| Name: <br> Enrolment No: |  |  |  |
| :---: | :---: | :---: | :---: |
| Course: Supersonic and Hypersonic Flows Semester: II <br> Program: M.Tech CFD Time $\mathbf{0 3}$ hrs. <br> Course Code: ASEG 7034P Max. Marks: $\mathbf{1 0 0}$ <br> Instructions: Required graph and tables are provided at the end of question paper.  |  |  |  |
| SECTION A |  |  |  |
| S. No. |  | Marks | CO |
| Q1. | Discuss various properties of hypersonic flow. | 5 | CO1 |
| Q2. | List the parameters which determines the strength of a shock wave. | 5 | CO2 |
| Q3. | "Stagnation pressure remains constant across an expansion fan" Whether the above sentence is true or false. Give reason for your answer. | 5 | $\mathrm{CO3}$ |
| Q4. | Discuss about small perturbation theory and its advantages. | 5 | CO4 |
| Q5. | Discuss the limitations of linearized velocity potential equation. | 5 | CO4 |
| Q6. | Define critical Mach number. What is the value of critical Mach number for a flat plate at zero angle of attack? | 5 | $\mathrm{CO5}$ |
| SECTION B |  |  |  |
| Q7. | Discuss on the severity of aerothermodynamics effects on a hypersonic vehicles and discuss about its control methods. | 10 | CO1 |
| Q8 | Consider the flow over a $22.2^{\circ}$ half-angle wedge. If the Mach number, pressure and temperature upstream of the shock wave are $2.5,1 \mathrm{~atm}$, and 300 K respectively, then calculate the wave angle and corresponding flow properties downstream of shock wave. | 10 | CO2 |
| Q9 | Consider a flow with pressure and temperature of 1 atm and 288 K . A Pitot tube is inserted into this flow and measures a pressure of 1.555 atm . What is the velocity of the flow? | 10 | $\mathrm{CO2}$ |
| Q10 | Consider the supersonic flow over an expansion corner. The deflection angle $\theta=$ $23.38^{0}$. If the flow upstream of the corner is given by $\mathrm{M}_{1}=2, \mathrm{P}_{1}=0.7 \mathrm{~atm}$ and $\mathrm{T}_{1}=$ 350 K , then calculate $\mathrm{M}_{2}, \mathrm{P}_{2}, \mathrm{~T}_{2}, \rho_{2}, \mathrm{P}_{0,2}$, and $\mathrm{T}_{0,2}$ downstream of the corner. Also, obtain the angles the forward and rearward Mach lines make with respect to the upstream direction. | 10 | $\mathrm{CO3}$ |
| Q11 | Derive velocity potential equation for compressible flow. | 10 | CO4 |
| SECTION-C |  |  |  |
