

Name:			
Enrolment No:			
UNIVERSITY OF PETROLEUM AND ENERGY STUDIES End Semester Examination, December 2022			
Course: Mathematics III (Probability and Statistics) Program: B.Tech EE Course Code: MATH 2046		Semester: III Time : 03 hrs. Max. Marks: 100	
Instructions: Attempt all questions			
SECTION A (5Qx4M=20Marks)			
S. No.		Marks	CO
Q 1	A bag contains 3 red and 4 white balls. Two draws are made without replacement. What is the probability that both the balls drawn are red.	4	CO1
Q2	If 10% of screws produced by a machine are defective, find the probability that out of 5 screws chosen at random none is defective.	4	CO3
Q3	The probability that a contractor will get a plumbing contract is $\frac{2}{3}$ and probability that he will get electric contract is $\frac{5}{9}$. If the probability of getting any one contract is $\frac{4}{5}$, what is the probability that he will get both the contract.	4	CO1
Q4	The equations of two regression lines, obtained in a correlation analysis of 60 observations are: $5x = 6y + 24$ and $1000y = 768x - 3608$. What is the correlation coefficient?	4	CO4
Q5	Find the relation between coefficient of correlation and coefficients of regression.	4	CO4
SECTION B (4Qx10M= 40 Marks)			
Q 6	If the random variable has the probability density function $f(x)$ as $f(x) = \begin{cases} 2e^{-2x} & x > 0 \\ 0 & x \leq 0 \end{cases}$ Find the probabilities that it will take on values i. Between 1 and 3 ii. Greater than 0.5	10	CO3
Q7	In a partially destroyed laboratory record of an analysis of a correlation data, the following results only are eligible: Variance of $x = 9$ Regression equations: $8x - 10y + 66 = 0$, $40x - 18y = 214$. What were (a) the mean values of x and y	10	CO4

	(b) the standard deviation of y and the co-efficient of correlation between x and y .																						
Q8	By the method of least squares, find the curve $y = ax + bx^2$ that best fits the following data: <table border="1" style="margin: 10px auto;"> <tr> <td>x</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>y</td> <td>1.8</td> <td>5.1</td> <td>8.9</td> <td>14.1</td> <td>19.8</td> </tr> </table>	x	1	2	3	4	5	y	1.8	5.1	8.9	14.1	19.8	10	CO4								
x	1	2	3	4	5																		
y	1.8	5.1	8.9	14.1	19.8																		
Q9	Calculate the first four moments, skewness and kurtosis of the following distribution <table border="1" style="margin: 10px auto;"> <tr> <td>x</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> <td>8</td> </tr> <tr> <td>f</td> <td>1</td> <td>8</td> <td>28</td> <td>56</td> <td>70</td> <td>56</td> <td>28</td> <td>8</td> <td>1</td> </tr> </table> <p style="text-align: center;">OR</p> The first four moments of distribution about $x = 2$ are 1, 2.5, 5.5 and 16. Calculate first four moments about mean	x	0	1	2	3	4	5	6	7	8	f	1	8	28	56	70	56	28	8	1	10	CO2
x	0	1	2	3	4	5	6	7	8														
f	1	8	28	56	70	56	28	8	1														

SECTION-C
(2Qx20M=40 Marks)

Q 10	<p>a. The troubleshooting capacity of an IC chip in a circuit is a random variable X whose distribution function is given by</p> $F(x) = \begin{cases} 0 & x \leq 3 \\ 1 - \frac{9}{x^2} & x > 3 \end{cases}$ <p>Where x denotes the number of years. Find the probability that the IC chip will work properly</p> <p>i. Less than 8 years ii. Beyond 8 years</p> <p>b. Given is the joint distribution of X and Y</p> <table border="1" style="margin: 10px auto;"> <tr> <td></td> <td></td> <td colspan="2" style="text-align: center;">X</td> </tr> <tr> <td style="text-align: center;">Y</td> <td style="text-align: center;">0</td> <td style="text-align: center;">1</td> <td style="text-align: center;">2</td> </tr> <tr> <td style="text-align: center;">0</td> <td style="text-align: center;">.02</td> <td style="text-align: center;">.08</td> <td style="text-align: center;">.1</td> </tr> <tr> <td style="text-align: center;">1</td> <td style="text-align: center;">.05</td> <td style="text-align: center;">.2</td> <td style="text-align: center;">.25</td> </tr> <tr> <td style="text-align: center;">2</td> <td style="text-align: center;">.03</td> <td style="text-align: center;">.12</td> <td style="text-align: center;">.15</td> </tr> </table> <p>Calculate marginal distribution and the conditional distribution of X and Y.</p>			X		Y	0	1	2	0	.02	.08	.1	1	.05	.2	.25	2	.03	.12	.15	20	CO2
		X																					
Y	0	1	2																				
0	.02	.08	.1																				
1	.05	.2	.25																				
2	.03	.12	.15																				

Q11	Records taken of the number of male and female births in 800 families having four children are as follows										20	CO4																				
Number of male births	0	1	2	3	4																											
Number of female births	4	3	2	1	0																											
Number of families	32	178	290	236	94																											
<p>Test whether the data are consistent with the hypothesis that the Binomial law holds and the chance of male birth is equal to that of female birth, namely $p = q = 1/2$.</p> <p>Value of χ^2 at 5% level of significance for 4 is 9.49.</p> <p style="text-align: center;">OR</p> <p>Ten students got the following percentage of marks in mathematics and physics</p> <table border="1" data-bbox="240 961 1157 1102"> <tr> <td>Mathematics(x)</td> <td>8</td> <td>36</td> <td>98</td> <td>25</td> <td>75</td> <td>82</td> <td>92</td> <td>62</td> <td>65</td> <td>35</td> </tr> <tr> <td>Physics (y)</td> <td>84</td> <td>51</td> <td>91</td> <td>60</td> <td>68</td> <td>62</td> <td>86</td> <td>58</td> <td>35</td> <td>49</td> </tr> </table> <p>Find the rank correlation coefficient.</p>													Mathematics(x)	8	36	98	25	75	82	92	62	65	35	Physics (y)	84	51	91	60	68	62	86	58
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