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| Progra <br> Course <br> Course <br> Nos. of | UNIVERSITY OF PETROLEUM AND ENERGY STUD <br> End Semester Examination, May 2021 | ES $\begin{aligned} & : \mathbf{8}^{\text {th }} \\ & : 03 \end{aligned}$ <br> rks : 100 |  |
| SECTION A |  |  |  |
| S. No. |  | Marks | CO |
| Q 1 | Explain the difference between finite element method and classical methods. | 5 | CO1 |
| Q 2 | Explain the Rayleigh Ritz method. | 5 | CO1 |
| Q 3 | Why are the polynomials preferred as shape functions? | 5 | CO1 |
| Q 4 | Explain plane stress and plane strain problems. | 5 | CO1 |
| Q 5 | Explain the properties of the global stiffness matrix. | 5 | CO1 |
| Q 6 | Explain the terms nodes, primary nodes, secondary nodes and internal nodes. | 5 | CO1 |
| SECTION B |  |  |  |
| Q 7 | A composite rod subjected to compression is modeled by two bar elements, as shown in Figure. Determine the nodal displacements and the axial stress in each element. $\begin{aligned} & E_{\mathrm{st}}=200 \mathrm{GPa} \\ & A_{\mathrm{st}}=4 \times 10^{-4} \mathrm{~m}^{2} \\ & E_{2 a}=70 \mathrm{GPa} \\ & A_{21}=2 \times 10^{-4} \mathrm{~m}^{2} \end{aligned}$ | 10 | CO2 |
| Q 8 | A plane truss is loaded and supported as shown in Figure. Determine the displacements at the free end using finite element method. Take, $\mathrm{E}=200 \mathrm{GPa}$ and A $=200 \mathrm{~mm}^{2}$ | 10 | CO2 |


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| Q 9 | For the beam shown in Figure, determine the nodal values at the point of applied load. Take $E=200 \mathrm{GPa}$. | 10 | $\mathrm{CO3}$ |
| Q 10 | For the frame shown in Figure, determine the global stiffness matrix and load vector and apply the boundary conditions using the elimination approach. Take $E=200$ GPa and $\mathrm{Area}=2 \times 2 \mathrm{~cm}^{2}$ | 10 | $\mathrm{CO3}$ |
| Q 11 | Determine the determinant of the Jacobian for the triangular element shown in Figure. | 10 | $\mathrm{CO3}$ |
| SECTION-C |  |  |  |


| Q 12 | Determine the stiffness matrix for the element shown in Figure. The coordinates are in units of meters. Assume plane stress condition. Let $E=200 \mathrm{GPa}, v=0.25$ and thickness $t=0.05 \mathrm{~m}$. | 20 | CO 3 |
| :---: | :---: | :---: | :---: |
|  | OR |  |  |
|  | If the sides of a rectangular box are 1 m , determine the stiffness matrix and load vector of the element. $E=5 \mathrm{GPa}$ and $v=0.25$. horizontal roller constraints are assumed at node 1 and 4. | 20 | CO 3 |

