

| Q 8 | (a) Show that the set of natural numbers $1,2,3,4$. $\qquad$ is not a group with respect to addition. <br> (b) Prove that the set $G=\{1,2,3,4,5,6\}$ is a finite abelian group of order 6 with respect to multiplication modulo 7 . | CO4 |
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| Q. 9 | Evaluate <br> (a) $\int_{0}^{\infty} \sqrt{x} e^{-\sqrt[3]{x}} d x$ <br> (b) $\int_{0}^{\infty} \cos x^{2} d x$ | CO2 |
| 1. Each Question carries 20Marks. <br> 2. Instruction: Write long answer. |  |  |
| Q10 | (a) Prove that $J_{n}(x)$ is the coefficient of $z^{n}$ in the expansion of $e^{\frac{x}{2}\left(z-\frac{1}{z}\right)}$. <br> (b) Prove that $J_{-\frac{1}{2}}(x)=\sqrt{\left(\frac{2}{\pi x}\right)} \cos x$ <br> OR <br> (a) Prove that $e^{2 x z-z^{2}}$ is the generating function for Hermite Polynomial. <br> (b) Convert Hermite polynomial $2 H_{4}(x)+3 H_{3}(x)-H_{2}(x)+5 H_{1}(x)+6 H_{0}$ <br> in to ordinary polynomial | CO 4 |
| Q. 11 | (a) Find the matrix P which diagonalize the matrix $A=\left[\begin{array}{ll} 4 & 1 \\ 2 & 3 \end{array}\right]$ <br> (b) Find the residue of $f(z)=\frac{z^{2}-2 z}{(z+1)^{2}\left(z^{2}+4\right)}$ | CO 2 |

