research effort has been expanded by constructing a pitch controller and putting a revolutionary navigational dead-reckoning approach into practice.

The methodology adopted for Parameter Estimation is Maximum likelihood and an observation is made that Aerodynamic derivative values derived with ML are fairly accurate and close to W.T values for most datasets. There is a maximum deviation in the values from Wind Tunnel result in the case of pulse Input as compared to Multi-step and Doublet thus Multi-step elevator control input is more consistent as compared to different elevator Inputs.

In the context of attitude control design in longitudinal motion, aircraft is modelled and a state-space representation of the system is developed, controllers are designed on MATLAB environment using Control System Toolbox thus performances in Time and Frequency domain using different techniques such as Root-Locus, Pole-Placement, Linear Quadratic Regulator are analysed and compared by setting some design specifications.

In this thesis, the simulation results obtained using root-locus, pole-placement and LQR illustrate and conclude that the LQR controller settles rapidly as Ts is 0.44s as compared to pole-placement with excellent property of eliminating steady-state error to zero which justifies robust-free, good performance characteristics, the efficiency of the controller against disturbances.

It is observed that no research paper is been published related to the navigation of Hansa-III henceforth, the dead reckoning navigational technique will be implemented to study the attitude, and orientation of the system so that it can be used for surveillance in terrain-prone areas, aerial photography, monitoring of floods/droughts.

The study incorporates the implementation of the navigational approach to estimate aircraft position. The result of the Dead Reckoning approach is compared with exponential smoothing in the form of longitude, and latitude and concludes that the percentage error of Longitude, and latitude is found to be very less which validates the result dominantly. Integration Dead Reckoning and Designing autonomous control system of Hansa-III singularize the work and make study novel.

## **FUTURE SCOPE**

The future prospects of the research on the basis of design techniques developed in this study are outlined as:

1. Parameter Estimation of an Aircraft in a non-linear state is beyond the

range of this study so the Neural Gauss-Newton method may be applied to consider non-linear aerodynamics. NGN will be more effective than ML for stall conditions, and unsteady states.

- Non-linear MIMO Systems for controller design are beyond the scope of the research study. The proposed controller applies to SISO linear, timevariant systems.
- An extension of the research work to design the attitude controllers (roll, Yaw) in lateral directional motion.
- 4. The proposed methodology to use neural networks and fuzzy logic can be extended to integrate flexibility, and the accuracy of the controller. Fuzzy logic handle system and measurement noise effectively hence considered for future application as signal processing, control system, structural health monitoring, fault-tolerant detection control system, and monitoring of environmental disasters. System Identification of Gallinaceous machines, and electric flying cars such as urban air mobility (UAM) creating new opportunities in transport engineering that need to be investigated in future(Postorino & Sarné, 2020).
- One more extension of the research study is the incorporation of different types of aircraft as this study involves the research trainer aircraft, Hansa-III.
- 6. Fuzzy logic effectively handles system and measurement noise; as a result, it is being explored for use in the future in areas such as signal processing, control systems, monitoring structural health, fault-tolerant detection controls, and environmental disaster monitoring.

# **CHAPTER-8**

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# **APPENDIX-** A

# **CURRICULUM VITAE**

# ROLI JAISWAL

ADDRESS: 543/22, Antarick Complex, Badamtala, Barrackpore

P.O. Bengal Enamel, N-24 Paragana West Bengal. EMAIL: rolijais89@gmail.com

MOB: 8954686133, 9123867571



Roli is a Research Scholar with 6.5 years of teaching and Industrial experience. Her ambition is to Pursue a challenging career and be a part of progressive organization that gives scope to enhance skills, knowledge and to reach pinnacle in this field with sheer determination, hard work and dedication so that her experience can beutilized and makes good use of for the organization.

#### Subjects comfortable to teach incudes:

Control Systems System Identification: Includes Kalman Filtering, ML Approaches etc.Fluid Mechanics Flight Mechanics Aircraft Systems and Maintenance

#### **Publication Summary:**

- "A preliminary study of parameter estimation for fixed wing aircraft and high endurability parafoil AerialVehicle", INCAS Bulletin, Vol-12, Issue-4, SCOPUS Indexed, Dec2020
- "Classical and Modern gain estimation approach of PID Controller for the pitch control of the RCTAAircraft", INCAS Bull., vol. 14, no. 1, pp. 39-56, 2022, Doi: 10.13111/2066-8201.2022.14.1.4
- "Estimation of Lateral Directional Aerodynamic Derivatives from Flight Data of Unmanned Poweredparafoil Aerial Vehicle", Proceedings of the AIAA Atmospheric Flight Mechanics Conference,2018

- "Vishkira, A Gallinacious aircraft", in International Conference of Material Science and Testing, China, 2019
- "Comparative study of longitudinal stability derivatives of Hansa-3 Aircraft Using Extended kalman Filtering Technique and ML Method" in Advances in Chemical Engineering, SCOPUS Indexed, Dehradun, Feb 2020.
- "Distinctive Navigational Approach –A Dead Reckoning for Aircraft Co-Ordinate Estimation", 4th International Conference on Smart and Sustainable Developments in Engineering and Technology, PiCET, 22nd May 2022

#### **Competencies and Academic Administrative Summary:**

- MIS Coordinator of Aerospace Department.
- Class- Coordinator of B-Tech Second Year students.
- Guided M-Tech graduates of UAV Program in thesis writing, major projects.
- Coordinator for Industrial Visit in ISRO, ADANI, & Bharat Dynamics Limited in Hyderabad for 2019.
- Coordinator for Industrial Visit in HAL, NAL & DRDO in Bangalore for 2018.
- Mentor-Mentee Coordinator of Second and Third Year.
- Member of Organizing committee in National Space Convention 2020: Tessy Thomas, Missile Women ofIndia was distinguished guest of the Convention.
- Summer Internship Coordinator of B-Tech Graduates.
- Technical and organizing support to students for Aero Kriti Competition.

#### Accreditation & Ranking Summary:

- Preparation of Criterion wise fie related to teaching learning process for NAAC.
- Curriculum Design and Development and addition of value-added courses for NAAC.
- Teaching & Learning process definition, implementation and impact analysis for NAAC.
- Outcome based Education System study and generation of report for NAAC.
- PPT preparation for NAAC.

#### Accomplishments:

- B-tech students in their major and minor projects.
- Helping hand of placement coordinator departmental wise in UPES
- Member of "Aeronautical society of India".
- Organized a national level seminar on "Recent trends in Aerospace Technology".
- Technical and organizing support for engineering Events as "AERO-SAMBHODHAN" at BBDNITM,Lucknow in UTKARSH.
- Astronomy (Member of UPAAC, Lucknow)
- Participated in Workshop on "Fundamentals of robotics" from 20-10-2008 to 22-10-2008.

#### Organization:

Organization	Designation	Duration
University of Petroleum& Energy studies, Dehradun	Assistant Professor	14 <sup>th</sup> Aug 2017- 4 <sup>th</sup> Sep 2020
DBU University, Punjab	Technical Assistant	Sep 2015 to June 2017
BBDNITM, Lucknow	Lecturer	Dec 01, 2014 to Sep 2015.
HAL, Kanpur	Design Trainee	1 <sup>st</sup> Jan 2013 to 31 <sup>st</sup> Dec 2013

#### Education:

Qualification	Year of Passing	Institute/ University	Class/Division	Percentage/DGPA
PhD	2018 (Pursuing)	UPES, Dehradun	-	-
M-TECH	2017	DBU, Punjab	First Class with Distinction	81.1%
B-TECH	2012	BBDNITM, Lucknow	First Division with Honors	80%
12тн	2007	C.B.S. E	First Class	67.7%
10 <sup>th</sup>	2005	C.B.S. E	First Class	77.8%

#### **Project Experience:**

## 1. <u>Involved in a project on comparison and analysis of AVRO class TURBO</u> <u>PROP Engine.</u>

Details: Study of AVRO class of ROLLS ROYCE DART Engine characteristics and comparisons with some suitable engines like PRATT& WHITNEY CANADA - PW123AF, PW124B, PW125B PW127Eand KLIMOV COOPERATION, RUSSIA –TV7-117S, TV7-117S SERIES2 to find out engine with better SFC and Performance.

Conclusion: TV7-117S SERIES2 (RUSSIAN) Engine can replace ROLLS ROYCE Dart533-2.

- SFC is reduced which helps in saving fuel cost.
- Low engine weight.
- About 300 crores is being saved per 200 hours.

## 2. <u>Involved in a project on aircraft material standards (from German std. to</u> <u>British, Italy, France, and USA) of aircraft parts.</u>

• It helps in comparing & finding the substitute of parts of aircraft material.

