Name:

**Enrolment No:** 



## UNIVERSITY OF PETROLEUM AND ENERGY STUDIES End Semester Examination, December-January 2021

**Course: Computational Gas Dynamics Program: M. Tech. CFD Course Code: ASEG 7020**  Semester: I Time: 03 hrs. Max. Marks: 100

## SECTION A

## Instructions: This Section has 05 questions and all questions are compulsory. Scan and upload all the correct answer(s).

S. No.		Marks	СО
Q 1	<ul> <li>For a one-dimensional flow of a perfect gas a compression wave is a region in the flow where</li> <li>i. The speed of acoustic waves increases monotonically</li> <li>ii. The speed of acoustic waves decreases monotonically</li> <li>iii. The speed of entropy waves increases monotonically</li> <li>iv. The speed of entropy waves increases monotonically</li> <li>v. Pressure decreases monotonically</li> </ul>	04	C01
Q 2	<ul> <li>The one dimensional unsteady Euler equations for a supersonic flow can be approximated as three wave equations. Which of the following statements are true for these waves?</li> <li>i. All the waves travel towards in the direction of flow</li> <li>ii. Two waves travel downstream while one wave travels upstream</li> <li>iii. Two waves travel upstream while one wave travels downstream</li> <li>iv. All waves travel upstream</li> <li>v. Speeds of all waves is higher than the local speed of sound.</li> </ul>	04	CO1
Q 3	Roe's approximate Riemann solver (three wave approximation) i. Yields exact solution for a single shock ii. Yields exact solution for a single contact iii. Yields exact solution for a single expansion wave iv. Allows expansion shock	04	CO2

	v. Yields inaccurate solution for a single compression wave		
Q 4	For Roe's approximate Riemann solver		
	i. The Roe averaged velocity at the interface is a linear average of the left and		
	right velocities	04	CO3
	ii. The Roes averaged enthalpy at the interface is a linear average of the left and		
	right enthalpies		
	iii. The Roes averaged density at the interface is a linear average of the left and		
	right densities		
	iv. The Roes averaged speed of sound at the interface is a linear average of the		
	left and right speeds of sound		
	v. The Roe averaged velocity at the interface is a geometric mean of the left and		
	right velocities		
Q 5	The interface flux for the Godunov's first order upwind scheme is		
	i. $f(u_L)$ for $u_L > 0$ and $u_R > 0$		
	ii. $f(u_L)$ for $u_L < 0$ and $u_R < 0$		CO4
	iii. $f(u_R)$ for $u_L > 0$ and $u_R > 0$	04	
	iv. $f(u_R)$ for $u_L < 0$ and $u_R < 0$		
	v. $f(u_L)$ for $u_L < 0$ and $u_R > 0$		
	SECTION B		
	ctions: This Section has 04 questions and all questions are compulsory. Scan and up nswer should be of short type (up to 200 words or equivalent numbers).	load the	answers.
Q 6	Consider the non-conservation form of Euler equation, given as		
		1	

QU	$\frac{\partial U}{\partial t} + A \frac{\partial U}{\partial x} = 0$ If matrix $T^{-1}$ , which the concatenation of the left eigenvector of Jacobian matrix $A$ is found to be	10	C01	

	$T^{-1} = \begin{cases} 1 - \frac{(\gamma - 1)}{2} \frac{u^2}{a^2} & (\gamma - 1) \frac{u}{a^2} & -\frac{(\gamma - 1)}{a^2} \\ \frac{(\gamma - 1)}{4} \frac{u^2}{a^2} - \frac{1}{2} \frac{u}{a} & -\frac{(\gamma - 1)}{2} \frac{u}{a^2} + \frac{1}{2a} & \frac{(\gamma - 1)}{2a^2} \\ \frac{(\gamma - 1)}{4} \frac{u^2}{a^2} + \frac{1}{2} \frac{u}{a} & -\frac{(\gamma - 1)}{2} \frac{u}{a^2} - \frac{1}{2a} & \frac{(\gamma - 1)}{2a^2} \end{cases} \end{cases}$ Find the elements the vector $dV$ , which represents changes in characteristic variables for the wave form of 1 D Euler equations.		
Q 7	Suppose that the solution to the Riemann problem produces only a shock. Using conservation principles derive an expression for the change in internal energy across the shock wave in terms of $p_R$ , $p_L$ , $\rho_R$ , and $\rho_L$ , where the subscripts $_L$ and $_R$ represent the left and right state respectively	10	CO1
Q 8	Discuss a Flux Vector Splitting technique in context to the solution of 1D unsteady Euler equations.	10	CO4
Q 9	Consider the scalar flux function illustrated below. Find the conservative numerical flux $f_{i+1/2}^n$ of Godunov's and Roe's first order upwind method. $ \int f(u) $ $ \int f(u) $ $ \int u $ $ \int u $ $ u $ $ u $ $ u $	10	CO4

## **SECTION-C**

Instructions: This Section has 02 questions and all questions are compulsory. Scan and upload the answer. The answer should be of long type (up to 500 words or equivalent numbers).

Q 10	Find the Roe's approximate solution to the Riemann problem for 1 D Euler equation at t = 0.01 s if $p_L = 50,000 \text{ N/m}^2$ , $\rho_L = 1 \text{ kg/m}^3$ , $u_L = 100 \text{ m/s}$ and $p_R = 10,000 \text{ N/m}^2$ , $\rho_R = 0.125 \text{ kg/m}^3$ , $u_R = -20 \text{ m/s}$ .	20	CO3
Q 11	Find the exact solution of the following Riemann problem for 1 D Euler equation at t = 0.01 s if $p_L = 25,000 \text{ N/m}^2$ , $\rho_L = 1 \text{ kg/m}^3$ , $u_L = 100 \text{ m/s}$ and $p_R = 5,000 \text{ N/m}^2$ , $\rho_R = 0.125 \text{ kg/m}^3$ , $u_R = -50 \text{ m/s}$ . $\frac{\partial u}{\partial t} + A \frac{\partial u}{\partial x} = 0$ where $u(x,0) = \begin{cases} u_L & x < 0\\ u_R & x > 0 \end{cases}$	20	CO2