

Name:

Enrolment No:



**UNIVERSITY OF PETROLEUM AND ENERGY STUDIES**  
**End Semester Examination, May 2020**

**Course: Operations Research**

**Program: B.Tech – ADE**

**Course Code: ADEG461**

**Instructions:**

**Semester: VIII**

**Time 03 hrs.**

**Max. Marks: 100**

**SECTION A**

| S. No. |  | Marks    | CO          |          |   |     |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |
|--------|--|----------|-------------|----------|---|-----|--|--------|---|---|---|--------|--|---|---|---|---|---|--|---|---|---|---|---|--|---|---|---|---|---|--|---|---|---|---|----|--|--------|---|---|----|----|--|---|-----|
| Q 1    | <p>The initial basic feasible solution for the following transportation problem using NWCM is _____.</p> <table border="1"><thead><tr><th></th><th colspan="4">Destination</th><th></th></tr><tr><th>Source</th><th>A</th><th>B</th><th>C</th><th>Supply</th><th></th></tr></thead><tbody><tr><td>P</td><td>2</td><td>7</td><td>4</td><td>5</td><td></td></tr><tr><td>Q</td><td>3</td><td>3</td><td>1</td><td>8</td><td></td></tr><tr><td>R</td><td>5</td><td>4</td><td>7</td><td>7</td><td></td></tr><tr><td>S</td><td>1</td><td>6</td><td>2</td><td>14</td><td></td></tr><tr><td>Demand</td><td>7</td><td>9</td><td>18</td><td>34</td><td></td></tr></tbody></table> |          | Destination |          |   |     |  | Source | A | B | C | Supply |  | P | 2 | 7 | 4 | 5 |  | Q | 3 | 3 | 1 | 8 |  | R | 5 | 4 | 7 | 7 |  | S | 1 | 6 | 2 | 14 |  | Demand | 7 | 9 | 18 | 34 |  | 5 | CO3 |
|        | Destination  |          |             |          |   |     |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |
| Source | A  | B        | C           | Supply   |   |     |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |
| P      | 2  | 7        | 4           | 5        |   |     |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |
| Q      | 3  | 3        | 1           | 8        |   |     |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |
| R      | 5  | 4        | 7           | 7        |   |     |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |
| S      | 1  | 6        | 2           | 14       |   |     |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |
| Demand | 7  | 9        | 18          | 34       |   |     |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |
| Q 2    | <p>If you solve the following linear programming problem by graphical method<br/><math>\text{Max } Z = 5X + 7Y</math><br/>Subject to constraints,<br/><math>X + Y \leq 4</math><br/><math>3X + 8Y \leq 24</math><br/><math>10X + 7Y \leq 35</math><br/><math>X, Y \geq 0</math><br/>The optimal solution is <math>X = \underline{\hspace{1cm}}</math> , <math>Y = \underline{\hspace{1cm}}</math></p>  | 5        | CO2         |          |   |     |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |
| Q 3    | <p>For a game , the value of the pay-off matrix is given below</p> <table border="1"><tr><td></td><td></td><td>Player B</td></tr></table>  |          |             | Player B | 5 | CO4 |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |
|        |  | Player B |             |          |   |     |  |        |   |   |   |        |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |   |  |   |   |   |   |    |  |        |   |   |    |    |  |   |     |

