


<b>Name:</b>  <b>Enrolment No:</b>			
<b>UPES</b> <b>End Semester Examination, May 2025</b>			
<b>Course: ADVANCED QUANTUM MECHANICS</b> <b>Program: M.Sc. Physics</b> <b>Course Code: PHYS7032</b>	<b>Semester: II</b> <b>Time : 03 hrs.</b> <b>Max. Marks: 100</b>		
<b>Instructions:</b> <ul style="list-style-type: none"> <li>Attempt all questions in Section A, Section B and Section C.</li> <li>Support your answers with appropriate equations, diagrams, and derivations wherever necessary.</li> <li>Use standard scientific notation and units.</li> </ul>			
<b>SECTION A</b> <b>(5Qx4M=20Marks)</b>			
S. No.		<b>Marks</b>	<b>CO</b>
Q 1	State and explain the first-order correction to energy in non-degenerate time-independent perturbation theory.	4	1
Q 2	Write the basic principle of the variation method and explain its significance in quantum mechanics.	4	2
Q 3	Write the Dirac equation in covariant form and explain the physical significance of Dirac matrices.	4	2
Q 4	A beam of particles is scattered from a spherical potential well. Calculate the total scattering cross-section using the partial wave approximation.	4	3
Q 5	Calculate the total energy of a particle with the rest mass $m = 0.511$ MeV/c <sup>2</sup> and momentum $p = 1$ MeV/c.	4	3
<b>SECTION B</b> <b>(4Qx10M= 40 Marks)</b>			
Q 6	Derive the expression for the first-order correction to the wave function in non-degenerate perturbation theory.	10	1
Q 7	Consider two non-interacting identical particles in a one-dimensional infinite potential well of width L. If both are in the lowest two energy levels, write down the total wavefunctions for: a. Bosons b. Fermions	10	2
Q 8	Apply the variation method to estimate the ground state energy of the helium atom.	10	3
Q 9	Explain the symmetric and antisymmetric wavefunction and drive the Slater Determinant for N-particle system. Show that two fermions cannot occupy the same quantum state using the antisymmetric wavefunction.	10	3
<b>OR</b>			

	Using the Dirac matrices, show how the Dirac equation reduces to the Pauli equation in the non-relativistic limit.		
<b>SECTION-C</b> <b>(2Qx20M=40 Marks)</b>			
Q 10	a. Apply the concept of partial wave analysis in scattering theory. b. Derive an expression for the scattering amplitude and discuss its application to low energy scattering.	<b>10+10</b>	<b>3</b>
Q 11	Starting from the Klein-Gordon equation, derive its solution for a free particle and discuss the difficulties in physical interpretation. Compare it with the Dirac equation. <p style="text-align: center;"><b>OR</b></p> Derive the semi-classical expression for the transition rate of emission or absorption of radiation by an atom interacting with an electromagnetic field.	<b>20</b>	<b>3</b>