## UNIVERSITY OF PETROLEUM AND ENERGY STUDIES <br> End Semester Examination, January 2021

Programme Name: B.Sc. (Hons.) Physics , B.Sc.(Hons.) Chemistry
Course Name : Matrices
Course Code : MATH-1029

Semester : I
Time : 3 Hrs
Max. Marks : 100

Nos. of page(s) : 2

## Section-A

1. Each question will carry 5 Marks. 2. Select correct answer in each question. 3. All Questions of this section are compulsory.

| S. No. |  | CO |
| :---: | :---: | :---: |
| Q1 | If $A$ and $B$ are Hermitian matrices, then $A B-B A$ is <br> A. Hermitian <br> B. Skew Hermitian Matrix <br> C. Unitary Matrix <br> D. None of the above | CO1 |
| Q2 | Rank of the matrix $\left[\begin{array}{ccc}3 & 1 & 7 \\ 1 & 2 & 4 \\ 4 & -1 & 7 \\ 2 & 1 & 5\end{array}\right]$ is <br> A. 1 <br> B. 2 <br> C. 3 <br> D. 4 | CO2 |
| Q3 | The value of $\lambda$ for which the following equations will have a non-trivial solution is: $\begin{aligned} & x+2 y+3 z=\lambda x \\ & 2 x+3 y+z=\lambda x \\ & 3 x+y+2 z=\lambda y \end{aligned}$ <br> A. 4 <br> B. Not equal to 4 <br> C. 6 <br> D. Not equal to 6 | CO 2 |
| Q4 | The value of $k$ for which the vectors $(1,-2, k),(2,-1,5)$ and $(3,-5,7 k)$ are linearly dependent is: <br> A. $5 / 14$ <br> B. $2 / 13$ <br> C. $5 / 12$ <br> D. 0 | $\mathrm{CO3}$ |
| Q5 | The eigenvalues of the matrix $\left[\begin{array}{ccc}1 & 2 & 2 \\ 0 & 2 & 1 \\ -1 & 2 & 2\end{array}\right]$ are: <br> A. $1,2,2$ <br> B. $0,2,3$ <br> C. $1,1,3$ <br> D. $0,0,5$ | CO4 |
| Q6 | The matrix A whose eigenvalues are $2,2,4$ and eigenvectors are $(-2,1,0)^{\prime},(-1,0,1)^{\prime},(1,0,1)^{\prime}$ is <br> A. $\left[\begin{array}{lll}1 & 1 & 1 \\ 2 & 3 & 4 \\ 7 & 2 & 4\end{array}\right]$ <br> B. $\left[\begin{array}{lll}3 & 2 & 1 \\ 2 & 2 & 2 \\ 1 & 2 & 3\end{array}\right]$ <br> C. $\left[\begin{array}{lll}3 & 2 & 3 \\ 1 & 2 & 1 \\ 1 & 2 & 3\end{array}\right]$ <br> D. $\left[\begin{array}{lll}3 & 2 & 1 \\ 0 & 2 & 0 \\ 1 & 2 & 3\end{array}\right]$ | $\mathrm{CO4}$ |

## Section-B

1. Each question will carry 10 Marks. All Questions of this section are compulsory. In Question 5, there is an internal choice.

| S. No. |  | CO |
| :---: | :---: | :---: |
| Q1 | Check for consistency and if possible, solve the following system of equations by Gauss elimination method: $\begin{aligned} 4 x-3 y-9 z+6 w & =0 \\ 2 x+3 y+3 z+6 w & =6 \\ 4 x-21 y-39 z-6 w & =-24 \end{aligned}$ | CO2 |
| Q2 | Solve the following system of equations using the Choleski LU decomposition method: $\begin{gathered} 4 x-y-z=3 \\ -x+4 y-3 z=-1 / 2 \\ -x-3 y+5 z=0 \end{gathered}$ | CO3 |
| Q3 | Find the algebraic and geometric multiplicity of all eigenvalues of the following matrix: $\left[\begin{array}{ccc} -3 & -7 & -5 \\ 2 & 4 & 3 \\ 1 & 2 & 2 \end{array}\right]$ | CO4 |
| Q4 | Find the characteristic and minimal polynomials of the following matrix: $A=\left[\begin{array}{lllll} 2 & 5 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 4 & 2 & 0 \\ 0 & 0 & 3 & 5 & 0 \\ 0 & 0 & 0 & 0 & 7 \end{array}\right]$ | CO5 |
| Q5 | Find the eigenvalues and eigenvectors of the matrix $A=\left[\begin{array}{lll}a & h & g \\ 0 & b & 0 \\ 0 & 0 & c\end{array}\right]$. <br> OR <br> Show that for any square matrix A , the product of all eigenvalues of A is equal to determinant of A. | CO4 |

Section-C

1. The question will carry 20 Marks. 2. Choose one question from two options.

| S. No. |  | CO |
| :--- | :--- | :--- | :--- |
| Q1 | Find the modal matrix $P$ and show that it diagonalizes the matrix $A=\left[\begin{array}{ccc}3 & 1 & -1 \\ -2 & 1 & 2 \\ 0 & 1 & 2\end{array}\right]$ by similarity |  |
|  | transformation $P^{-1} A P$. | OR |
|  | Find $A^{n}\left(n\right.$ is a positive integer) using Cayley Hamilton's theorem given that $A=\left[\begin{array}{ccc}1 & -1 & 2 \\ 0 & 2 & -1 \\ 0 & 0 & 3\end{array}\right]$. |  |