3. <u>Optimization of Aerofoil</u> (Symmetrical, cambered) by analytical method on selection of series of Aerofoilsby JAVAFOIL Software from IIT, Kanpur

**Personal Details:** 

Date of Birth	03.11.1990
Pan card No.	AUCPJ1037E
Gender	Female
Marital Status	Married
Nationality	Indian
Language Known	English, Hindi, Bangla
Hobbies	Cooking, Travelling

# **APPENDIX-B**

# MATLAB CODES

## **B1. ZIEGLER NICHOLAS METHOD**

%% Zieger nicholas method clear all clc

%Define plant transfer function G\_NUM=[0 0 0 55.94 103.3]; G\_DEN=[1 10.07 31.18 101.8 103.3]; KU=1.34; %% ROUTH HURWITZ CRITERION TU=1.504; %% SIMULINK BLOCK DIAGRAM %% LOOK THE VALUE OF KP, Ti, Td KP=0.6\*KU; % CLASSIC PID Ti=0.5\*TU; % CLASSIC PID Td=TU/8: % CLASSIC PID %% COMPUTE Ki and Kd Ki=1.2\*KU/TU; % CLASSIC PID Kd=0.075\*KU\*TU: % CLASSIC PID %%COMPUTE Ki and Kd Kp=0.45\*KU; % PI CONTROLLER ti=TU/1.2; %PI CONTROLLER %% COMPUTE Ki ki=054\*KU/TU; %PI CONTROLLER %% unstable characteristics using PI CONTROLLER IN SIMULINK B/D %%%% COMPUTE Kd FOR PD CONTROLLEr kp=0.8\*KU; td=TU/8;kd=0.1\*KU\*TU; %% STABLE CHARACTERISTICS USING PD CONTROLLER IN SIMULINK B/D

#### **B2.MODIFIED ZIEGLER NICHOLAS METHOD**

%% Modified Zieger nicholas method clear all

clc %Define plant transfer function G\_NUM=[0 0 0 55.94 103.3]; G\_DEN=[1 10.07 31.18 101.8 103.3]; KU=0.3; %% ROUTH HURWITZ CRITERION TU=1.873; %% SIMULINK BLOCK DIAGRAM %% LOOK THE VALUE OF KP, Ti, Td KPmzn=0.33\*KU; % CLASSIC PID %% COMPUTE Ki and Kd Kimzn=0.5\*TU; % CLASSIC PID Kdmzn=0.33\*TU; % CLASSIC PID

## **B3. ASTROM- HAGGULUND METHOD**

%% Astrom-Haggulund method clear all clc %Define plant transfer function G\_NUM=[0 0 0 55.94 103.3]; G\_DEN=[1 10.07 31.18 101.8 103.3]; KU=0.3; %% ROUTH HURWITZ CRITERION TU=1.873; %% SIMULINK BLOCK DIAGRAM %% LOOK THE VALUE OF KP, Ti, Td Kpag=0.33\*KU; % CLASSIC PID %% COMPUTE Ki and Kd KIag=0.94\*TU; % CLASSIC PID KDag=0; % CLASSIC PID

## **B4. TYREUS LUYBEN METHOD**

%% Tyreus luyben method clear all clc %Define plant transfer function G\_NUM=[0 0 0 55.94 103.3]; G\_DEN=[1 10.07 31.18 101.8 103.3]; KU=1.3400; %% ROUTH HURWITZ CRITERION TU=1.5040; %% SIMULINK BLOCK DIAGRAM %% LOOK THE VALUE OF KP, Ti, Td Kpcl=0.3125\*KU; % CLASSIC PID %% COMPUTE Ki and Kd KIcl=2.2\*TU; % CLASSIC PID KDcl=0.158\*TU; % CLASSIC PID

#### **B5. POLE- PLACEMENT ALGORITHM**

clc % define state and control matrices A= [-1.851 0.8207 0;-4.403 -2.01 0;0 1 0]; B= [0.00562;8.95;0];  $C = [0 \ 0 \ 1];$ D=[0]; initialX = [1;0;0];% create state space object sys=ss(A,B,C,D); %CHECK OPEN LOOP EIGEN VALUES E = eig(A)% % desired closed loop poles using butterworth polynomial equation P= [-1.35+2.338i -1.35-2.338i -1.3]; % % solve for K using pole placement GainK = acker(A,B,P);disp('Feedback Gain Matrix: '); disp(GainK); % OR USE place to determine closed loop system gain % GAIN= place(A,B,P) % %CHECK for closed loop eigen values Acl= A-B\*GainK; Ecl = eig(Acl)% % % create closed loop system syscl= ss(Acl,B,C,D); % %CHECK STEP RESPONSE step(0.2\*syscl) %solve for kr kdc= dcgain(syscl); kr=1/kdc % % % create scaled input closed system syscl\_scaled = ss(Acl,B\*kr,C,D); step(syscl\_scaled) %ylabel('pitch angle (rad)'); title('Closed-Loop Step Response: pole placement');

#### **B6. LINEAR QUADRATIC REGULATOR**

A= [-1.851 0.8207 0 -4.403 -2.01 0 0 1 0 ]; B= [0.00562;8.95;0]; C= [0 0 1]; D= [0]; poles= eig(A) %% poles lies in complex left side of the plane hence system is stable % poles = %% 0.0000 + 0.0000i%%-1.9305 + 1.8993i %%-1.9305 - 1.8993i rank(ctrb(A,B)); rank(obsv(A,C)); p = 400;Q = p \* C \* C;R = 1; [K] = lqr(A,B,Q,R) $sys_cl = ss(A-B*K, B, C, D);$ step(0.2\*sys\_cl); ylabel('pitch angle (rad)'); title('Closed-Loop Step Response: LQR'); % p = 400; % Q = p\*C'\*C;% R = 1: % [K] = lqr(A,B,Q,R); % Nbar = rscale(A,B,C,D,K) % sys\_cl = ss(A-B\*K,B\*Nbar,C,D) % step(0.2\*sys\_cl); % ylabel('pitch angle (rad)'); % title('Closed-Loop Step Response: LQR with Precompensation');

## **B7. CARTESIAN COORDINATES TO GEODETIC COORDINATES CONVERSION CODE**

X=xyaS2(:,1); Y=xyaS2(:,2); Z=xyaS2(:,3); X=X{:,1}; Y=Y{:,1}; Z=Z{:,1}; % Y=double(Y'); % Z=double(Z'); origin= [80.232293,26.518886,126.63]; [lat,lon]=local2latlon(X,Y,Z,origin); % save latlon\_rad.txt zoomlevel=12; player = geoplayer(lat(1),lon(1),zoomLevel); plotRoute(player,lat,lon);

#### **APPENDIX – C**

#### **C.1 EQUATIONS OF MOTION**

A stationary aircraft uses an earth axes system also termed an inertial frame of reference for deriving the equation of motion in an inertial reference frame.

Expression of Newton's second law of motion:

$$\sum \vec{F} = \frac{d}{dt} m \vec{v}$$
C.1

$$\sum \vec{M} = \frac{d}{dt} (\vec{H})$$
C.2

Where F, M, H, m, and v are the net force components (aerodynamic, structural, propulsive, gravitational), net Moment, angular momentum, the mass of the aircraft, and velocity.

Force equation in X, Y, and Z direction is expressed as follows:

$$\overrightarrow{F_x} = \frac{d}{dt} (m \overrightarrow{u})$$
C.3

$$\overrightarrow{F_y} = \frac{d}{dt}(m\vec{v})$$
C.4

$$\vec{F_z} = \frac{d}{dt} (m\vec{w})$$
C.5

where *u*, *v*, and *w* are the components of forces in X, Y, Z directions respectively. Similarly, the moment equation is expressed as:

$$\vec{L} = \frac{d}{dt} \overrightarrow{(H_x)}$$
C.6

$$\vec{M} = \frac{d}{dt} \overrightarrow{(H_y)}$$
C.7

$$\vec{N} = \frac{d}{dt} \overrightarrow{(H_z)}$$
C.8

where *L*, *M*, and *N* are the rolling moment, pitching moment, yawing moment and  $H_x$ ,  $H_y$ ,  $H_z$  refers to angular momentum in X, Y, and Z directions. Consider  $\delta$  m as the elemental mass of the airplane, v is the velocity in an inertial frame of reference, and  $\delta$  F stands for net force acting on  $\delta$ m thus

$$\vec{F} = \sum \delta F$$
 and  $\delta \vec{F} = \delta m \frac{d \vec{V}}{dt}$  C.9

Thus the velocity of elemental mass  $\delta$  m is

$$\vec{v} = \vec{(v_c)} + \frac{d\vec{r}}{dt}$$
C.10

Where  $v_c$  refers to the velocity of the center of mass and  $\frac{d\vec{r}}{dt}$  stands for velocity for the center of mass. Now substituting equation (3.10) into (3.9) yields

$$\vec{F} = \sum \delta F = \frac{d}{dt} \sum \left( \vec{v_c} + \frac{d\vec{r}}{dt} \right) \delta m$$
 C.11

$$\vec{F} = m \, \frac{d\vec{v_c}}{dt} + \frac{d}{dt} \sum \frac{d\vec{r}}{dt} \,\delta \,m \tag{C.12}$$

$$\vec{F} = m \, \frac{d\vec{v_c}}{dt} + \frac{d^2}{dt^2} \sum r \delta \, m \tag{C.13}$$

Where r is the position vector measured from the center of mass thus  $\sum r \delta m$  is zero and the new force equation formulated as

$$\vec{F} = m \, \frac{d\vec{v_c}}{dt} \tag{C.14}$$

Similarly rewriting moment equation 3.2 as the force equation as

$$\delta \vec{M} = \frac{d}{dt} \,\delta \vec{H} \tag{C.15}$$

Where M is the moment and H is angular momentum. H is written in vector form as

$$\vec{H} = \vec{r} \times \vec{p}$$
 and  $\delta \vec{H} = (\vec{r} \times \vec{v}) \,\delta m$  C.16

Now substituting the value of  $\delta \vec{H}$  from equation 3.16 to 3.15 and written as

$$\delta \vec{M} = \frac{d}{dt} \left( \vec{r} \times \vec{v} \right) \delta m \tag{C.17}$$

The velocity of elemental mass can be expressed in form of position vector 'r' in an inertial frame of reference as

$$\vec{v} = (v_c) + \frac{d\vec{r}}{dt} + (\vec{\omega} \times \vec{r})$$
C.18

Where  $v_c$  refers to the velocity of the center of mass,  $\frac{d\vec{r}}{dt}$  stands for velocity for the center of mass,  $\vec{\omega}$  is the angular velocity of the aircraft, and  $\vec{r}$  as position vector of elemental mass. The net moment can be expressed by substituting the value of equation 3.18 to 3.16 as

$$\vec{H} = \sum \delta \vec{H} = \sum r \delta m \times v_c + \sum [r \times (\vec{\omega} \times \vec{r})] \delta m \qquad C.19$$