| Q 12 | Consider a diamond-wedge airfoil with a half-angle $\varepsilon=10^{\circ}$. The airfoil is at an angle of attack $\alpha=15^{\circ}$ to a Mach 3 freestream. Calculate the lift and wave-drag coefficients for the airfoil. | 20 | $\mathrm{CO5}$ |

## Prandtl-Meyer Function and Mach Angle

| M | $v$ | $\mu$ | M | $v$ | $\mu$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $0.1000+01$ | 0.0000 | $0.9000+02$ | $0.1600+01$ | $0.1486+02$ | 0.5868+02 |
| $0.1020+01$ | $0.1257+00$ | $0.7864+02$ | $0.1620+01$ | $0.1545+02$ | $0.5812+02$ |
| $0.1040+01$ | $0.3510+00$ | $0.7406+02$ | $0.1640+01$ | $0.1604+02$ | $0.3757+02$ |
| $0.1060+01$ | $0.6767+00$ | $0.7063+02$ | $0.1660+01$ | $0.163+02$ | $0.3704+02$ |
| $0.1080+01$ | $0.9650+00$ | $0.6781+02$ | $0.1680+01$ | $0.1722+02$ | $0.565+02$ |
| $0.1100+01$ | $0.1336+01$ | $0.6538+02$ | $0.1700+01$ | $0.1781+02$ | $0.5003+02$ |
| $0.1120+01$ | $0.1735+01$ | $0.6323+02$ | $0.1720+01$ | $0.1840+02$ | $0.3555+02$ |
| $0.1140+01$ | $0.2160+01$ | $0.6131+02$ | $0.1740+01$ | $0.1898+02$ | $0.3508+02$ |
| $0.1160+01$ | $0.2007+01$ | $0.5955+02$ | $0.1760+01$ | 0.195602 | $0.3462+02$ |
| $0.1180+01$ | $0.3074+01$ | $0.5794+02$ | $0.1780+01$ | $0.2015+02$ | $0.3418+02$ |
| $0.1200+01$ | $0.3558+01$ | $0.5644+02$ | $0.1800+01$ | $0.2073+02$ | $0.3375+02$ |
| $0.1220+01$ | $0.4057+01$ | $0.5505+02$ | $0.1820+01$ | $0.2130+02$ | $0.3333+02$ |
| $0.1240+01$ | $0.4569+01$ | $0.5375+02$ | $0.1840+01$ | $0.2188+02$ | $0.3292+02$ |
| $0.1260+01$ | $0.5093+01$ | $0.5253+02$ | $0.1860+01$ | $0.2245+02$ | $0.5252+02$ |
| $0.1280+01$ | $0.5627+01$ | $0.5138+02$ | $0.1880+01$ | $0.2702+02$ | $0.3213+02$ |
| $0.1300+01$ | $0.6170+01$ | $0.5028+02$ | $0.1900+01$ | $0.2759+02$ | $0.3176+02$ |
| $0.1320+01$ | $0.6721+01$ | $0.4925+02$ | $0.1920+01$ | $0.2415+02$ | $0.3139+02$ |
| $0.1340+01$ | $0.7779+01$ | $0.4827+02$ | $0.1940+01$ | $0.2471+02$ | $03103+02$ |
| $0.1360+01$ | $0.7844+01$ | $0.4733+02$ | $0.1960+01$ | $0.2527+02$ | $0.3068+02$ |
| $0.1380+01$ | $0.8413+01$ | $0.4644+02$ | $0.1980+01$ | $0.2583+02$ | $0.3033+02$ |
| $0.1400+01$ | $0.8957+01$ | $0.4558+02$ | $0.2000+01$ | $0.2688+02$ | $0.3000+02$ |
| $0.1420+01$ | 0.9565+01 | $0.4477+02$ | $0.2050+01$ | $0.2775+02$ | $0.2920+02$ |
| $0.1440+01$ | $0.1015+02$ | $0.4398+02$ | $0.2100+01$ | $0.2910+02$ | $0.2844+02$ |
| $0.1460+01$ | $0.1073+02$ | $0.4323+02$ | $0.2150+01$ | $0.3043+02$ | $0.2772+02$ |
| $0.1480+01$ | $0.1132+02$ | $0.4251+02$ | $0.2200+01$ | $0.3173+02$ | $0.2704+02$ |
