

#### UNIVERSITY OF PETROLEUM AND ENERGY STUDIES

Supplementary Examination, Dec 2020

Course: Process Optimization (Elective) Semester: VI
Program: B. Tech. Chemical Engg. (spl. RP); CE-RP Time: 3 Hrs
Course Code: CHCE3020 (Elective) Max. Marks: 100

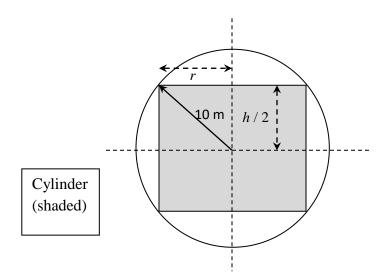
No. of pages: 3

**INSTRUCTIONS:** In this **OPEN BOOK(S)** (any number of books and kind) and **NOTES EXAM**, you are allowed to have any books, *all* handouts provided (including your textbook in xeroxed form), *your own class-notes* and your solutions to assignment problems, *etc.* 

- 1. Show all <u>intermediate steps</u> of your answers (and not just the final answers) to earn marks
- 2. **Please answer the questions in the sequence:** 1, 2, 3. You can do this by assigning, a priori, a few pages to each question, in the correct sequence. You may then answer the questions in whatever sequence you wish to, all parts in one place

### Section A: ANSWER ALL $2 \times 30 = 60$ Marks

Q.1 Find the optimum value of the radius, *r*, and height, *h*, of a cylinder (as shown in the diagram on the next page) which can be fully inscribed within a sphere of radius, 10 m. The optimum cylinder should have the maximum volume.



(30 *Points*)

# Q. 2 We wish to minimize

$$Min f(x_1, x_2) \equiv (x_1 - 2)^2 + (x_2 - 1)^2$$

with the *equality* constraint

$$g_1(x_1,x_2,x_3) \equiv x_1 + x_2 - x_3^2 - 3 = 0$$

Use the penalty function technique with  $\upsilon$  as the penalty parameter to

- (a) write the expression for the function, F, incorporating the constraint (5)
- (b) deduce *all* the equations for optimality (12)
- (c) solve these equations taking  $x_3 = 0$  (this leaves only three equations in three variables)

(8)

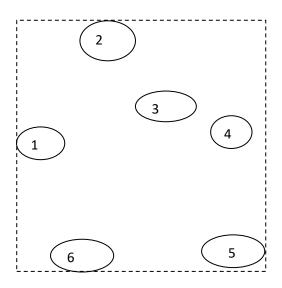
- (d) Solve these equations to give  $x_1$  and  $x_2$
- (e) Can you get a value of  $\upsilon$  (5)

(*30 points*)

## Section B: ANSWER ALL $1 \times 40 = 40$ Marks

## Q. 1 (Open-ended Problem again, possibly with several solutions)

We would like to solve the TSP (Travelling Salesman Problem) discussed in the Lecture using GA (and in Chapter 5 of the book), with Headquarter as Node 1, and five additional nodes/shops numbered 2, 3, 4, 5 and 6, as shown in the diagram below, using **Single-Objective Simulated Annealing (SSA)**.



Develop the algorithm you would use to minimize the total distance covered by the salesman from Node 1 and back to node 1 with the standard assumptions of the TSP. The coordinates,  $x_i$ ,  $y_i$ , are given for each node.

(40 *Points*)