The first term of equation  $3.19 \sum r \delta m$  is substituted as zero as r is the position vector measured from the center of mass. Now the equation is reduced to

$$\vec{H} = \sum [\vec{r} \times (\vec{\omega} \times \vec{r})] \,\delta m \qquad C.20$$
  
Where  $\vec{r} = x\hat{\imath} + y\hat{\jmath} + z\hat{k}$ 

 $\overrightarrow{\omega} = p\hat{\imath} + q\hat{\jmath} + r\hat{k}$ 

Solving equation 3.20 using  $\vec{r}$ ,  $\vec{\omega}$  is expressed as

$$(\vec{\omega} \times \vec{r}) = \begin{bmatrix} \hat{\imath} & \hat{\jmath} & \hat{k} \\ p & q & r \\ x & y & z \end{bmatrix}$$
$$(\vec{\omega} \times \vec{r}) = \hat{\imath}[qz - ry] - \hat{\jmath}[pz - xr] + \hat{k}[py - qx] \qquad C.21$$
$$[\vec{r} \times (\vec{\omega} \times \vec{r})] = \begin{bmatrix} \hat{\imath} & \hat{\jmath} & \hat{k} \\ x & y & z \\ qz - ry & xr - pz & py - qx \end{bmatrix}$$
$$= \hat{\imath}[py^2 - qxy - rxz + pz^2] - \hat{\jmath}[pxy - qx^2 - qz^2 + ryz] + \hat{k}[px^2 - pzx - qyz + ry^2]$$

Substituting the above equation in equation no (3.20) to get moment equations in X, Y, and Z direction

$$H_x = p \sum (y^2 + z^2) \,\delta m - q \sum xy \,\delta m - r \sum xz \delta m \qquad C.22$$

$$H_{y} = q \sum (x^{2} + z^{2}) \,\delta m - p \sum xy \,\delta m - r \sum yz \delta m \qquad C.23$$

$$H_z = r \sum (x^2 + y^2) \,\delta m - q \sum yz \,\delta m - p \sum xz \delta m \qquad C.24$$

The moment and product of inertia of aircraft are defined in the below section:

$$I_{x} = \iiint (y^{2} + z^{2}) \delta m \qquad \qquad I_{xy} = \iiint (xy) \delta m$$
$$I_{y} = \iiint (x^{2} + z^{2}) \delta m \qquad \qquad I_{xz} = \iiint (xz) \delta m \qquad \qquad C.25$$
$$I_{z} = \iiint (x^{2} + y^{2}) \delta m \qquad \qquad I_{yz} = \iiint (yz) \delta m$$

Where  $I_x$ ,  $I_y$ ,  $I_z$  are the mass moment of inertia of the system in x, y, and z directions respectively. While substituting equation 3.23 in equation 3.22 the moment of momentum equation is expressed as

$$H_x = pI_x - qI_{xy} - rI_{xz}$$
C.26

$$H_y = qI_y - pI_{xy} - rI_{yz}$$
C.27

$$H_z = rI_z - qI_{yz} - pI_{xz}$$
C.28

# C.2 Transformation of equations in a rotational frame from an inertial frame of reference

The vector identity used to transform the inertial frame of reference to the body fixed frame of reference is represented as:

$$\left|\frac{dA}{dt}\right|_{IF} = \left|\frac{dA}{dt}\right|_{BF} + \omega \times A \tag{C.29}$$

Where  $\omega$  is the angular velocity of vector A, IF is the inertial frame of reference, and BF is the body-fixed frame of reference. The identity applied to an aircraft for axes transformation is written as:

$$\vec{F} = m \left| \frac{dV_C}{dt} \right|_{BF} + m \left( \omega \times V_C \right)$$
C.30

$$\vec{M} = \left| \frac{d\bar{H}}{dt} \right|_{BF} + (\omega \times H)$$
 C.31

Solving the equations 3.26 and 3.27 to deduce force and moment equations in scaler form is represented as

$$V_c = u\,\hat{\imath} + v\,\hat{\jmath} + w\,\hat{k} \tag{C.32}$$

$$\vec{\omega} = p\hat{\imath} + q\hat{\jmath} + r\hat{k}$$
C.33

$$(\omega \times V_C) = \begin{bmatrix} \hat{i} & \hat{j} & \hat{k} \\ p & q & r \\ u & v & w \end{bmatrix}$$
C.34

$$(\omega \times V_C) = \hat{\imath}[qw - rv] - \hat{\jmath}[pw - ur] + \hat{k}[pv - qu]$$
C.35

The force equations in X, Y, and Z direction while substituting the value of curl  $(\omega \times V_c)$  in below equations are given by

$$F_x = m[\dot{u} + qw - rv] \tag{C.36}$$

$$F_{y} = m[\dot{v} + ru - pw] \tag{C.37}$$

$$F_z = m[\dot{w} + pv - qu] \tag{C.38}$$

The moment equations in X, Y, and Z direction while substituting the value of curl ( $\omega \times H$ ) in equation 3.27 is given by

$$\vec{\omega} = p\hat{\imath} + q\hat{\jmath} + r\hat{k}$$
C.39

$$\vec{H} = H_x \hat{\imath} + H_y \hat{\jmath} + H_z \hat{k}$$
C.40

$$(\omega \times H) = \begin{bmatrix} \hat{\iota} & \hat{j} & \hat{k} \\ p & q & r \\ H_x & H_y & H_z \end{bmatrix}$$
C.41

$$(\omega \times H) = \hat{\imath} [qH_z - rH_y] - \hat{\jmath} [pH_z - rH_x] + \hat{k} [pH_y - qH_x]$$
C.42

Recalling Scaler moment equation 3.24 as discussed in the previous section

$$H_{x} = pI_{x} - qI_{xy} - rI_{xz}$$

$$H_{y} = qI_{y} - pI_{xy} - rI_{yz}$$

$$H_{z} = rI_{z} - qI_{yz} - pI_{xz}$$

$$L = m[\dot{H}_{x} + qH_{z} - rH_{y}]$$

$$M = m[\dot{H}_{y} + rH_{x} - pH_{z}]$$

$$C.44$$

$$N = m[\dot{H}_{z} + pH_{y} - qH_{x}]$$

Substituting the values of  $H_x$ ,  $H_y$ ,  $H_z$  into equation 3.38 to deduce rolling, pitching, and yawing moment along the X, Y, and Z axes and assuming the XZ plane as the symmetry of the airplane thus  $I_{yz} = I_{xy} = 0$ .

The moment equation of an airplane in an XZ plane can be written as

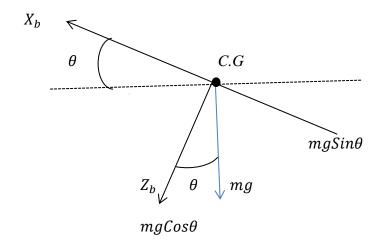
$$L = I_x p - I_{xz} \dot{r} + qr (I_z - I_y) - I_{xz} pq \qquad C.45$$

$$M = I_y \dot{q} + rp(I_x - I_z) + I_{xz}(p^2 - r^2)$$
C.46

$$N = -I_{xz}\dot{p} + I_z\dot{r} + pq(I_y - I_x) + I_{xz}qr$$
C.47

Rewriting Force equation by considering Gravitational, and thrust effects on Aircraft:

Gravitational Force (mg) lies at the center of gravity position of the airplane in body fixed axes as shown in fig1. The resolved components are written as:





By comparing both figures  $F_{y_{gravity}}$ ,  $F_{z_{gravity}}$  can be resolved as shown below

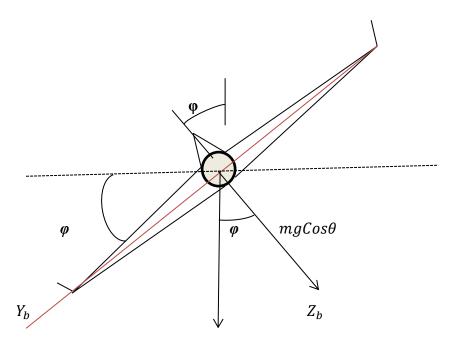


Fig C.1: Components of gravitational force in body axis

 $F_{y_{gravity}} = mgCos\thetaSin\varphi$  C.49

$$F_{z_{aravity}} = mgCos\thetaCos\varphi$$
C.50

The thrust forces acting on an airplane in X, Y, and Z directions can be written as

$$F_{X_T} = X_T$$

$$F_{y_T} = Y_T$$

$$F_{Z_T} = Z_T$$
C.51

The thrust moments acting on an airplane in X, Y, and Z directions can be written as  $L_T$ ,  $M_T$ ,  $N_T$ 