| $0.1500+01$ | $0.1191+02$ | $0.4181+02$ | $0.2250+01$ | $0.3702+02$ | $0.2639+02$ |
| $0.1520+01$ | $0.1249+02$ | $0.4114+02$ | $0.2300+01$ | $0.3428+02$ | $02577+02$ |
| $0.1540+01$ | $0.1309+02$ | $0.4049+02$ | $0.2350+01$ | $0.3553+02$ | $02518+02$ |
| $0.1560+01$ | $0.1368+02$ | $0.3987+02$ | $0.2400+01$ | $0.3675+02$ | $0.2462+02$ |
| $0.1580+01$ | $0.1427+02$ | $0.3927+02$ | $0.2450+01$ | $0.3795+02$ | $0.2409+02$ |


| M | $v$ | $\mu$ | M | $\nu$ | $\mu$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $0.2500+01$ | $0.3912+02$ | $0.2858+02$ | $0.5000+011$ | $0.7692+02$ | $0.1154+02$ |
| $0.2550+01$ | $0.4008+02$ | $0.2309+02$ | $0.5100+01$ | $0.7784+02$ | $0.1131+02$ |
| $0.2600+01$ | $0.4141+02$ | $0.2262+02$ | $0.5200+01$ | $0.7873+02$ | $0.1109+02$ |
| $0.2650+01$ | $0.4250+02$ | $0.2217+02$ | $0.5300+01$ | $0.7960+02$ | $0.1088+02$ |
| $0.2700+01$ | $0.4362+02$ | $0.2174+02$ | $0.5400+011$ | $0.8043+02$ | $0.1007+02$ |
| $0.2750+01$ | $0.4469+02$ | $0.2132+02$ | $0.5500+01$ | $0.8124+02$ | $0.1048+02$ |
| $0.2800+01$ | $0.4575+02$ | $0.2092+02$ | $0.5600+011$ | $0.8200+02$ | $0.1029+02$ |
| $0.2850+01$ | $0.4678+02$ | $0.2054+02$ | $0.5700+01$ | $0.8280+02$ | $0.1010+02$ |
| $0.2900+01$ | $0.4779+02$ | $0.2017+02$ | $0.5800+011$ | $0.8354+02$ | $0.9928+01$ |
| $0.2950+01$ | $0.4878+02$ | $0.1981+02$ | $0.5900+01$ | $0.8426+02$ | $0.9758+01$ |
| $0.3000+01$ | $0.4976+02$ | $0.1947+02$ | $060000+01$ | $0.8456+02$ | $0.9594+01$ |
| $0.3050+01$ | $0.5071+02$ | $0.1914+02$ | $06100+01$ | $0.8563+02$ | $0.9435+01$ |
| $0.3100+01$ | $0.5165+02$ | $0.1882+02$ | $0.6200+011$ | $0.8699+02$ | $0.9282+01$ |
| $0.3150+01$ | $0.5257+02$ | $0.1551+02$ | $0.6300+01$ | $0.869+02$ | $0.9133+01$ |
| $0.3200+01$ | $0.5347+0.2$ | $0.1821+02$ | $06400+01$ | $0.8756+02$ | $0.8589+01$ |
| $0.3250+01$ | $0.5435+02$ | $0.1792+02$ | $0.6500+01$ | $0.8817+02$ | $0.8850+01$ |
| $0.3300+01$ | $0.5522+02$ | $0.1764+02$ | $0.6600+011$ | $0.8876+02$ | $0.8715+01$ |
| $0.3350+01$ | $0.5607+02$ | $0.1737+02$ | $0.6700+011$ | $0.8933+02$ | $08584+01$ |
| $0.3400+01$ | $0.5691+02$ | $0.1710+02$ | $0.6800+01$ | $0.8989+02$ | $0.8457+01$ |
| $0.3450+01$ | $0.5773+02$ | $0.1685+02$ | $0.6900+01$ | $0.9044+02$ | $0.8333+01$ |
| $0.3500+01$ | $0.5850+02$ | $0.1660+02$ | $0.7000+011$ | $0.9097+02$ | $0.8213+01$ |
| $0.3550+01$ | $0.5932+02$ | 0.1636+02 | $0.7100+011$ | $0.9149+02$ | $0.8097+01$ |
