| Name: <br> Enrolment No: |  |  |  |
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|  | UNIVERSITY OF PETROLEUM AND ENERGY STUDIES   <br> End Semester Examination, Jan 2021   <br> Chemical Engineering Computing Semester: I <br> Chemical Engineering: MTech PD Time: $\mathbf{0 3} \mathbf{~ h r}$ <br> Code: CHPD 7002 Max. Marks: $\mathbf{1 0 0}$ <br> ges: 2   | exam |  |
| Instru <br> (includ <br> PLEAS <br> Also, p | In this Open $\operatorname{Book}(\underline{S})$ and Notes Exam, you are allowed any number of books, all han your textbook), your own class notes and solutions to assignment problems, etc. (OBVIO <br> SCAN YOUR ANSWERS AND UPLOAD (WITH CALCULATIONS) <br> ase show all intermediate steps to earn full credit. | outs pro USLY no |  |
| SECTION A: (Open Books Exam) (2*30 = 60 Marks) Scan and Upload |  |  |  |
| Q 1 | Consider the following system of equations, (with $\boldsymbol{x} \equiv\left[x_{1}, x_{2}\right]$ ) $\begin{array}{r} f_{1}\left(x_{1}, x_{2}\right) \equiv 4 x_{1}+3 x_{2}=6 \\ f_{2}\left(x_{1}, x_{2}\right) \equiv 2 x_{1}+x_{2}=5 \tag{2} \end{array}$ <br> subject to the bounds: $0 \leq x_{1} \leq 10,0 \leq x_{2} \leq 10$ <br> a. Evaluate the analytical solution to give values of $x_{1}$ and $x_{2}$ <br> b. Write the solution in terms of Cramers' rule (Eqn. 1.4 in the text) in terms of appropriate determinants as: $\left.x_{j}=\left\|\mathbf{A}_{\mathbf{j}}\right\| /\|\mathbf{A}\|\right) ; \quad j=1,2 .$ <br> Here, $\|\mathbf{A}\|$ is the determinant of matrix, $\mathbf{A}$. Obtain the solution using this rule. (15) | (30 <br> Points) | $\begin{gather*} \text { CO1- }  \tag{15}\\ \text { CO2 } \end{gather*}$ |
| Q. 2 | Consider the set of equations in Problem 1. Use the Gauss Seidel technique to find the solution given $x_{1}^{(1)}=-1 \text { and } x_{2}^{(1)}=-2$ <br> Do only till: $x_{1}^{(2)}$ and $x_{2}^{(2)}$. | $\begin{gathered} (30 \\ \text { Points) } \end{gathered}$ | $\begin{gathered} \mathrm{CO} 3- \\ \mathrm{CO} 4 \end{gathered}$ |

## SECTION B: (40 Marks) Scan and Upload

| Q. 3 | Consider the following set of two ODE-IVPs $[d \boldsymbol{y} / d t=\boldsymbol{f}(\boldsymbol{y})]$ : $\begin{aligned} & \frac{d y_{1}}{d t}=2 y_{1}+6 y_{2} \\ & \frac{d y_{2}}{d t}=-6 y_{1}+5 y_{2} \end{aligned}$ <br> (a) Write this equation in terms of the Jacobian, $\boldsymbol{A}$, of $\boldsymbol{f}(\boldsymbol{y})$. <br> (b) Evaluate the eigenvalues of $\boldsymbol{A}$ <br> What can you say about the trajectory (variation with time, $t$ ) of the system starting from non-steady state values of $\boldsymbol{y}$. | $\begin{gathered} (40 \\ \text { Points) } \end{gathered}$ | CO5 |
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