The finalized set of force equations is expressed as:

$$X - mgSin\theta = m[\dot{u} + qw - rv]$$
C.52

$$Y + mgCos\theta Sin\phi = m[\dot{v} + ru - pw]$$
C.53

$$Z + mgCos\thetaCos\phi = m[\dot{w} + pv - qu]$$
C.54

Where X, Y, and Z indicate the net forces (Propulsive force, gravitational force, thrust force, etc) acting in X, Y, and Z direction

$$m\dot{u} = m(rv - qw) + \bar{q}C_X S - mgSin\theta + T$$
C.55

$$m\dot{v} = m(pw - ru) + \bar{q}C_YS + mgCos\thetaSin\emptyset$$
C.56

$$m\dot{w} = m(qu - pv) + \bar{q}C_Z S + mgCos\thetaCos\phi \qquad C.57$$

### **APPENDIX -D**

## GAIN & COORDINATE ESTIMATION

## D1. GAIN ESTIMATION OF CONTROLLERS USING TRADITIONAL APPROACHES ZN, MZN, AH, TL OF DIFFERENT DATASETS

### **D1.1 PID CONTROLLER**

KP -PID								
Data Set	ZN	MZN	AH	TL				
H0	0.618	0.3399	0.3399	0.3219				
H1	0.42	0.231	0.231	0.2188				
H2	0.804	0.4422	0.4422	0.4188				
H3	0.414	0.2277	0.2277	0.2156				
H4	0.588	0.3234	0.3234	0.3063				
H5	0.468	0.2574	0.2574	0.2438				
H6	0.93	0.5115	0.5115	0.4844				
H7	0.162	0.0891	0.0891	0.0844				
H8	2.58	1.419	1.419	1.3438				
H9	0.72	0.396	0.396	0.375				
H10	1.062	0.5841	0.5841	0.5531				
H11	0.402	0.2211	0.2211	0.2094				
H12	2.58	1.419	1.419	1.3438				
HP1	0.522	0.2871	0.2871	0.2719				
HP2	0.528	0.2904	0.2904	0.275				
HD1	0.18	0.099	0.099	0.0938				

KP -PID

Twelve datasets of Multistep Input, one dataset of Doublet Input, and 2 dataset of Pulse Input are used for Proportional gain estimation of PID Controller using traditional approach such as ZN, MZN, AH and TL

KI-PID							
Dataset	ZN	MZN	AH	TL			
HO	0.7774	0.795	1.4946	3.498			
H1	0.4841	0.8675	1.6309	3.817			
H2	1.072	0.752	1.4138	3.3088			

H3	0.5156	0.803	1.5096	3.5332
H4	0.7323	0.803	1.5096	3.5332
H5	0.6671	0.7015	1.3188	3.0866
H6	1.3248	0.702	1.3198	3.0888
H7	0.2017	0.803	1.5096	3.5332
H8	6.45	0.4	0.752	1.76
H9	0.8933	0.806	1.5153	3.5464
H10	1.5128	0.702	1.3198	3.0888
H11	0.4988	0.806	1.5153	3.5464
H12	4.219	0.6115	1.1496	2.6906
HP1	0.582	0.8965	1.6854	3.9446
HP2	0.598	0.883	1.66	3.8852
HD1	0.1922	0.9365	1.7606	4.1206

Twelve datasets of Multistep Input, one dataset of Doublet Input, and 2 dataset of Pulse Input are used for Integral gain estimation of PID Controller using traditional approach such as ZN, MZN, AH and TL

KD-PID									
Dataset	ZN	MZN	AH	TL					
HO	0.1228	0.5247	0	0.2523					
H1	0.0911	0.5726	0	0.2753					
H2	0.1508	0.4963	0	0.2387					
H3	0.0831	0.53	0	0.2549					
H4	0.118	0.53	0	0.2549					
H5	0.0821	0.463	0	0.2227					
H6	0.1632	0.4633	0	0.2228					
H7	0.0325	0.53	0	0.2549					
H8	0.258	0.264	0	0.127					
H9	0.1451	0.532	0	0.2558					
H10	0.1864	0.4633	0	0.2228					
H11	0.081	0.532	0	0.2558					
H12	0.3944	0.4036	0	0.1941					
HP1	0.117	0.5917	0	0.2845					
HP2	0.1166	0.5828	0	0.2803					
HD1	0.0421	0.6181	0	0.2972					

Twelve datasets of Multistep Input, one dataset of Doublet Input, and 2 dataset of Pulse Input are used for Integral gain estimation of PID Controller using traditional approach such as ZN, MZN, AH and TL

### **D1.2 PI CONTROLLER**

KP-PI							
Dataset	ZN	TL					
H0	0.4635	0.3219					
H1	0.315	0.2188					
H2	0.603	0.4188					
H3	0.3105	0.2156					
H4	0.441	0.3063					
H5	0.351	0.2438					
H6	0.6975	0.4844					
H7	0.1215	0.0844					
H8	1.935	1.3438					
H9	0.54	0.375					
H10	0.7965	0.5531					
H11	0.3015	0.2094					
H12	1.935	1.3438					
HP1	0.315	0.2719					
HP2	0.396	0.275					
HD1	0.135	0.0938					

Twelve datasets of Multistep Input, one dataset of Doublet Input, and 2 dataset of Pulse Input are used for Proportional gain estimation of PI Controller using traditional approach such as ZN, MZN, AH and TL

KI-PI							
Dataset	ZN	TL					
H0	0.3512	3.498					
H1	0.2187	3.817					
H2	0.4843	3.3088					
H3	0.2329	3.5332					
H4	0.3308	3.5332					
H5	0.3014	3.0866					
H6	0.5985	3.0888					

H7	0.0911	3.5332
H8	2.9138	1.76
H9	0.4035	3.5464
H10	0.6834	3.0888
H11	0.2253	3.5464
H12	1.906	2.6906
HP1	0.263	3.9446
HP2	0.2701	3.8852
HD1	0.0868	4.1206

Twelve datasets of Multistep Input, one dataset of Doublet Input, and 2 dataset of Pulse Input are used for Integral gain estimation of PI Controller using traditional approach such as ZN, MZN, AH and TL

PD using ZN Tuning							
Dataset	Кр	Kd					
H0	0.824	0.1638					
H1	0.56	0.1214					
H2	1.072	0.201					
H3	0.552	0.1108					
H4	0.784	0.1574					
H5	0.624	0.1094					
H6	1.24	0.2176					
H7	0.216	0.0434					
H8	3.44	0.344					
H9	0.96	0.1934					
H10	1.416	0.2485					
H11	0.536	0.108					
H12	3.44	0.5259					
HP1	0.696	0.156					
HP2	0.704	0.1554					
HD1	0.24	0.0562					

#### **D1.3 PD CONTROLLER**

Twelve datasets of Multistep Input, one dataset of Doublet Input, and 2 dataset of Pulse Input are used for Proportional, Integral gain estimation of PD Controller using traditional approach such as ZN

#### D2. MULTI-STEP 3211 INPUT DATASETS (H0-H12)

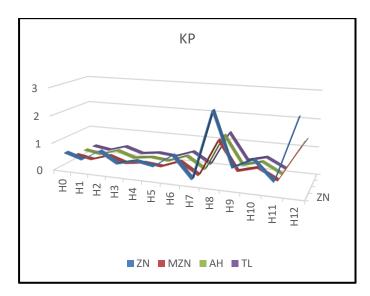


Fig D.1 Comparison of Proportional gain value of Multi-step datasets using Tuning approaches such as: ZN, MZN, TL, and AH

Proportional gain value of twelve datasets of multistep Input form using PID tuning approaches are compared and observed H7 dataset has highest gain value while using ZN Technique. Moreover, gain values of all datasets using various tuning methods superimposes each other

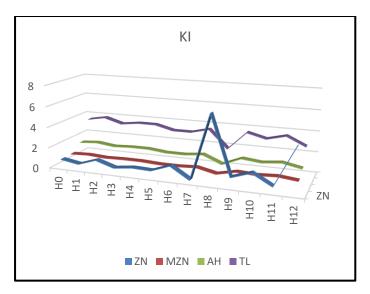


Fig D.2 Comparison of Integral gain value of Multi-step datasets using Tuning approaches such as: ZN, MZN, TL, and AH

Integral gain value of twelve datasets of multistep Input form using PID tuning approaches are compared and observed H7 and H9 dataset has highest gain value while using ZN Technique. Moreover, gain values of all datasets using various tuning methods superimposes each other.

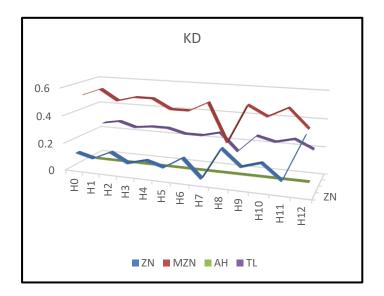


Fig D.3 Comparison of Derivative gain value of Multi-step datasets using Tuning approaches such as: ZN, MZN, TL, and AH

Derivative gain value of twelve datasets of multistep Input form using PID tuning approaches are compared and observed H1 dataset has highest gain value while using MZN Technique

### PULSE INPUT DATASETS (HP1-HP2)

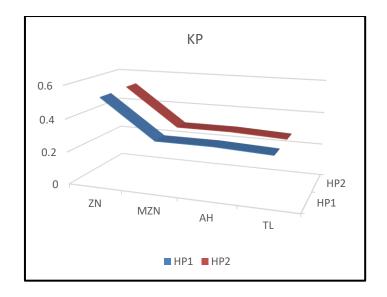


Fig D.4 Comparison of Proportional gain value of Pulse Input datasets using Tuning approaches such as: ZN, MZN, TL, and AH

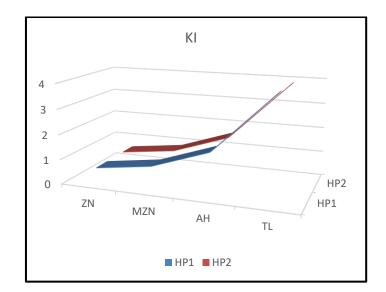


Fig D.5 Comparison of Integral gain value of Pulse Input datasets using Tuning approaches such as: ZN, MZN, TL, and AH