| $0.3600+01$ | $0.6009+02$ | $0.1613+02$ | $0.7200+01$ | $0.9200+02$ | $0.7984+01$ |
| $0.3650+01$ | $0.005+02$ | $0.1590+02$ | $0.7300+01$ | $0.9249+02$ | $0.7873+01$ |
| $0.3700+01$ | $0.6160+02$ | $0.1568+02$ | $0.7400+01$ | $0.9297+02$ | $0.7766+01$ |
| $0.3750+01$ | $0.6239+02$ | $0.1547+02$ | $0.7500+01$ | $0.9344+02$ | $0.7662+01$ |
| $0.3800+01$ | $0.6104+02$ | $0.1526+02$ | $0.7600+011$ | $0.9790+02$ | $0.7561+01$ |
| $0.3850+01$ | $0.6375+02$ | $0.1505+02$ | $0.7700+01$ | $0.9434+02$ | $0.7462+01$ |
| $0.3900+01$ | $0.6444+02$ | $0.1486+02$ | $0.7800+011$ | $0.9478+02$ | $0.7366+01$ |
| $0.3950+01$ | $0.6512+02$ | $0.1466+02$ | $0.7900+01$ | $0.9521+02$ | $0.7272+01$ |
| $0.4000+01$ | $0.6578+02$ | $0.1448+02$ | $08000+01$ | $0.9562+02$ | $0.7181+01$ |
| $0.4050+01$ | $0.6644+02$ | $0.1429+02$ | $0.9000+011$ | $0.9972+02$ | $0.6379+01$ |
| $0.4100+01$ | $0.6708+02$ | $0.1412+02$ | $0.1000+02$ | $0.1023+03$ | $0.5739+01$ |
| $0.41 .50+01$ | $0.6771+02$ | $0.1394+02$ | $0.1100+02$ | $0.1048+03$ | $0.5216+01$ |
| $0.4200+01$ | $0.6835+02$ | $0.1377+02$ | $0.1200+02$ | $0.109+03$ | $0.4780+01$ |
| $0.4250+01$ | $0.6894+02$ | $0.1361+02$ | $0.1300+02$ | $0.1087+03$ | $0.4412+01$ |
| $0.4300+01$ | $0.6954+02$ | $0.1345+02$ | $0.1400+02$ | $0.1102+03$ | $0.4096+01$ |
| $0.4350+01$ | $0.7013+02$ | $0.1329+02$ | $0.1500+02$ | $0.1115+08$ | $0.3823+01$ |
| $0.4400+01$ | $0.7071+02$ | $0.1314+02$ | $0.1600+00$ | $0.1127+03$ | $0.3583+01$ |
| $0.4450+01$ | $0.7127+02$ | $0.1299+02$ | $0.1700+02$ | $0.1137+03$ | $0.3372+01$ |
| $0.4500+01$ | $0.7183+02$ | $0.1284+02$ | $0.1800+02$ | $0.1146+03$ | $0.3185+01$ |
| $0.4590+01$ | $0.7238+02$ | $0.1270+02$ | $0.1900+00$ | $0.1155+03$ | $0.3017+01$ |
| $0.4600+01$ | $0.7792+02$ | $0.1256+02$ | $0.2000+00$ | $0.1162+03$ | $0.2866+01$ |
| $0.4650+01$ | $0.7345+02$ | $0.1242+02$ | $0.2200+02$ | $0.1175+03$ | $0.2005+01$ |
| $0.4700+01$ | $0.7397+02$ | $0.1228+02$ | $0.2400+02$ | $0.1186+03$ | $0.2888+01$ |
| $0.4750+01$ | $0.7448+02$ | $0.1215+02$ | $0.2600+00$ | $0.1195+03$ | $0.2204+01$ |
| $0.4800+01$ | $0.7499+02$ | $0.1202+02$ | $0.2800+02$ | $0.1202+08$ | $0.2047+01$ |
| $0.4850+01$ | $0.7548+02$ | $0.1190+02$ | $03000+02$ | $0.1209+03$ | $0.1910+01$ |
| $0.4900+01$ | $0.7597+02$ | $0.1178+02$ | $03200+02$ | $0.1215+08$ | $0.1791+01$ |
| $0.4950+01$ | $0.7645+02$ | 0.1166+02 | $03400+02$ | $0.1200+03$ | $0.1685+01$ |

## $\theta-\beta-M$ Relationship



