| Name: <br> Enrolment No: |  |  |  |
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| UNIVERSITY OF PETROLEUM AND ENERGY STUDIES <br> End Semester Examination, December 2019  <br> Course: FORMAL LANGUAGES AND AUTOMATA THEORY  |  |  |  |
| SECTION A |  |  |  |
| S. No. |  | Marks | CO |
| Q 1 | Construct RE where, $\mathrm{L}=\left\{\mathrm{a}^{\mathrm{m}} \mathrm{b}^{\mathrm{n}} \mid \mathrm{m}+\mathrm{n}=\right.$ odd and $\left.\|\mathrm{w}\| \mathrm{n}>2\right\}$ | 4 | CO2 |
| Q 2 | Design CFG for $\mathrm{L}=\left\{\mathrm{a}^{\mathrm{m}} \mathrm{b}^{\mathrm{n}} \mathrm{c}^{\mathrm{k}}, \mathrm{n}=\|\mathrm{m}-\mathrm{k}\|\right\}$ | 4 | CO3 |
| Q 3 | Design Minimum DFA $\left\{\mathrm{w}: \mathrm{na}(\mathrm{w}) \mathrm{mod} 3>\mathrm{nb}(\mathrm{w}) \bmod 2, \mathrm{w} €(\mathrm{a}+\mathrm{b})^{*}\right\}$ | 4 | CO1 |
| Q 4 | Construct Regular grammar for the language having input symbol $\sum=(a, b)$, and length of string is even. | 4 | CO2 |
| Q 5 | Explain closure properties of Recursive Enumerable Language under Intersection, Union, Concatenation and Complementation | 4 | CO 4 |
| SECTION B |  |  |  |
| Q 6. | Minimize following DFA using Myhill-Nerode Theorem | 10 | CO 2 |


| Q 7. | Explain Chomsky classification of Grammar with example. <br> OR <br> Use the pumping lemma to show that following languages are not context free. $\text { L1: }\left\{a^{i} b^{j} / j=i^{3}\right\}$ | 10 | CO1 |
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| Q 8. | Simplify given grammar and Convert to CNF $\mathrm{G} 2=\{\mathrm{S}->\mathrm{aA}\|\mathrm{bB}, \mathrm{~B}->\mathrm{bB}\| \varepsilon, \mathrm{A}->\mathrm{aA} \mid \varepsilon\}$ | 10 | CO 3 |
| Q 9. | For $\mathrm{S} \in(0+1)$ * let $\mathrm{d}(\mathrm{s})$ denote the decimal value of $\mathrm{s}(\mathrm{e} . \mathrm{g} . \mathrm{d}(101)=5)$. Let $\mathrm{L}=\left\{\mathrm{s} \in(0+1)^{*}\right.$ $\mathrm{d}(\mathrm{s}) \bmod 5=2$ and $\mathrm{d}(\mathrm{s}) \bmod 7!=4\}$. What is the type of language L? Explain. | 10 | $\mathrm{CO2}$ |
| SECTION-C |  |  |  |
| Q 10 | Design a non -deterministic PDA for accepting the language $\mathrm{L}=\left\{\mathrm{ww}^{\mathrm{R}} \mathrm{w} \in(\mathrm{a}+\mathrm{b})^{+}\right\}$. | 20 | CO 3 |
| Q 11 | Construct a Turing Machine for language $\mathrm{L}=\{\mathrm{ww} \mid \mathrm{w} \in\{0,1\}\}$ <br> OR <br> Construct a Turing machine for $\mathrm{L}=\left\{\mathrm{a}^{\mathrm{n}} \mathrm{b}^{\mathrm{n}} \mathrm{a}^{\mathrm{n}} \mid \mathrm{n}>0\right\}$ | 20 | CO4 |