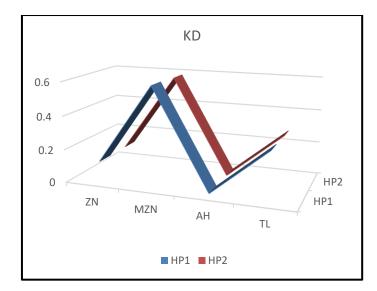
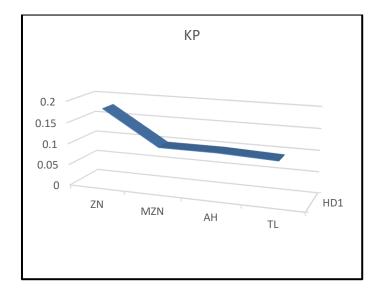


Fig D.6 Comparison of Derivative gain value of Pulse Input datasets using Tuning approaches such as: ZN, MZN, TL, and AH

Proportional, Derivative and Integral gain value of two datasets of Pulse Input form using PID tuning approaches are compared in above figure (D.4-6)



#### **DOUBLET INPUT DATASETS (HD1)**

Fig D.7 Comparison of Proportional gain value of Doublet Input datasets using Tuning approaches such as: ZN, MZN, TL, and AH

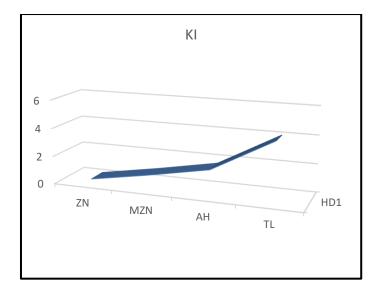


Fig D.8 Comparison of Integral gain value of Doublet Input datasets using Tuning approaches such as: ZN, MZN, TL, and AH

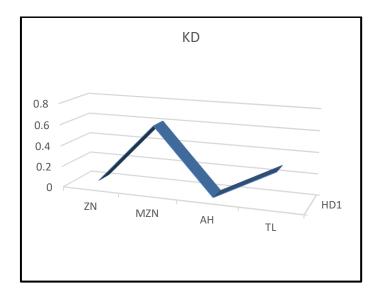


Fig D.9 Comparison of Derivative gain value of Doublet Input datasets using Tuning approaches such as: ZN, MZN, TL, and AH

Proportional, Derivative and Integral gain value of one datasets of Pulse Inputform using PID tuning approaches are compared in above figure (D.7-9)

## COMPARE MULTI STEP, DOUBLET, AND PULSE INPUT DATASETS OF PID CONTROLLER

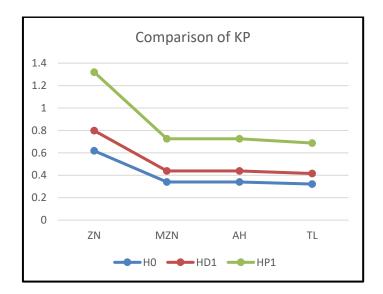


Fig D.10 Comparison of Proportional gain value of Multi-step, Doublet, and Pulse input datasets using Tuning approaches such as: ZN, MZN, TL, and AH

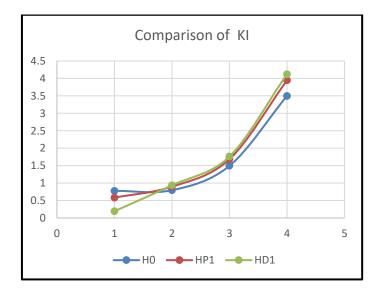


Fig D.11 Comparison of Integral gain value of Multi-step, Doublet, and Pulse input datasets using Tuning approaches such as: ZN, MZN, TL, and AH

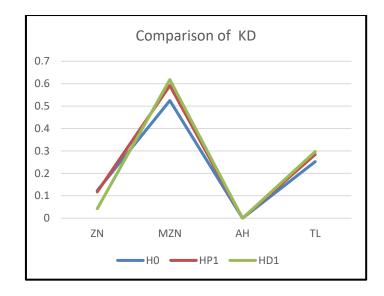


Fig D.12 Comparison of Derivative gain value of Multi-step, Doublet, and Pulse input datasets using Tuning approaches such as: ZN, MZN, TL, and AH

## COMPARE MULTI STEP, DOUBLET, AND PULSE INPUT DATASETS OF PD CONTROLLER

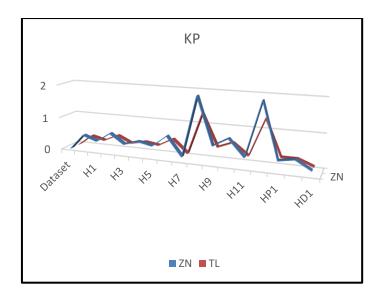


Fig D.13 Comparison of Proportional gain value of Multi-step, Doublet, and Pulse input datasets of PD Controller using Tuning approaches such as: ZN, and TL

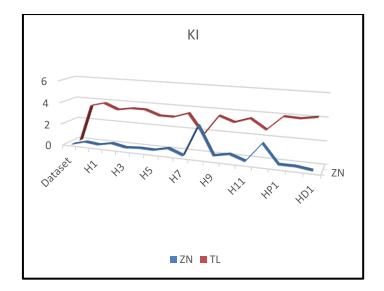


Fig D.14 Comparison of Integral gain value of Multi-step, Doublet, and Pulse input datasets of PD Controller using Tuning approaches such as: ZN, and TL

## COMPARE MULTI STEP, DOUBLET, AND PULSE INPUT DATASETS OF PD CONTROLLER

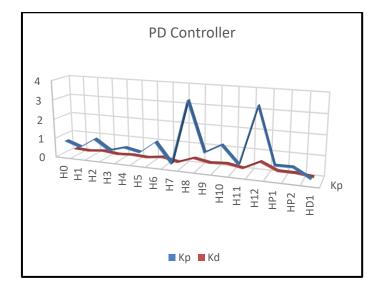
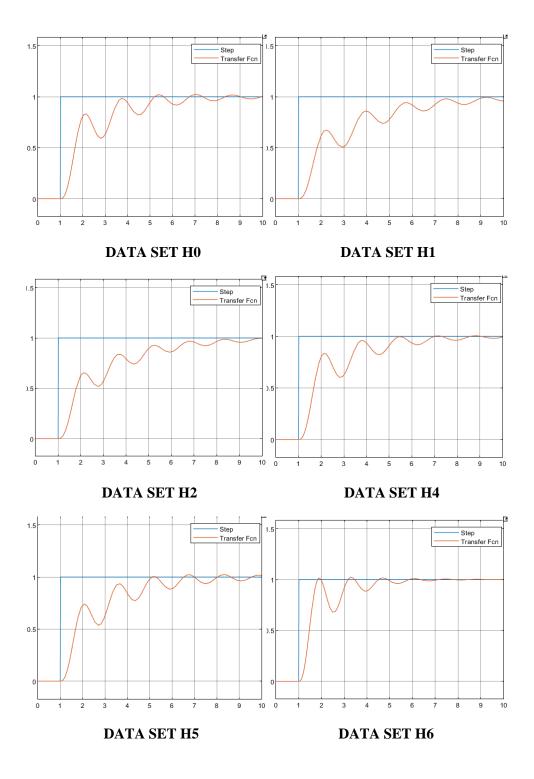


Fig D.15 Comparison of Proportional Integral gain value of Multi-step, Doublet, and Pulse input datasets of PD Controller

## ZIEGLER NICHOLAS FIGURES OF MULTI-STEP, DOUBLET, AND PULSE INPUT



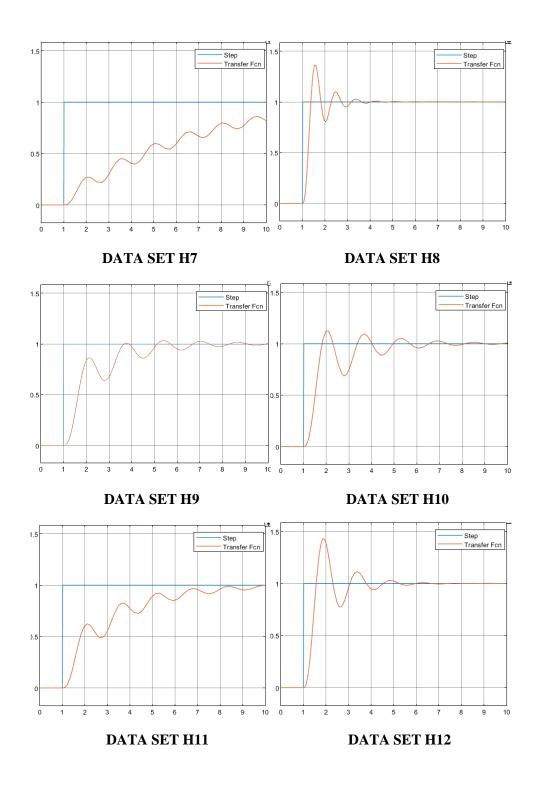
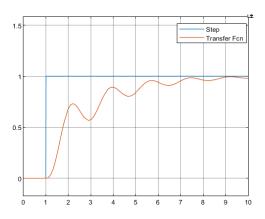


Fig D.16 Step response of Multi-step Input Dataset H0-H12 using Ziegler Nicholas tuning technique



DATA SET D1



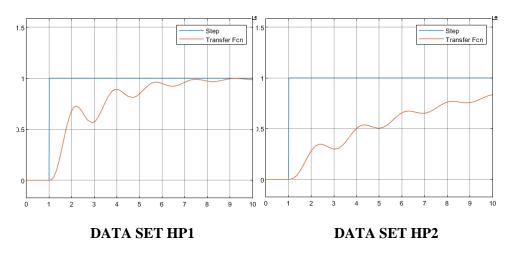
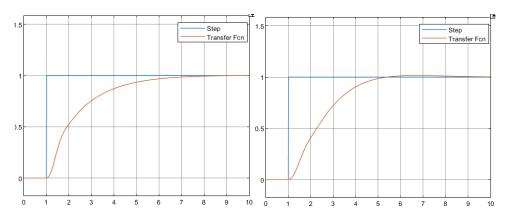


Fig D.17 Step response of Doublet, and Pulse Input Dataset D1, HP1, and HP2 using Ziegler Nicholas tuning technique

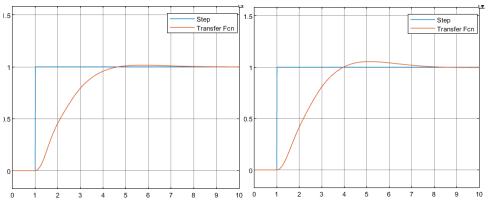
Various datasets are used for gain optimization to design controller using PID tuning Approach. In this figure, X axes denotes time(sec) and Y axes as amplitude. The step response shows oscillatory behaviour of input form which gets damped after short interval. Dataset H12 shows optimal response among all datasets.





