


Name:			
Enrolment No:			
<b>UPES</b> <b>Supplementary Examination, December 2023</b>			
<b>Course:</b> Remedial Mathematics <b>Semester :</b> I <b>Program:</b> Int. BMSC Microbiology/N &D/Clinical Research, BT Biomedical/Biotechnical, B.Sc. FND/Microbiology/Clinical Research			
<b>Course Code:</b> BP106RMT		<b>Duration : 3 Hours</b> <b>Max. Marks: 100</b>	
<b>Instructions:</b> All questions are compulsory.			
S. No.	Section A Short answer questions/ MCQ/T&F (20Qx1.5M= 30 Marks)	Marks	COs
Q 1	The order of Matrix $A$ is $4 \times 4$ and $B$ is $4 \times 3$ the order of $AB$ is: a. $1 \times 3$ b. $4 \times 3$ c. $3 \times 3$ d. $3 \times 4$	1.5	CO1
Q2.	The cofactor of 4 in $\begin{bmatrix} 1 & 2 & 3 \\ 5 & 4 & 2 \\ 3 & 2 & 1 \end{bmatrix}$ is: a. 0 b. -8 c. 8 d. -4	1.5	CO1
Q3.	Find the order of $A^T$ if the matrix $A = \begin{pmatrix} 2 & -3 & 5 \\ 1 & 6 & 9 \end{pmatrix}$	1.5	CO1
Q4.	Check whether the following matrix is invertible: $\begin{bmatrix} 2 & 4 & -6 \\ 7 & 3 & 5 \\ 1 & -2 & 4 \end{bmatrix}$	1.5	CO1
Q5.	If $A^2 - A + I = O$ then inverse of then the inverse of $A$ is: a. $I - A$ b. $A - I$ c. $A$ d. $A + I$	1.5	CO1

<b>Q6.</b>	The slope of a line $ax + by + c = 0$ is: a. $\frac{a}{b}$ b. $-\frac{a}{b}$ c. $\frac{c}{b}$ d. $-\frac{c}{b}$	<b>1.5</b>	<b>CO2</b>
<b>Q7.</b>	The lines $3x + 4y = 9$ and $6x + 8y = 15$ are parallel: a. True b. False	<b>1.5</b>	<b>CO2</b>
<b>Q8.</b>	Find the distance of $(5, 12)$ from the origin.	<b>1.5</b>	<b>CO2</b>
<b>Q9.</b>	Write the condition for two lines to be perpendicular.	<b>1.5</b>	<b>CO2</b>
<b>Q10.</b>	$\int_0^2 (x^2 + 2) dx$ is equal to: a. $\frac{24}{3}$ b. $\frac{25}{3}$ c. $\frac{26}{3}$ d. $\frac{27}{3}$	<b>1.5</b>	<b>CO2</b>
<b>Q11.</b>	$\int_0^\pi \sin^2 x dx =$ a. $\frac{\pi}{2}$ b. $\frac{\pi}{4}$ c. $2\pi$ d. $4\pi$	<b>1.5</b>	<b>CO2</b>
<b>Q12.</b>	If $f(x) = x^4 + 5x^3 - 11x^2 - 45x + 60$ then find $f''(x)$ .	<b>1.5</b>	<b>CO3</b>
<b>Q13.</b>	Write the formula of $\frac{d}{dx}(uv)$ where $u$ & $v$ are the functions of $x$ .	<b>1.5</b>	<b>CO3</b>
<b>Q14.</b>	$\frac{d}{dx}(\sin x \cos x)$ is equal to: a. $\cos^2 x + \sin^2 x$ b. $\sin^2 x - \cos^2 x$ c. $\cos^2 x - \sin^2 x$ d. $-2\cos^2 x$	<b>1.5</b>	<b>CO3</b>
<b>Q15.</b>	If $f(x) = \frac{e^x}{x^2}$ then, $f'(1)$ is: a. $e$ b. $-e$ c. $2e$ d. $-2e$	<b>1.5</b>	<b>CO3</b>
<b>Q16.</b>	If $u$ & $v$ are two functions of $x$ then write the formula for integration of $uv$ .	<b>1.5</b>	<b>CO2</b>
<b>Q17.</b>	Integration of $xe^x$ is given by: a. $e^x(x + 1)$ b. $-e^x(x + 1)$	<b>1.5</b>	<b>CO2</b>