|  |  | Player A                  | $\begin{bmatrix} -2 & 0 & 0 & 5 & 3 \\ 3 & 2 & 1 & 2 & 2 \\ -4 & -3 & 0 & -2 & 6 \\ 5 & 3 & -4 & 2 & -6 \end{bmatrix}$ |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
|--|--|---------------------------|--|-----|----|-----|----------|--------------------------|---------------------------|---------------------------|-----|---|---|----|-----|----|-----|----|---------|---|----|----|-----|----|---|----|-----|----|----|----|-----|---|---|----|-----|---|---|---|-----|---|---|----|-----|---|----|----|
| The value of the game is   |  |                           | (A) 2      (B) -4      (C) 3      (D) 1  |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| Q 4  | Customers arrive at a one-window drive-in bank according to Poisson distribution with mean 10 per hour. Service time per customer is exponential with mean 5 minutes. The traffic intensity is |                           |  |     | 5  | CO3 |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| (A) 0.55      (B) 0.35      (C) 0.83      (D) 0.25   |  |                           |  |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| Q 5  | Consider the following project   |                           |  |     | 5  | CO4 |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| <table border="1"> <thead> <tr> <th>Activity</th> <th>Optimistic time estimate</th> <th>Most likely time estimate</th> <th>Pessimistic time estimate</th> </tr> </thead> <tbody> <tr><td>1-2</td><td>3</td><td>6</td><td>15</td></tr> <tr><td>1-6</td><td>2</td><td>5</td><td>14</td></tr> <tr><td>2-3</td><td>6</td><td>12</td><td>30</td></tr> <tr><td>2-4</td><td>2</td><td>5</td><td>8</td></tr> <tr><td>3-5</td><td>5</td><td>11</td><td>17</td></tr> <tr><td>4-5</td><td>3</td><td>6</td><td>15</td></tr> <tr><td>5-8</td><td>1</td><td>4</td><td>7</td></tr> <tr><td>6-7</td><td>3</td><td>9</td><td>27</td></tr> <tr><td>7-8</td><td>4</td><td>19</td><td>28</td></tr> </tbody> </table> |  |                           |  |     |    |     | Activity | Optimistic time estimate | Most likely time estimate | Pessimistic time estimate | 1-2 | 3 | 6 | 15 | 1-6 | 2  | 5   | 14 | 2-3     | 6 | 12 | 30 | 2-4 | 2  | 5 | 8  | 3-5 | 5  | 11 | 17 | 4-5 | 3 | 6 | 15 | 5-8 | 1 | 4 | 7 | 6-7 | 3 | 9 | 27 | 7-8 | 4 | 19 | 28 |
| Activity   | Optimistic time estimate   | Most likely time estimate | Pessimistic time estimate  |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| 1-2  | 3  | 6                         | 15   |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| 1-6  | 2  | 5                         | 14   |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| 2-3  | 6  | 12                        | 30   |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| 2-4  | 2  | 5                         | 8  |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| 3-5  | 5  | 11                        | 17   |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| 4-5  | 3  | 6                         | 15   |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| 5-8  | 1  | 4                         | 7  |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| 6-7  | 3  | 9                         | 27   |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| 7-8  | 4  | 19                        | 28   |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| The critical path is   |  |                           |  |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| (A) 1-2-3-5-8      (B) 1-2-4-5-8      (C) 1-6-7-8      (D) None  |  |                           |  |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| Q 6  | In an assignment problem the time taken by different workers in completing the different jobs is given by  |                           |  |     | 5  | CO3 |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| <table border="1"> <thead> <tr> <th colspan="2"></th> <th colspan="4">Jobs</th> </tr> <tr> <th colspan="2"></th> <th>I</th> <th>II</th> <th>III</th> <th>IV</th> </tr> </thead> <tbody> <tr> <th rowspan="3">Workers</th> <th>A</th> <td>8</td> <td>10</td> <td>12</td> <td>16</td> </tr> <tr> <th>B</th> <td>11</td> <td>11</td> <td>15</td> <td>8</td> </tr> <tr> <th>C</th> <td>9</td> <td>6</td> <td>5</td> <td>14</td> </tr> </tbody> </table>  |  |                           |  |     |    |     |          |                          | Jobs                      |                           |     |   |   |    | I   | II | III | IV | Workers | A | 8  | 10 | 12  | 16 | B | 11 | 11  | 15 | 8  | C  | 9   | 6 | 5 | 14 |     |   |   |   |     |   |   |    |     |   |    |    |
|  |  | Jobs                      |  |     |    |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
|  |  | I                         | II   | III | IV |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
| Workers  | A  | 8                         | 10   | 12  | 16 |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
|  | B  | 11                        | 11   | 15  | 8  |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |
|  | C  | 9                         | 6  | 5   | 14 |     |          |                          |                           |                           |     |   |   |    |     |    |     |    |         |   |    |    |     |    |   |    |     |    |    |    |     |   |   |    |     |   |   |   |     |   |   |    |     |   |    |    |

|                  |  |           |            |    |   |   |  |  |
|------------------|--|-----------|------------|----|---|---|--|--|
|                  | <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>D</td> <td>15</td> <td>14</td> <td>9</td> <td>7</td> </tr> </table> <p>The total time taken to complete the jobs is</p> <p>(A) 42      (B) 54      (C) 31      (D) 28</p> | D         | 15         | 14 | 9 | 7 |  |  |
| D                | 15   | 14        | 9          | 7  |   |   |  |  |
| <b>SECTION B</b> |  |           |            |    |   |   |  |  |
| Q 7              | Explain areas of application of Linear Programming.  | <b>10</b> | <b>CO1</b> |    |   |   |  |  |
| Q 8              | Differentiate Programme Evaluation and Review Technique (PERT) and Critical Path Method (CPM).   | <b>10</b> | <b>CO2</b> |    |   |   |  |  |
| Q 9              | Explain the terms queue length, system length and traffic intensity.   | <b>10</b> | <b>CO1</b> |    |   |   |  |  |
| Q 10             | Explain properties of a game.  | <b>10</b> | <b>CO2</b> |    |   |   |  |  |
| Q 11             | Write different steps to solve LPP by simplex method.  | <b>10</b> | <b>CO2</b> |    |   |   |  |  |
| <b>SECTION C</b> |  |           |            |    |   |   |  |  |
| Q 12             | Classify the queueing models with the help of suitable examples.   | <b>20</b> | <b>CO3</b> |    |   |   |  |  |