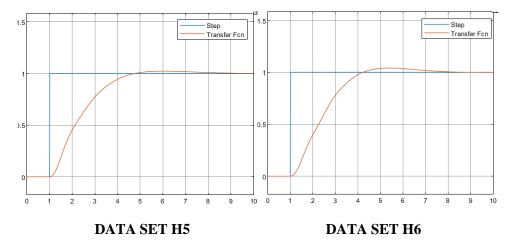








DATA SET H4



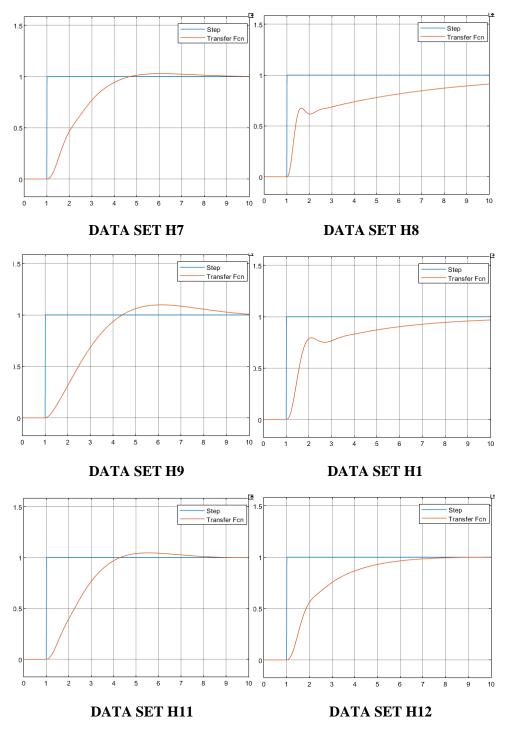
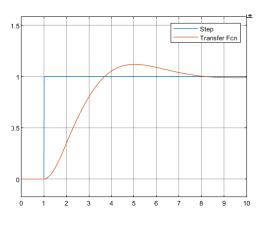


Fig D.18 Step response of Multi-step Input Dataset H0-H12 using Modified Ziegler Nicholas tuning technique



**DATA SET HD1** 



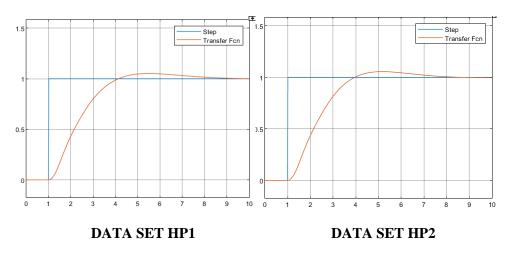
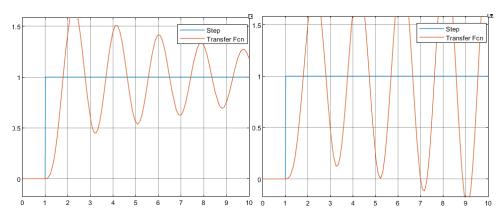


Fig D.19 Step response of Multi-step Input Dataset H0-H12 using Modified Ziegler Nicholas tuning technique

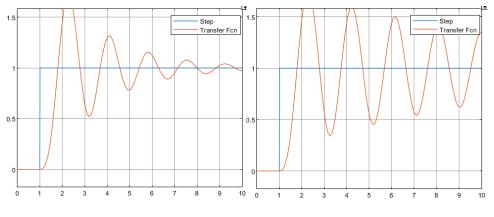
Various datasets are used for gain optimization to design controller using PID tuning Approach. In this figure, X axes denotes time(sec) and Y axes as amplitude. The step response shows oscillatory behaviour of input form which gets damped after short interval. Dataset H5 shows optimal response among all datasets as meeting all control system design requirements





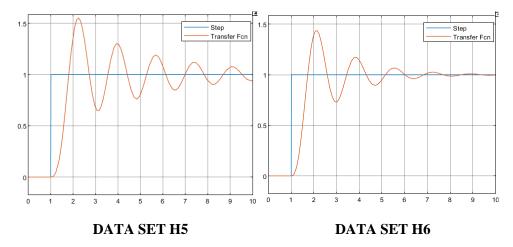








DATA SET H4



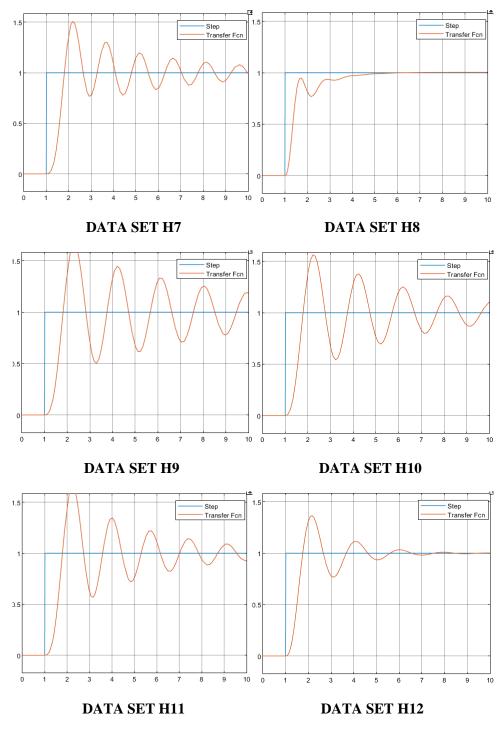
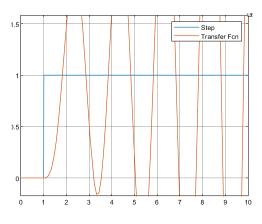


Fig D.20 Step response of Multi-step Input Dataset H0-H12 using Tyreus-Luyben tuning technique



**DATA SET HD1** 



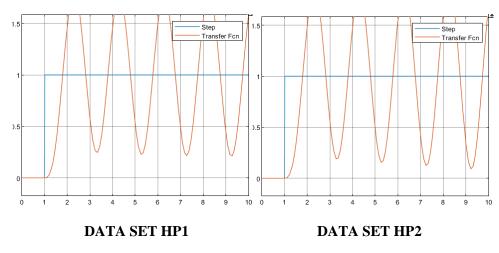
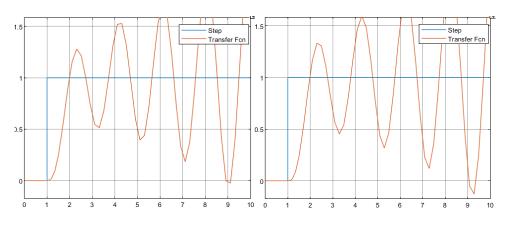


Fig D.21 Step response of Doublet, Pulse Input Dataset HD1, HP1, and HP2 using Tyreus-Luyben tuning technique

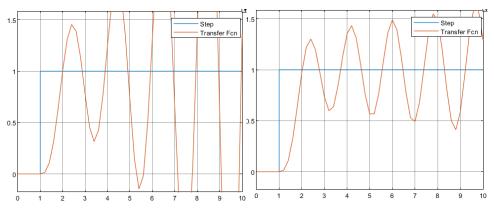
Various datasets are used for gain optimization to design controller using PID tuning Approach. In this figure, X axes denotes time(sec) and Y axes as amplitude. The amplitude of the step response shows oscillatory behaviour of input form which gets damped after short interval. Dataset H12 shows optimal response among all datasets whereas amplitude goes on increasing with respect to time of doublet and pulse input dataset