	c. $e^x(x - 1)$ d. $xe^x$		
<b>Q18.</b>	Define upper triangular matrix.	<b>1.5</b>	<b>CO1</b>
<b>Q19.</b>	Find the value of $\lim_{x \rightarrow 8} \frac{x^2 - 64}{x - 8}$	<b>1.5</b>	<b>CO1</b>
<b>Q20.</b>	The function $f(x) = x^3 - 4x^2 + 4x + 3$ defined on $[-1, 3]$ has: a. Minimum value $-6$ at $x = -1$ b. Minimum value $6$ at $x = 3$ c. Minimum value $3$ at $x = 2$ d. None of these	<b>1.5</b>	<b>CO3</b>
<b>Section B</b> <b>(4Qx5M=20 Marks)</b>			
<b>Attempt any 4 questions out of 5.</b>			
<b>Q 1</b>	Find the equation of a line passing through the point $(3, -2)$ and perpendicular to the line $x - 3y + 5 = 0$ .	<b>5</b>	<b>CO2</b>
<b>Q 2</b>	Show that the points $A(-3, -3), B(3, 3)$ & $C(-3\sqrt{3}, 3\sqrt{3})$ are the vertices of equilateral triangle.	<b>5</b>	<b>CO2</b>
<b>Q 3</b>	Evaluate $\frac{dy}{dx}$ when $y = (3x^4e^x + 5)$	<b>5</b>	<b>CO3</b>
<b>Q 4</b>	Evaluate the Laplace transform of $(t^2 + 4t + 2)e^{3t}$	<b>5</b>	<b>CO3</b>
<b>Q 5</b>	Evaluate $I = \int \frac{x}{x^2 - 1} dx$	<b>5</b>	<b>CO3</b>
<b>Section C</b> <b>(2Qx15M=30 Marks)</b>			
<b>All questions are compulsory Q1 has internal choice.</b>			
<b>Q 1</b>	A pharmaceutical company produces three medicines using ingredients $A, B$ and $C$ . One unit of $P$ requires 1, 2 and 3 units of $A, B$ and $C$ respectively. One unit of $Q$ requires 2, 3 and 2 units of $A, B$ and $C$ respectively. One unit of $R$ requires 1, 2 and 2 units of $A, B$ and $C$ respectively. The number of units available for ingredients $A, B$ and $C$ are 8, 14 and 13 units respectively. Using the matrix method, determine the number of units of each medicine to produce to utilize completely the available resources. <b>OR</b> Bacteria increases at the rate proportional to the number of bacteria present. If the original number $N$ doubles in 4 hours, find how many hours the number of bacteria will be $16N$ .	<b>15</b>	<b>CO4</b>
<b>Q 2</b>	Evaluate the integral $I$ using the method of partial fractions $I = \int \frac{x + 4}{(3 + 2x - x^2)} dx$	<b>15</b>	<b>CO3</b>

**Section D**  
**(2Qx10M=20 Marks)**

**All questions are compulsory Q2 has internal choice.**

<b>Q 1</b>	Find the equation of the line which passes through the point (3, 4) and the sum of its intercept on the axes is 14.	<b>10</b>	<b>CO2</b>
<b>Q 2</b>	Apply Cramer's rule to solve the following system of equations: $x + y + z = 6$ $y + 3z = 11$ $x - 2y + z = 0$ <p style="text-align: center;"><b>OR</b></p> Determine whether the matrix $A$ is invertible or not. If it is invertible then apply adjoint method to find the inverse of matrix $A$ : $A = \begin{bmatrix} 2 & 6 & 3 \\ 4 & -1 & 3 \\ 1 & 3 & 2 \end{bmatrix}$	<b>10</b>	<b>CO1</b>