| Name: <br> Enrolment No: |  |  |
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| Progr Cours Cours Nos. 0 | UNIVERSITY OF PETROLEUM AND ENERGY STUDIES <br> End Semester Examination, December 2020 | $\begin{aligned} & \text { II } \\ & \mathrm{hrs} \\ & 00 \end{aligned}$ |
| SECTION A(Attempt all questions; Each question carries 5 marks) |  |  |
| S. No. |  | CO |
| Q1. | Consider the set $S=\{1,2,3,4,6,9\}$. The maximal and minimal elements of the partial ordered set $(S, /)$ are <br> A. maximal elements $4,6,9$ and minimal element 1 <br> B. maximal element does not exist and minimal element 1 <br> C. maximal element 9 and minimum element 1 <br> D. None of these. | CO 3 |
| Q2. | The linear homogeneous recurrence relation with constant coefficients having its general solution as $a_{n}=c_{1} 3^{n}+\left(c_{2}+c_{3} n\right) 2^{n}$, where $c_{1}, c_{2}, c_{3}$ are arbitrary constants is given by <br> A. $a_{n+3}-7 a_{n+2}+16 a_{n+1}-12 a_{n}=0$ <br> B. $a_{n+3}+7 a_{n+2}+16 a_{n+1}+12 a_{n}=0$ <br> C. $a_{n+3}-11 a_{n+2}+16 a_{n+1}-12 a_{n}=0$ <br> D. $a_{n+3}-7 a_{n+2}+12 a_{n}=0$ | CO4 |
| Q3. | The proposition $(p \vee q) \wedge(\sim p) \wedge(\sim q)$ is <br> A. Tautology <br> B. Contradiction <br> C. Contingency <br> D. equivalent to $p$ | CO2 |
| Q4. | Inverse Laplace transform of $\frac{s^{2}-3 s+4}{s^{3}}$ is <br> A. $1-3 t+2 t^{2}$ <br> B. $1+3 t-2 t^{2}$ <br> C. $1-2 t+3 t^{2}$ <br> D. $1+2 t-3 t^{2}$ | CO1 |
| Q5. | If z-transform of $u_{n}, Z\left[u_{n}\right]=U(z)$, then $Z\left[a^{-n} u_{n}\right]$ is <br> A. $U(a z)$ <br> B. $U\left(\frac{a}{z}\right)$ <br> C. $U\left(\frac{z}{a}\right)$ <br> D. $U(z)$ | CO1 |
| Q6. | The sequence $\left\{a_{n}\right\}$ having generating function $\frac{x}{1-2 x}$ is given by ( $n=1,2,3, \ldots$ ) <br> A. $2^{n-1}$ <br> B. $2^{n}$ <br> C. $2^{n+1}$ <br> D. $n^{2}$ | $\mathrm{CO4}$ |

## SECTION B

(Q7-Q10 are compulsory and Q11 has internal choice; Each question carries $\mathbf{1 0}$ marks)

| Q7. | Consider the partial ordered set $A=\{1,2,3,4,5,6,7,8\}$ with the partial order relation $R=$ $\{(1,3),(2,3),(3,4),(3,5),(4,6),(4,7),(5,6),(5,7),(6,8),(7,8)\}$. <br> a. Draw Hasse diagram of $(A, R)$. <br> b. Find lower and upper bounds of the subset $B=\{3,4,5\}$ of $A$. <br> c. Find greatest lower bound (glb) and least upper bound (lub) of $B$. | $\mathrm{CO3}$ |
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| Q8. | Find the Laplace transform of $\int_{0}^{t} \frac{e^{-t} \sin t}{t} d t$. | CO1 |
| Q9. | Let $D_{n}$ denote the set of all the positive divisors of $n$. By constructing closure tables for lub $(\mathrm{V})$ and $\mathrm{glb}(\Lambda)$ show that $D_{15}$ is a lattice. | $\mathrm{CO3}$ |
| Q10. | Represent the following argument symbolically and determine whether the argument is valid. <br> "If I study, then I will pass the examination. If I do not go to cinema, then I will study. However, I failed in the examination. Therefore, I went to cinema." | CO 2 |
| Q11. | Using truth table, find the principal conjunctive normal form (penf) of $(p \vee \sim q \wedge \sim r) \vee(q \wedge r)$ <br> OR <br> Establish the following equivalence using truth table $(p \vee q) \rightarrow r \equiv(p \rightarrow r) \wedge(q \rightarrow r)$ | CO 2 |
| SECTION C(Q12a. and Q12b. both have internal choices; Each question carries 10 marks) |  |  |

Q12. a. Solve the following recurrence relation using generating function

$$
y_{n+2}-2 y_{n+1}+y_{n}=2^{n}, y_{0}=2, y_{1}=1
$$

OR
Given that generating function of the sequence $\left\{a_{n}\right\}$ is $G(x)$. Find the generating function of $\left\{a_{n+1}\right\},\left\{a_{n+2}\right\}$ and $\left\{a_{n+3}\right\}$.
b. Solve the recurrence relation of the Fibonacci sequence of the numbers $y_{n}=$ $y_{n-1}+y_{n-2}, n \geq 2$ with the initial conditions $y_{0}=0$ and $y_{1}=1$.

## OR

Solve the recurrence relation of the Lucas sequence of the numbers $y_{n}=$ $y_{n-1}+y_{n-2}, n \geq 2$ with the initial conditions $y_{0}=1$ and $y_{1}=3$.