## ASTROM-HAGGLUND FIGURES OF MULTI-STEP, DOUBLET, AND PULSE INPUT



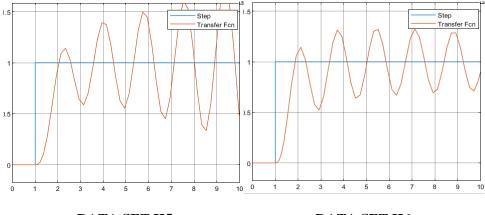






DATA SET H2

DATA SET H4



DATA SET H5

DATA SET H6

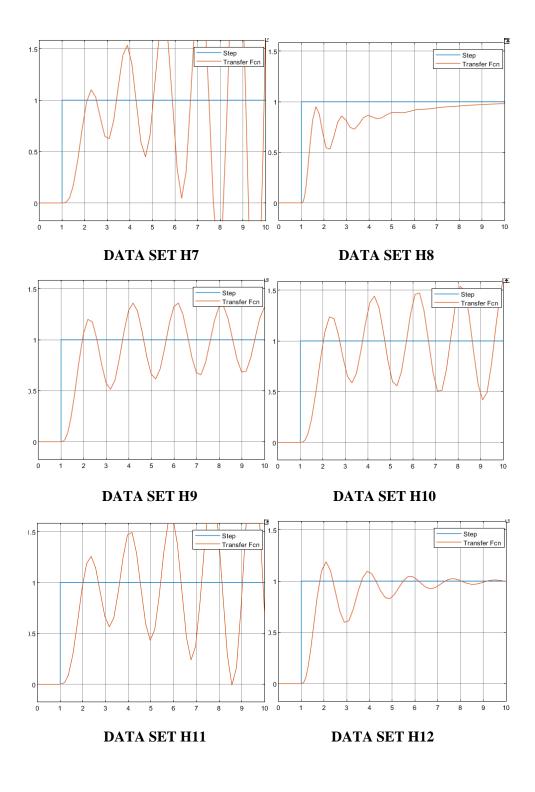
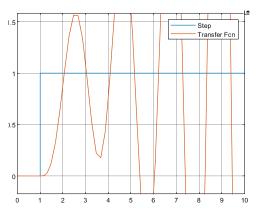


Fig D.22 Step response of Multi-step Input Dataset H0-H12 using Astrum-Hagglund tuning technique



**DATA SET HD1** 



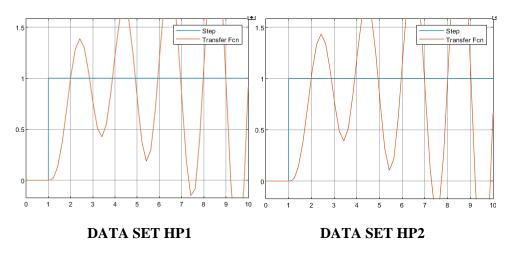
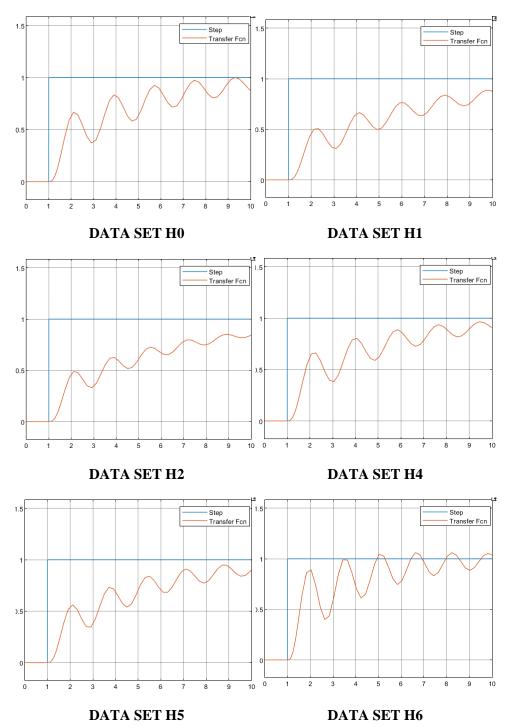


Fig D.23 Step response of Doublet, Pulse Input Dataset HD1, HP1, and HP2 using Astrum- Hagglund tuning technique

Various datasets are used for gain optimization to design controller using PID tuning Approach. In this figure, X axes denotes time(sec) and Y axes as amplitude. The amplitude of the step response shows oscillatory behaviour of input form which gets damped after short interval. Dataset H12 shows optimal response among all datasets whereas amplitude goes on increasing with respect to time of doublet and pulse input data

## ZIEGLER NICHOLAS FIGURES OF MULTI STEP, DOUBLET, AND PULSE INPUT DATASETS OF PI CONTROLLER

### **MULTISTEP INPUT**



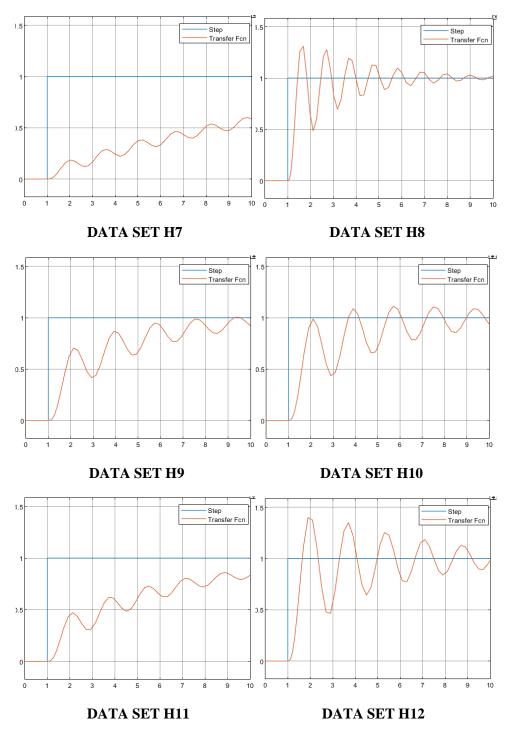
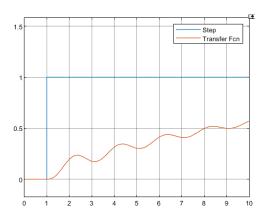


Fig D.24 Step response of Multi-step Input Dataset H0-H12 using Ziegler Nicholas tuning technique of PI Controller



**DATA SET HD1** 



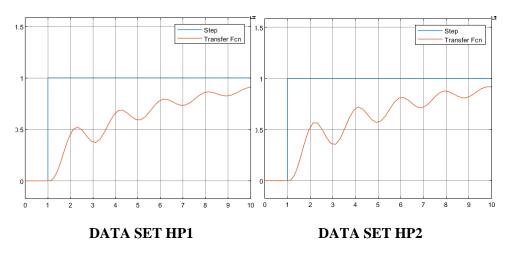
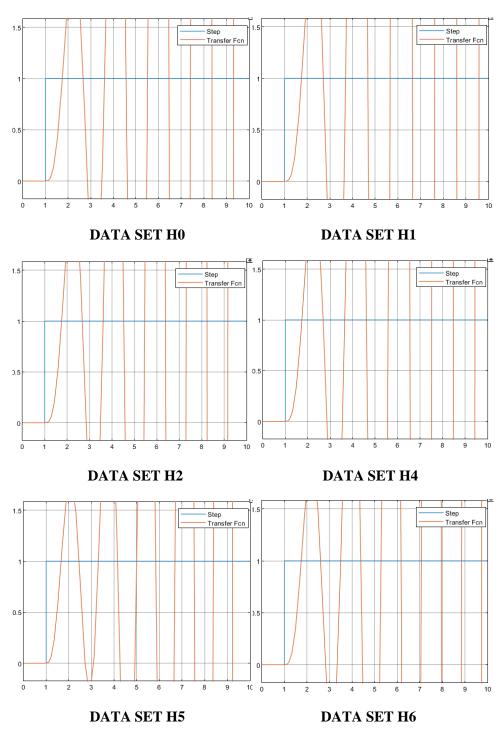


Fig D.25 Step response of Doublet, Pulse Input Dataset HD1, HP1, and HP2 using Astrum- Hagglund tuning technique

Various datasets are used for gain optimization to design controller using PI tuning Approach. In this figure, X axes denotes time(sec) and Y axes as amplitude. The amplitude of the step response shows oscillatory behaviour of input form which gets damped after short interval. Dataset H12 shows optimal response among all datasets

# TYREUS-LUYBEN FIGURES OF MULTI STEP, DOUBLET, AND PULSE INPUT DATASETS OF PI CONTROLLER



#### **MULTI STEP INPUT**

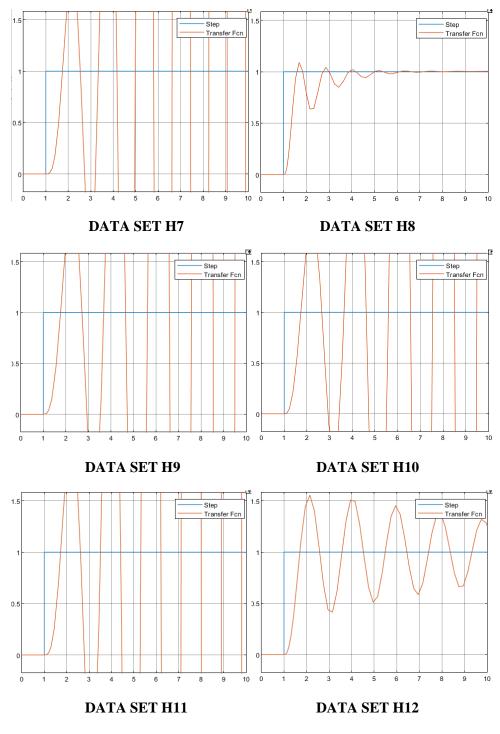
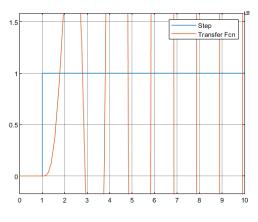


Fig D.26 Step response of Multi-step Input Dataset H0-H12 using Tyreus-Luyben tuning technique of PI Controller



