| Name: <br> Enrolment No: |  |  |  |
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| UNIVERSITY OF PETROLEUM AND ENERGY STUDIES End Semester Supplementary Examination, December 2023 |  |  |  |
| Course: Advanced Physical Chemistry <br> Program: M.Sc. Chemistry <br> Course Code: CHEM7016 |  |  |  |
| Instructions: <br> 1. Write your enrolment number on the top left of the question paper <br> 2. Do not write anything else on the question paper except your enrolment number <br> 3. Attempt all part of a question at one place only |  |  |  |
| $\begin{gathered} \text { SECTION A } \\ \text { (5Qx4M=20Marks) } \end{gathered}$ |  |  |  |
| S. No. |  | Marks | CO |
| Q 1 | A particle in three dimensional cubic box with length "a" has energy of $17 \mathrm{~h}^{2} / 8 \mathrm{ma}^{2}$. What is the degeneracy of the state? | 4 | CO1 |
| Q 2 | Explain the origin of degeneracy in the cubic box. | 4 | CO1 |
| Q 3 | Find the value of commutator $\left[\mathrm{p}_{\mathrm{x}}, \mathrm{x}\right]$, where $\mathrm{p}_{\mathrm{x}}$ is the momentum and x is position. | 4 | CO2 |
| Q 4 | The absorbance of a dye solution at 500 nm is 1.2 when a quartz cuvette with path length of 1 cm is used. What is the transmittance of the dye solution? | 4 | CO4 |
| Q 5 | The energy $2^{\text {nd }}$ vibrational state of 1D linear harmonic oscillator is 200 $\mathrm{cm}^{-1}$. What is the zero-point energy? | 4 | CO4 |
| $\begin{gathered} \text { SECTION B } \\ \text { (4Qx10M=40 Marks) } \end{gathered}$ |  |  |  |
| Q 1 | (a) Calculate the rotational energy of the $\mathrm{J}=2$ state when rotational constant $\mathrm{B}=500 \mathrm{~cm}^{-1}$. What is the degeneracy of rotational state with $\mathrm{J}=1$ ? <br> (b) Explain $1^{\text {st }}$ and $2^{\text {nd }}$ postulates of quantum mechanics. | 5+5 | $\mathrm{CO3}$ |
| Q 2 | (a) What are the gross and specific selection rule of pure rotational spectroscopy? <br> (b) What are the characteristics of well behaved wavefunction? | 5+5 | $\mathrm{CO3}$ |
| Q 3 | Find the eigen value of function $f=e^{-4 i x}$ operated by an operator $\hat{A}=$ $\left(\frac{d^{2}}{d x^{2}}\right)$. | 10 | $\mathrm{CO3}$ |


| Q 4 | (a) Find the expression of angular momentum operator along $x, y$ and z directions. <br> (b) What are the causes of spectral line broadening? | 5+5 | $\mathrm{CO3}$ |
| :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { SECTION-C } \\ \text { (2Qx20M=40 Marks) } \end{gathered}$ |  |  |  |
| Q 1 | (i) Using a suitable diagram show the origin fundamental, $1^{\text {st }}$ overtone, $2^{\text {nd }}$ overtone and hot bands in vibrational spectroscopy. <br> (ii) (a) Write relation between rotational constant (B) and bond length (r). Explain all the terms involved. (b) The fundamental vibration frequency of ${ }^{1} \mathrm{H}^{35} \mathrm{Cl}$ molecule is 5 X $10^{13} \mathrm{~Hz}$. Calculate the force constant for this molecule. (Given: Plank constant $=6.626 \times 10-34 \mathrm{Js}$ ). <br> OR <br> (i) Using thermodynamic square find all the Maxwell's relation. <br> (ii) Derive the expression of wave function and energy of a particle in three-dimensional box. | 10+10 | $\mathrm{CO4}$ |
| Q 2 | (i) Given that a particle is restricted to the region $-\mathrm{a}<\mathrm{x}<\mathrm{a}$ and has a wave function $\psi$ proportional to $\boldsymbol{\operatorname { c o s }}\left(\frac{\pi x}{2 a}\right)$, normalize the wave function. <br> (ii) Using a suitable diagram show the origin of $\mathrm{P}, \mathrm{Q}, \mathrm{R}$ branch in a rotational-vibrational. Write the specific selection rules for $\mathrm{P}, \mathrm{Q}$ and R branches. | 10+10 | CO 2 |