DATA SET HD1

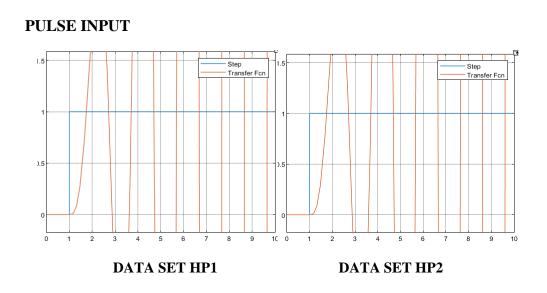
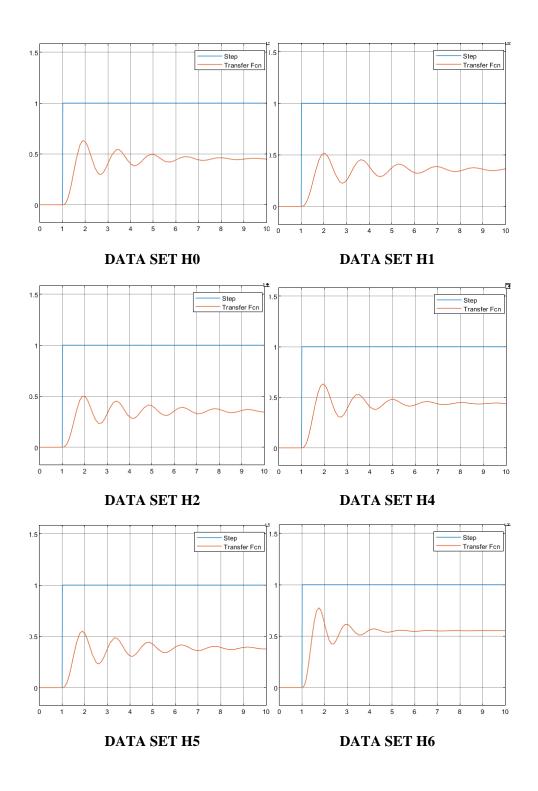


Fig D.27 Step response of Doublet, Pulse Input Dataset HD1, HP1, and HP2 using Astrum- Hagglund tuning technique

Various datasets are used for gain optimization to design controller using PI tuning Approach. In this figure, X axes denotes time(sec) and Y axes as amplitude. The amplitude of the step response shows oscillatory behaviour of input form which gets damped after short interval. Dataset H8 shows optimal response among all datasets. Moreover, all other datasets have ever increasing amplitude.

## ZIEGLER NICHOLAS FIGURES OF MULTI STEP, DOUBLET, AND PULSE INPUT DATASETS OF PD CONTROLLER

### **MULTISTEP INPUT**



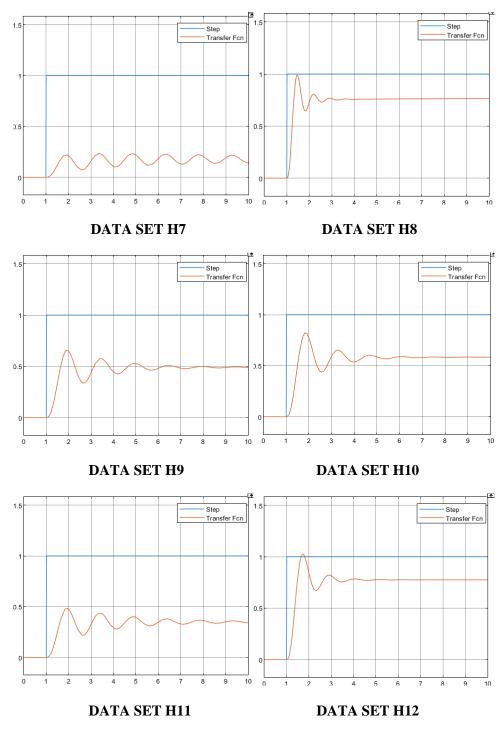
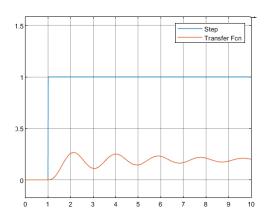


Fig D.28 Step response of Multi-step Input Dataset H0-H12 using Ziegler Nicholas tuning technique of PD Controller



DATA SET D1

#### **PULSE INPUT**

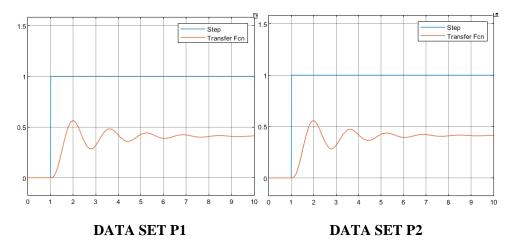


Fig D.29 Step response of Doublet, Pulse Input Dataset D1, P1, and P2 using Ziegler Nicholas tuning technique

Various datasets are used for gain optimization to design controller using PD tuning Approach. In this figure, X axes denotes time(sec) and Y axes as amplitude. The amplitude of the step response shows oscillatory behaviour of input form which gets damped after short interval.

# **D3. ESTIMATION OF CARTESIAN COORDINATES USING FLIGHT DATA**

Δt	ах	az	vx(k-1)	vx(k)	vz(k-1)	vz(k)	X(K-1)	Z(K-1)	Altitude( Y)	X(k)	Z(K)
0.02	2.474977	3.31304	36.5718	36.6213	26.682	26.74826	0	0	30540.65268	0.732426	0.534965
0.02	2.443499	3.326073	36.6213	36.67017	26.74826	26.81478	0.732426	0.534965	30540.65591	1.465829	1.071261
0.02	2.430449	3.315653	36.67017	36.71878	26.81478	26.8811	1.465829	1.071261	30540.65915	2.200205	1.608883
0.02	2.460625	3.335148	36.71878	36.76799	26.8811	26.9478	2.200205	1.608883	30540.66239	2.935565	2.147839
0.02	2.474912	3.320663	36.76799	36.81749	26.9478	27.01421	2.935565	2.147839	30540.66563	3.671915	2.688123
0.02	2.443434	3.312962	36.81749	36.86636	27.01421	27.08047	3.671915	2.688123	30540.66886	4.409242	3.229732
0.02	2.430385	3.318601	36.86636	36.91497	27.08047	27.14684	4.409242	3.229732	30540.6721	5.147541	3.772669
0.02	2.46056	3.302547	36.91497	36.96418	27.14684	27.21289	5.147541	3.772669	30540.67534	5.886825	4.316927
0.02	2.474847	3.337831	36.96418	37.01367	27.21289	27.27965	5.886825	4.316927	30540.67858	6.627098	4.86252
0.02	2.44337	3.311102	37.01367	37.06254	27.27965	27.34587	6.627098	4.86252	30540.68182	7.368349	5.409438
0.02	2.43032	3.305892	37.06254	37.11115	27.34587	27.41199	7.368349	5.409438	30540.68505	8.110572	5.957677
0.02	2.460496	3.310376	37.11115	37.16036	27.41199	27.4782	8.110572	5.957677	30540.68829	8.853779	6.507241
0.02	2.474782	3.31665	37.16036	37.20985	27.4782	27.54453	8.853779	6.507241	30540.69153	9.597976	7.058132
0.02	2.443305	3.317889	37.20985	37.25872	27.54453	27.61089	9.597976	7.058132	30540.69477	10.34315	7.61035
0.02	2.430255	3.298646	37.25872	37.30732	27.61089	27.67686	10.34315	7.61035	30540.698	11.0893	8.163887
0.02	2.460431	3.299971	37.30732	37.35653	27.67686	27.74286	11.0893	8.163887	30540.70124	11.83643	8.718744
0.02	2.474717	3.294893	37.35653	37.40603	27.74286	27.80876	11.83643	8.718744	30540.70448	12.58455	9.274919
0.02	2.44324	3.316298	37.40603	37.45489	27.80876	27.87508	12.58455	9.274919	30540.70772	13.33365	9.832421
0.02	2.43019	3.286346	37.45489	37.5035	27.87508	27.94081	13.33365	9.832421	30540.71095	14.08372	10.39124
0.02	2.460366	3.301883	37.5035	37.5527	27.94081	28.00685	14.08372	10.39124	30540.71419	14.83477	10.95137
0.02	2.474653	3.285324	37.5527	37.6022	28.00685	28.07256	14.83477	10.95137	30540.71743	15.58681	11.51283
0.02	2.443175	3.289663	37.6022	37.65106	28.07256	28.13835	15.58681	11.51283	30540.72067	16.33984	12.07559

Table D.3 Cartesian Coordinates Estimation Using Flight Data

## **APPENDIX-E**

## LIST OF PUBLICATIONS

### SCOPUS INDEXED JOURNALS

- 1. "A preliminary study of parameter estimation for fixed wing aircraft and high endurability parafoil Aerial Vehicle", INCAS Bulletin, Vol-12, Issue-4, SCOPUS Indexed, Dec2020
- "Classical and Modern gain estimation approach of PID Controller for the pitch control of the RCTA Aircraft", *INCAS Bull.*, vol. 14, no. 1, pp. 39-56, SCOPUS Indexed, 2022, Doi: 10.13111/2066-8201.2022.14.1.4

### CONFERENCES

- "Estimation of Lateral Directional Aerodynamic Derivatives from Flight Data of Unmanned Powered parafoil Aerial Vehicle", Proceedings of the AIAA Atmospheric Flight Mechanics Conference,2018
- 2. "Comparative study of longitudinal stability derivatives of Hansa-3 Aircraft Using Extended Kalman Filtering Technique and ML Method" in *Advances in Chemical Engineering*, SCOPUS Indexed, Dehradun, Feb2020.
- "Distinctive Navigational Approach –A Dead Reckoning for Aircraft Co-Ordinate Estimation", 4<sup>th</sup> International Conference on Smart and Sustainable Developments in Engineering and Technology, PiCET, 22<sup>nd</sup> May 2022.
- 4. "Comparative assessment of stochastic approaches-EKF, ML to determine parameters of an RCTA aircraft for autopilot design" is submitted on International Conference on Engineering and Technology, PiCET 2023

PhD	) Thesis				
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